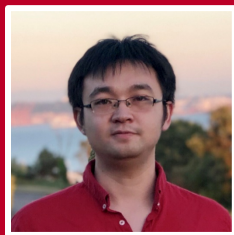
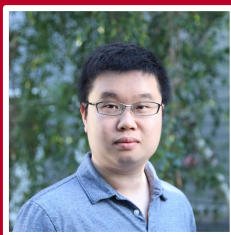


# Confidence Regularized Self-Training

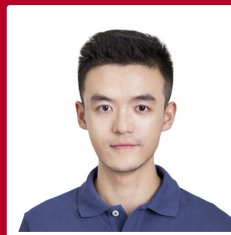
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Yang Zou



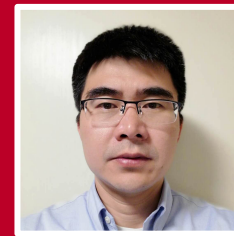
Zhiding Yu



Xiaofeng Liu



Vijayakumar  
Bhagavatula



Jinsong Wang

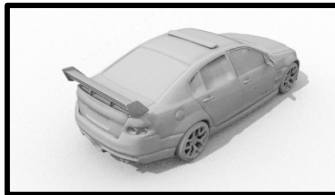


Carnegie Mellon University

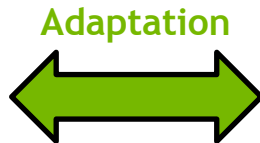


# Unsupervised Domain Adaptation (UDA)

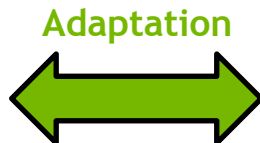
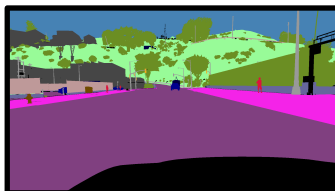
Image  
classification



Car



Semantic  
segmentation

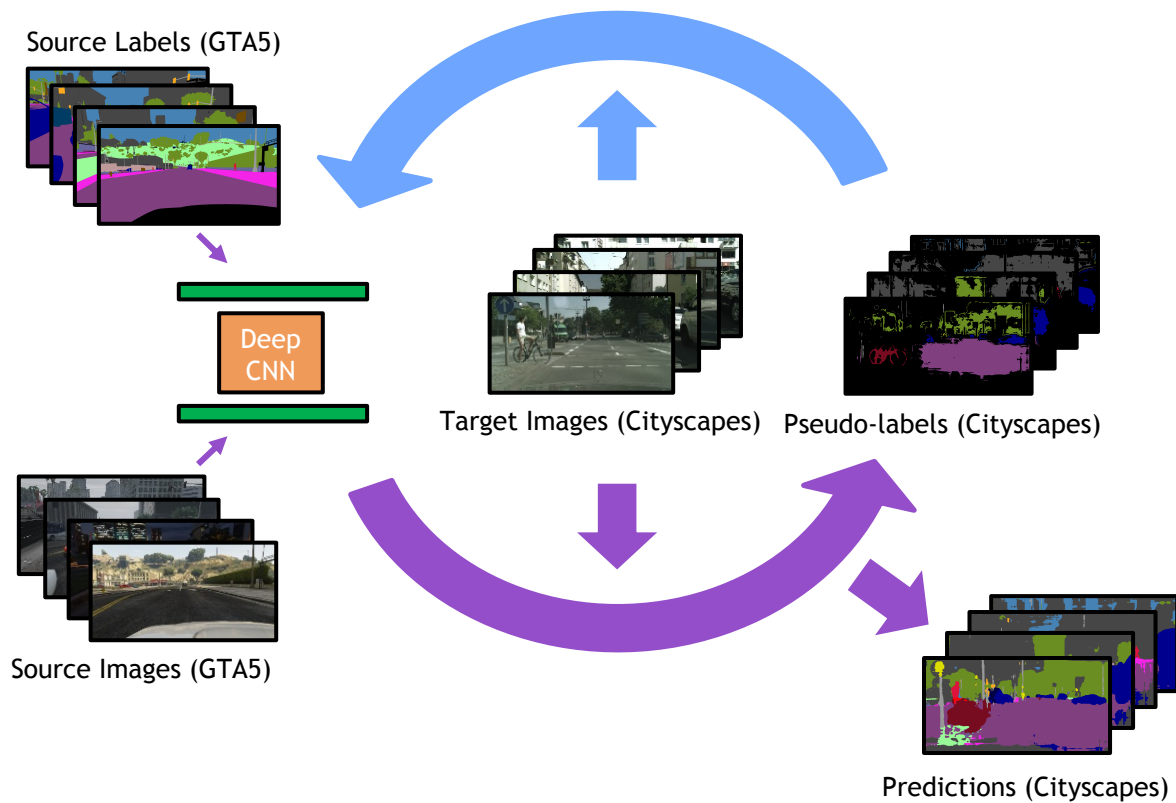


Source Domain (Labeled)

Target Domain (Unlabeled)

# UDA through Iterative Deep Self-Training

GTA5 → Cityscapes



# Class-Balanced Self-Training (CBST)

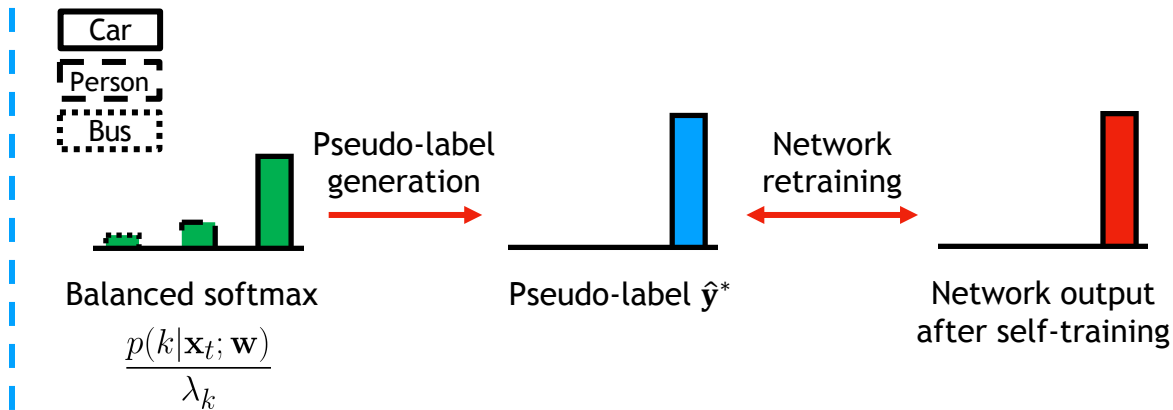
$$\min_{\mathbf{w}, \hat{\mathbf{Y}}_T} \mathcal{L}_{CB}(\mathbf{w}, \hat{\mathbf{Y}}_T) = - \sum_{s \in S} \sum_{k=1}^K y_s^{(k)} \log p(k|\mathbf{x}_s; \mathbf{w}) - \sum_{t \in T} \sum_{k=1}^K \hat{y}_t^{(k)} \log \frac{p(k|\mathbf{x}_t; \mathbf{w})}{\lambda_k}$$

$$s.t. \hat{\mathbf{y}}_t = (\hat{y}_t^{(1)}, \dots, \hat{y}_t^{(K)}) \in \Delta^{K-1} \cup \{\mathbf{0}\}, \forall t$$

$$\lambda_k > 0$$

**where:**  $\mathbf{x}$ : input sample  $\mathbf{p}$ : class predication vector  $\mathbf{y}$ : label vector  $\hat{\mathbf{y}}$ : pseudo-label vector  
 $\mathbf{w}$ : network parameters  $s$ : source sample index  $t$ : target sample index  $\Delta^{K-1}$ : probability simplex

$$\hat{y}_t^{(k)*} = \begin{cases} 1, & \text{if } k = \arg \max_k \left\{ \frac{p(k|\mathbf{x}_t; \mathbf{w})}{\lambda_k} \right\} \\ & \text{and } p(k|\mathbf{x}_t; \mathbf{w}) > \lambda_k \\ 0, & \text{otherwise} \end{cases}$$



# Issues in Self-Training: Overconfident Mistakes



Sample from BDD100K

Green: Correctly classified

Red: Misclassified



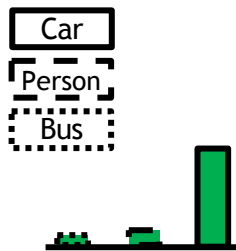
Samples from VisDA-17 (With label "Car")



Image label: car



Backbone Network



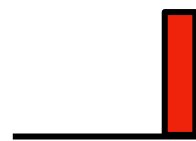
Network output before self-training

Pseudo-label generation



Pseudo-label

Network retraining



Sharp output after self-training

# Label Regularized Self-Training (LR)

$$\min_{\mathbf{w}, \hat{\mathbf{Y}}_T} \mathcal{L}_{LR}(\mathbf{w}, \hat{\mathbf{Y}}_T) = - \sum_{s \in S} \sum_{k=1}^K y_s^{(k)} \log p(k|\mathbf{x}_s; \mathbf{w}) - \sum_{t \in T} \left[ \sum_{k=1}^K \hat{y}_t^{(k)} \log \frac{p(k|\mathbf{x}_t; \mathbf{w})}{\lambda_k} - \alpha r_c(\hat{\mathbf{y}}_t) \right]$$

$$s.t. \hat{\mathbf{y}}_t = (\hat{y}_t^{(1)}, \dots, \hat{y}_t^{(K)}) \in \Delta^{K-1} \cup \{\mathbf{0}\}, \forall t$$

$$\lambda_k > 0$$

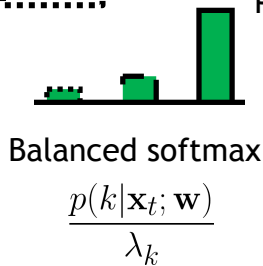
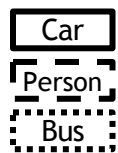
where:  $\alpha$ : regularizer weight

$$\mathcal{C}(\hat{\mathbf{y}}_t) = -\hat{y}_t^{(k)} \sum_{k=1}^K \log \frac{p(k|\mathbf{x}_t; \mathbf{w})}{\lambda_k} + \alpha r_c(\hat{\mathbf{y}}_t)$$

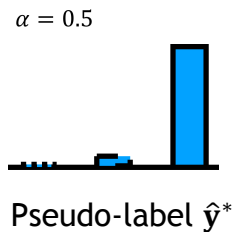
$$\hat{\mathbf{y}}_t^\dagger = \arg \min_{\hat{\mathbf{y}}_t} \mathcal{C}(\hat{\mathbf{y}}_t)$$

$$s.t. \hat{\mathbf{y}}_t \in \Delta^{(K-1)}, \forall t$$

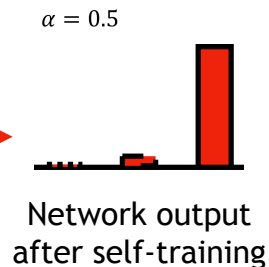
$$\hat{\mathbf{y}}_t^* = \begin{cases} \hat{\mathbf{y}}_t^\dagger, & \text{if } \mathcal{C}(\hat{\mathbf{y}}_t^\dagger) < \mathcal{C}(\mathbf{0}) \\ \mathbf{0}, & \text{otherwise} \end{cases}$$



Pseudo-label generation



Network retraining



# Model Regularized Self-Training (MR)

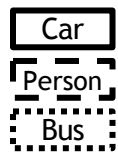
$$\min_{\mathbf{w}, \hat{\mathbf{Y}}_T} \mathcal{L}_{MR}(\mathbf{w}, \hat{\mathbf{Y}}_T) = - \sum_{s \in S} \sum_{k=1}^K y_s^{(k)} \log p(k|\mathbf{x}_s; \mathbf{w}) - \sum_{t \in T} \left[ \sum_{k=1}^K \hat{y}_t^{(k)} \log \frac{p(k|\mathbf{x}_t; \mathbf{w})}{\lambda_k} - \alpha r_c(p(\mathbf{x}_t; \mathbf{w})) \right]$$

$$s.t. \hat{\mathbf{y}}_t = (\hat{y}_t^{(1)}, \dots, \hat{y}_t^{(K)}) \in \Delta^{K-1} \cup \{\mathbf{0}\}, \forall t$$

$$\lambda_k > 0$$

where:  $\alpha$ : regularizer weight

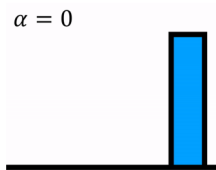
$$\min_{\mathbf{w}} - \sum_{t \in T} \left[ \sum_{k=1}^K \hat{y}_t^{(k)} \log p(k|\mathbf{x}_t; \mathbf{w}) - \alpha r_c(p(\mathbf{x}_t; \mathbf{w})) \right]$$



Balanced softmax

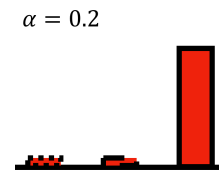
$$\frac{p(k|\mathbf{x}_t; \mathbf{w})}{\lambda_k}$$

Pseudo-label generation



Pseudo-label  $\hat{\mathbf{y}}^*$

Network retraining



Network output after self-training

# Proposed Confidence Regularizers

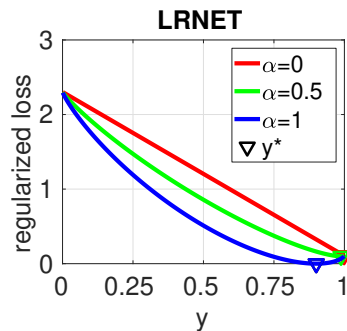
**LR-Entropy (LRENT)**  $r_c(\hat{\mathbf{y}}_t) = \sum_{k=1}^K \hat{y}_t^{(k)} \log(\hat{y}_t^{(k)})$

**Pseudo-label solver**  $\hat{y}_t^{(i)\dagger} = \frac{\left(\frac{p(i|\mathbf{x}_t)}{\lambda_k}\right)^{\frac{1}{\alpha}}}{\sum_{k=1}^K \left(\frac{p(k|\mathbf{x}_t)}{\lambda_k}\right)^{\frac{1}{\alpha}}}$

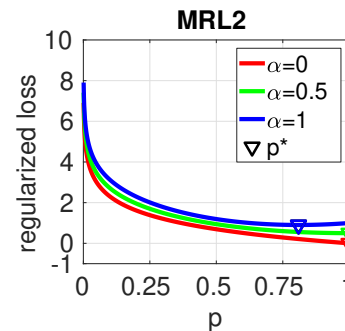
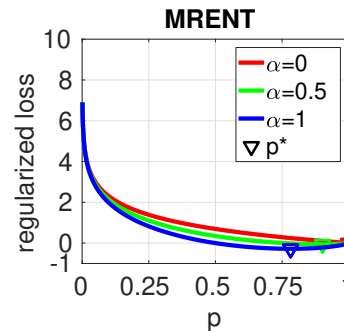
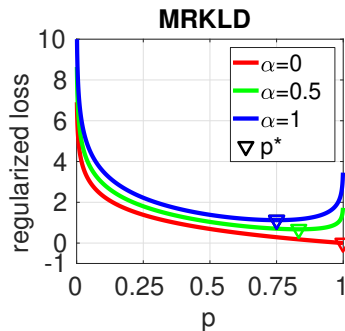
**MR-KLDiv (MRKLD)**  $r_c(p(\mathbf{x}_t; \mathbf{w})) = -\sum_{k=1}^K \frac{1}{K} \log p(k|\mathbf{x}_t)$

**MR-Entropy (MRENT)**  $r_c(p(\mathbf{x}_t; \mathbf{w})) = \sum_{k=1}^K p(k|\mathbf{x}_t) \log p(k|\mathbf{x}_t)$

**MR-L2 (MRL2)**  $r_c(p(\mathbf{x}_t; \mathbf{w})) = \sum_{k=1}^K p(k|\mathbf{x}_t)^2$



Pseudo-label generation loss  
v.s. probability



Regularized retraining loss  
v.s. probability



# Theoretical Analysis

## Probabilistic Explanation

**Proposition 1.** CRST can be modeled as a regularized maximum likelihood for classification (RCML) problem optimized via classification expectation maximization.

## Convergence Analysis

**Proposition 2.** Given pre-determined  $\lambda_k$ 's, CRST is convergent with gradient descent for network retraining optimization.

# Experiment: UDA for Image Classification

## Results on VisDA-17

Method	Aero	Bike	Bus	Car	Horse	Knife	Motor	Person	Plant	Skateboard	Train	Truck	Mean
Source [50]	55.1	53.3	61.9	59.1	80.6	17.9	79.7	31.2	81.0	26.5	73.5	8.5	52.4
MMD [33]	87.1	63.0	76.5	42.0	90.3	42.9	85.9	53.1	49.7	36.3	85.8	20.7	61.1
DANN [15]	81.9	77.7	82.8	44.3	81.2	29.5	65.1	28.6	51.9	54.6	82.8	7.8	57.4
ENT [18]	80.3	75.5	75.8	48.3	77.9	27.3	69.7	40.2	46.5	46.6	79.3	16.0	57.0
MCD [51]	87.0	60.9	<b>83.7</b>	64.0	88.9	79.6	84.7	<b>76.9</b>	<b>88.6</b>	40.3	83.0	25.8	71.9
ADR [50]	87.8	79.5	<b>83.7</b>	65.3	<b>92.3</b>	61.8	<b>88.9</b>	73.2	87.8	60.0	<b>85.5</b>	32.3	74.8
SimNet-Res152 [44]	<b>94.3</b>	82.3	73.5	47.2	87.9	49.2	75.1	79.7	85.3	68.5	81.1	50.3	72.9
GTA-Res152 [53]	-	-	-	-	-	-	-	-	-	-	-	-	77.1
Source-Res101	68.7	36.7	61.3	<b>70.4</b>	67.9	5.9	82.6	25.5	75.6	29.4	83.8	10.9	51.6
CBST	87.2±2.4	78.8±1.0	56.5±2.2	55.4±3.6	85.1±1.4	79.2±10.3	83.8±0.4	77.7±4.0	82.8±2.8	88.8±3.2	69.0±2.9	72.0±3.8	76.4±0.9
MRL2	87.0±2.9	79.5±1.9	57.1±3.2	54.7±2.9	85.5±1.1	78.1±11.7	83.0±1.5	77.7±3.7	82.4±1.7	88.6±2.7	69.1±2.2	71.8±3.0	76.2±1.0
MRENT	87.1±2.7	78.3±0.7	56.1±4.0	54.4±2.7	84.4±2.3	79.9±10.6	80.7±1.1	77.9±4.4	82.7±2.4	87.4±2.8	70.0±1.4	72.8±3.3	76.2±0.8
MRKLD	87.3±2.5	79.4±1.9	60.5±2.4	59.7±2.5	87.6±1.4	<b>82.4±4.4</b>	86.5±1.1	78.4±2.6	84.6±1.7	86.4±2.8	72.5±2.4	69.8±2.5	77.9±0.5
LRNT	87.7±2.4	78.7±0.8	57.3±3.3	54.5±4.0	84.8±1.7	79.7±10.3	84.2±1.4	77.4±3.7	83.1±1.5	<b>88.3±2.6</b>	70.9±2.1	<b>72.6±2.4</b>	76.6±0.9
MRKLD+LRNT	88.0±0.6	79.2±2.2	61.0±3.1	60.0±1.0	87.5±1.2	81.4±5.6	86.3±1.5	78.8±2.1	85.6±0.9	86.6±2.5	73.9±1.3	68.8±2.3	<b>78.1±0.2</b>

## Results on Office-31

Method	A→W	D→W	W→D	A→D	D→A	W→A	Mean
ResNet-50 [21]	68.4±0.2	96.7±0.1	99.3±0.1	68.9±0.2	62.5±0.3	60.7±0.3	76.1
DAN [33]	80.5±0.4	97.1±0.2	99.6±0.1	78.6±0.2	63.6±0.3	62.8±0.2	80.4
RTN [35]	84.5±0.2	96.8±0.1	99.4±0.1	77.5±0.3	66.2±0.2	64.8±0.3	81.6
DANN [15]	82.0±0.4	96.9±0.2	99.1±0.1	79.7±0.4	68.2±0.4	67.4±0.5	82.2
ADDA [61]	86.2±0.5	96.2±0.3	98.4±0.3	77.8±0.3	69.5±0.4	68.9±0.5	82.9
JAN [36]	85.4±0.3	97.4±0.2	99.8±0.2	84.7±0.3	68.6±0.3	70.0±0.4	84.3
GTA [53]	<b>89.5±0.5</b>	97.9±0.3	99.8±0.4	87.7±0.5	72.8±0.3	71.4±0.4	86.5
CBST	87.8±0.8	98.5±0.1	<b>100±0.0</b>	86.5±1.0	71.2±0.4	70.9±0.7	85.8
MRL2	88.4±0.2	98.6±0.1	<b>100±0.0</b>	87.7±0.9	71.8±0.2	<b>72.1±0.2</b>	86.4
MRENT	88.0±0.4	98.6±0.1	<b>100±0.0</b>	87.4±0.8	<b>72.7±0.2</b>	71.0±0.4	86.4
MRKLD	88.4±0.9	98.7±0.1	<b>100±0.0</b>	88.0±0.9	71.7±0.8	70.9±0.4	86.3
LRNT	88.6±0.4	98.7±0.1	<b>100±0.0</b>	<b>89.0±0.8</b>	72.0±0.6	71.0±0.3	86.6
MRKLD+LRNT	89.4±0.7	<b>98.9±0.4</b>	<b>100±0.0</b>	88.7±0.8	72.6±0.7	70.9±0.5	<b>86.8</b>

# Experiment: UDA for Semantic Segmentation

## Results on SYNTHIA -> Cityscapes (mIoU\* - 13 class)

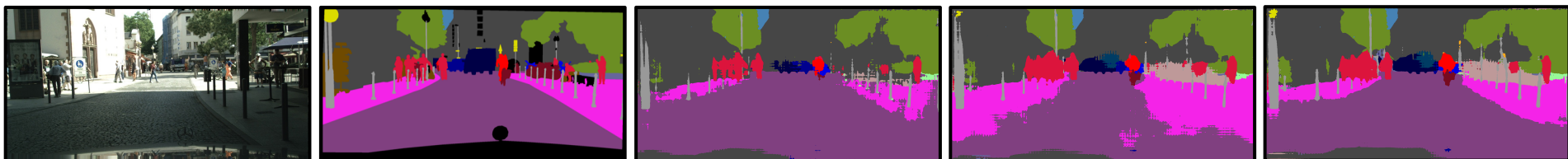
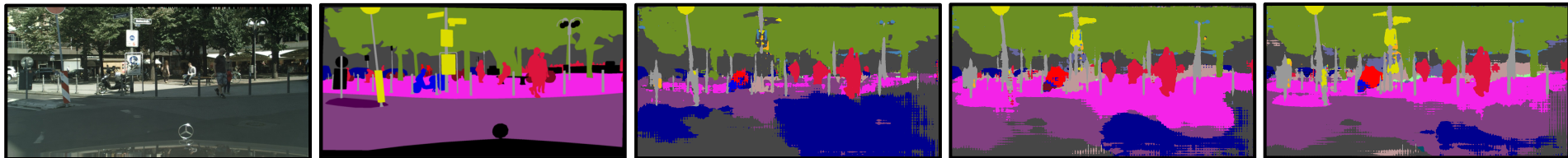
Method	Backbone	Road	SW	Build	Wall*	Fence*	Pole*	TL	TS	Veg.	Sky	PR	Rider	Car	Bus	Motor	Bike	mIoU	mIoU*
Source	DRN-105	14.9	11.4	58.7	1.9	0.0	24.1	1.2	6.0	68.8	76.0	54.3	7.1	34.2	15.0	0.8	0.0	23.4	26.8
MCD [51]		84.8	<b>43.6</b>	79.0	3.9	0.2	29.1	7.2	5.5	83.8	83.1	51.0	11.7	79.9	27.2	6.2	0.0	37.3	43.5
Source	DeepLabv2	55.6	23.8	74.6	-	-	-	6.1	12.1	74.8	79.0	55.3	19.1	39.6	23.3	13.7	25.0	-	38.6
AdaptSegNet [60]		84.3	42.7	77.5	-	-	-	4.7	7.0	77.9	82.5	54.3	21.0	72.3	32.2	18.9	32.3	-	46.7
AdvEnt [63]	DeepLabv2	<b>85.6</b>	42.2	<b>79.7</b>	8.7	0.4	25.9	5.4	8.1	80.4	<b>84.1</b>	57.9	23.8	73.3	<b>36.4</b>	14.2	33.0	41.2	48.0
Source	ResNet-38	32.6	21.5	46.5	4.8	0.1	26.5	14.8	13.1	70.8	60.3	56.6	3.5	74.1	20.4	8.9	13.1	29.2	33.6
CBST [69]		53.6	23.7	75.0	12.5	0.3	36.4	23.5	26.3	<b>84.8</b>	74.7	<b>67.2</b>	17.5	<b>84.5</b>	28.4	15.2	<b>55.8</b>	42.5	48.4
Source	DeepLabv2	64.3	21.3	73.1	2.4	1.1	31.4	7.0	<b>27.7</b>	63.1	67.6	42.2	19.9	73.1	15.3	10.5	38.9	34.9	40.3
CBST		68.0	29.9	76.3	10.8	1.4	33.9	22.8	<b>29.5</b>	77.6	78.3	60.6	28.3	81.6	23.5	18.8	39.8	42.6	48.9
MRL2		63.4	27.1	76.4	14.2	1.4	35.2	<b>23.6</b>	29.4	78.5	77.8	61.4	<b>29.5</b>	82.2	22.8	18.9	42.3	42.8	48.7
MRENT		69.6	32.6	75.8	12.2	<b>1.8</b>	35.3	23.3	<b>29.5</b>	77.7	77.9	60.0	28.5	81.5	25.9	19.6	41.8	43.4	49.6
MRKLD		67.7	32.2	73.9	10.7	1.6	<b>37.4</b>	22.2	31.2	80.8	<b>80.5</b>	<b>60.8</b>	29.1	82.8	25.0	19.4	45.3	<b>43.8</b>	<b>50.1</b>
LRENT		65.6	30.3	74.6	<b>13.8</b>	1.5	35.8	23.1	29.1	77.0	77.5	60.1	28.5	82.2	22.6	<b>20.1</b>	41.9	42.7	48.7

## Results on GTA5 -> Cityscapes

Method	Backbone	Road	SW	Build	Wall	Fence	Pole	TL	TS	Veg.	Terrain	Sky	PR	Rider	Car	Truck	Bus	Train	Motor	Bike	mIoU	
Source	DRN-26	42.7	26.3	51.7	5.5	6.8	13.8	23.6	6.9	75.5	11.5	36.8	49.3	0.9	46.7	3.4	5.0	0.0	5.0	1.4	21.7	
CyCADA [23]		79.1	33.1	77.9	23.4	17.3	32.1	33.3	31.8	81.5	26.7	69.0	62.8	14.7	74.5	20.9	25.6	6.9	18.8	20.4	39.5	
Source	DRN-105	36.4	14.2	67.4	16.4	12.0	20.1	8.7	0.7	69.8	13.3	56.9	37.0	0.4	53.6	10.6	3.2	0.2	0.9	0.0	22.2	
MCD [51]		90.3	31.0	78.5	19.7	17.3	28.6	30.9	16.1	83.7	30.0	69.1	58.5	19.6	81.5	23.8	30.0	5.7	25.7	14.3	39.7	
Source	DeepLabv2	75.8	16.8	77.2	12.5	21.0	25.5	30.1	20.1	81.3	24.6	70.3	53.8	26.4	49.9	17.2	25.9	6.5	25.3	36.0	36.6	
AdaptSegNet [60]		86.5	36.0	79.9	23.4	23.3	23.9	35.2	14.8	83.4	33.3	75.6	58.5	27.6	73.7	32.5	35.4	3.9	30.1	28.1	42.4	
AdvEnt [63]	DeepLabv2	89.4	33.1	<b>81.0</b>	26.6	26.8	27.2	33.5	24.7	83.9	<b>36.7</b>	78.8	58.7	30.5	84.8	38.5	44.5	1.7	31.6	32.4	45.5	
Source	DeepLabv2	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	29.2
FCAN [67]		-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-
Source	DeepLabv2	71.3	19.2	69.1	18.4	10.0	35.7	27.3	6.8	79.6	24.8	72.1	57.6	19.5	55.5	15.5	15.1	11.7	21.1	12.0	33.8	
CBST		91.8	53.5	80.5	32.7	21.0	34.0	28.9	20.4	83.9	34.2	80.9	53.1	24.0	82.7	30.3	35.9	16.0	25.9	42.8	45.9	
MRL2		<b>91.9</b>	55.2	80.9	32.1	21.5	36.7	30.0	19.0	84.8	34.9	80.1	56.1	23.8	83.9	28.0	29.4	20.5	24.0	40.3	46.0	
MRENT		91.8	53.4	80.6	32.6	20.8	34.3	29.7	21.0	84.0	34.1	80.6	53.9	24.6	82.8	30.8	34.9	16.6	26.4	42.6	46.1	
MRKLD		91.0	<b>55.4</b>	80.0	33.7	21.4	37.3	32.9	24.5	<b>85.0</b>	34.1	80.8	57.7	24.6	84.1	27.8	30.1	26.9	26.0	42.3	47.1	
LRENT		91.8	53.5	80.5	32.7	21.0	34.0	29.0	20.3	83.9	34.2	<b>80.9</b>	53.1	23.9	82.7	30.2	35.6	16.3	25.9	42.8	45.9	
Source	ResNet-38	70.0	23.7	67.8	15.4	18.1	40.2	41.9	25.3	78.8	11.7	31.4	62.9	29.8	60.1	21.5	26.8	7.7	28.1	12.0	35.4	
CBST [69]		86.8	46.7	76.9	26.3	24.8	42.0	46.0	38.6	80.7	15.7	48.0	57.3	27.9	78.2	24.5	49.6	17.7	25.5	45.1	45.2	
MRL2		84.4	52.7	74.7	38.0	<b>32.2</b>	43.7	<b>53.7</b>	38.6	73.9	24.4	64.4	45.6	24.6	63.2	3.22	31.9	<b>45.9</b>	44.2	34.8	46.0	
MRENT		84.6	49.5	73.9	<b>35.8</b>	25.1	<b>46.2</b>	53.3	43.3	75.2	24.2	63.8	48.2	<b>33.8</b>	65.7	2.89	32.6	39.2	<b>50.0</b>	34.7	46.4	
MRKLD		84.5	47.7	74.1	27.9	22.1	43.8	46.5	37.8	<b>83.7</b>	22.7	56.1	56.8	26.8	81.7	22.5	46.2	27.5	32.3	<b>47.9</b>	46.8	
LRENT		80.3	40.8	65.8	24.6	30.5	43.1	49.5	40.3	82.1	26.0	54.6	59.4	32.1	68.0	31.9	30.0	21.9	44.8	46.7	45.9	
Source	ResNet-38	85.6	55.1	76.9	26.8	23.4	38.9	47.1	<b>46.9</b>	83.4	25.5	68.7	45.6	15.7	79.7	27.7	50.3	38.2	33.4	44.6	48.1	
MRKLD-SP		90.8	46.0	79.9	27.4	23.3	42.3	46.2	40.9	83.5	19.2	59.1	63.5	30.8	83.5	36.8	<b>52.0</b>	28.0	36.8	46.4	49.2	
MRKLD-SP-MST		91.7	45.1	80.9	29.0	23.4	43.8	47.1	40.9	84.0	20.0	60.6	<b>64.0</b>	31.9	<b>85.8</b>	<b>39.5</b>	48.7	25.0	38.0	47.0	<b>49.8</b>	

# Experiment: Qualitative Results (GTA5 -> Cityscapes)

road	sidewalk	building	wall	fence	pole	traffic lgt	traffic sgn	vegetation	ignored
terrain	sky	person	rider	car	truck	bus	train	motorcycle	bike



Original Image

Ground Truth

Source Model

CBST

CRST (MRKLD)

# Conclusions and Future Works

## Conclusions

- Compared with supervised learning, self-training is an under-determined problem (EM with latent variables).
- Our work shows the importance of confidence regularizations as inductive biases to help under-constrained problems such as unsupervised domain adaptation and semi-supervised learning.
- CRST is still aligned with entropy minimization. The proposed confidence regularization only serves as a safety measure to prevent over self-training/entropy minimization.
- MR-KLD is most recommended in practice for its efficiency and good performance.

## Future Works

- This work could potentially inspire many other meaningful regularizations/inductive biases for similar problems.