

# Diversions on the minimum spanning tree with mstree

Nicholas Lewin-Koh<sup>1,\*</sup>

1. Genentech, 1 DNA way, South San Francisco, CA 94080

\*Contact author: nikko@hailmail.net

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The minimum spanning tree (MST), is the tree that covers all points with minimum distance or cost. There are many results on the MST that relate to clustering, ordering of data, and dimension reduction. This package provides several functions for doing analysis on the MST.

The package is designed around a C core set of functions for calculating the MST. A variation on Primm's algorithm is used with a Fibonacci heap based on code by Ben Pfaff. The interface will accept a numeric matrix and calculate Euclidean distance, or a `dist` object and return the MST as a vector of integers as in the similar Splus function `mstree`. The function also returns the linear and radial node orderings of Friedman and Rafsky (1981) as well as the optimal ordering as proven by Shiloach (1979) and Chung (1983).

Further functions calculate the runt distribution of the MST edges. These can be used to prune the cluster tree of a density as outlined in Stuetzle 2003. Other functions using the MST may be added in the future.

## References

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