

Modeling & Control of Launch Vehicles

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Perspectives In Dynamical Systems & Control

Outline

□ ISRO Missions

ISRO Launch Vehicles

- Structure Configuration (PSLV / GSLV / RLV)
- Propulsion Configuration
- Aerodynamics
- Actuation Systems
- Navigation systems
- Trajectory Design Guidance & Control

Digital Auto-Pilot (DAP)

- Inputs for design
- Design problem
- Design specification
- Design methodology
- Control Configuration

Launch Vehicle Modelling

- Input Data
- Assumptions
- Rigid Body rotational dynamics
- Slosh
- □ Flexibility

Outline

RLV-TD (HEX) Mission

- Mission profile
- Different phase during descent
- RLV-TD dynamics

Non-linear Control

Design parameters

□ Implementation aspect

Control design & validation philosophy

Post flight analysis

□ Challenges in design

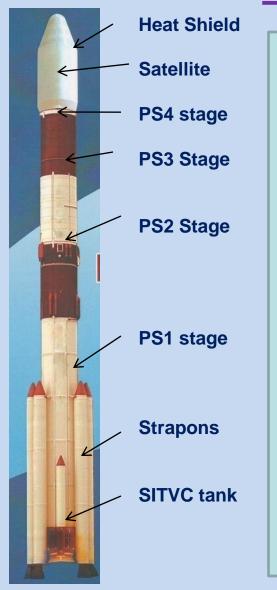
ISRO Missions

- ***** Sun Synchronous Polar Orbit (SSPO)
- Eastward Missions GTO
 Elliptical Orbits(Moon Mission/Mars Mission)
- ***** Space Capsule Recovery
- RLV Technology Demonstrator

ISRO Launch Vehicles

GSLV-Mix III Lift-off weight : 629 tonne Payload : 4 tonne PSLV into GTO GSLV Mk 1 & II Height : 42 Metre Lift-off Lift-off weight : 295 tonne weight :414 tonne Payload : 1600 Kg into Payload : 2 to 2.5 tonne 620 KM Polar Orbit, into GTO 3-1060 Kg into Height : 49 Metre Geosynchronous GSLV Transfer Orbit (GTO) 111 Height :44 Metre No-of SLV-3 ASLV N S D Lift-off Lift-off R ĩ INDIA weight :39 tonne weight : 17 tonne A 0 Payload : 150 Kg (LEO) Payload: 40 Kg to Height : 23.5 Metre Low Earth Orbit (LEO) भा Height : 22 Metre 7 ਸ਼ ਰ

PSLV Configuration



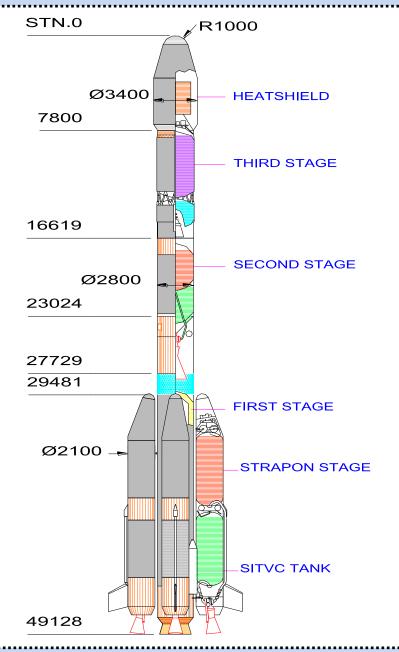
* Sensors

- Inertial navigation system
- Gyros(Attitude)
- Accelerometers

(Secondary injection Thrust Vector Control)

- Engine Gimbal Control
- Flex Nozzle control

GSLV-MK2 Configuration



Definition (4L40+S139)+L37.5+C12.5

Specification	
Overall length	: 49.128 m
Lift off Mass	: 401.8 t
GTO payload	: 1600 kg

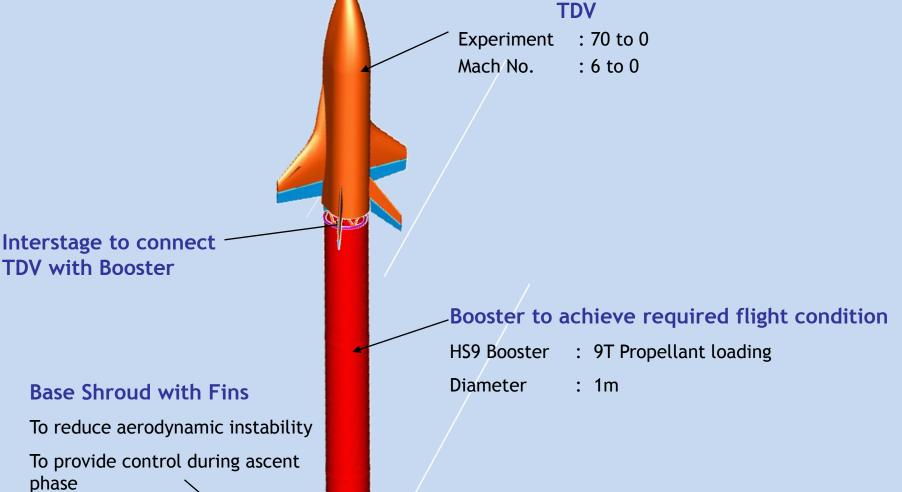
Sensors : RESINS at EB,

RGP at 1/2 M

Actuators: EGC(L40) EGC(L37.5),

CSCE, OSS





Propulsion/Configuration

- SLV-3: Core (S9) + 2nd stage solid + 3rd stage solid
- ASLV: Core (S9) + 2 Strapons (S9) + Solid Upper Stage
- PSLV: Core S139 (Solid) + 6 Strapons + PS2 (L37.5) + PS3 (Solid) + PS4 (L2.5)
- **GSLV:** Core S139 (Solid) + 4 L40 + Cryo (C12)
- Mk3: Core S200 (Solid) + 2 L110 + Cryo (C25)
- **RLV: Core** + **TDV** (No Propulsion)

Aerodynamics

- ***** SLV-3: Core with Fins
- ***** ASLV: Core with 2 Strapons in 1st stage
- ***** PSLV: Core alone & (Core + 6 Strapons)
- **GSLV:** Core + 4 liquid Strapons

Actuation Systems : Thrust Vector Control

- ***** SITVC (Secondary Injected Thrust Vector Control)
- Engine Gimbal Control
- Flex Nozzle Control
- ***** Vernier Engine Control
- Reaction Control System (On-Off Control)
- * Aerodynamic Surfaces

Navigation System

- *** RESINS:** Redundant Strap-down Inertial Navigation System
- *** RGP: Rate Gyro Package**
- LAP: Lateral Accelerometer Package

Trajectory Design – Guidance & Control

Guidance : Point Mass Trajectory

- Maximizing the payload
 - **Atmospheric Phase Flight**
- Dynamic Pressure Curve
- Structural Loads
- Heating Constraints
- Range Safety

Control:

Attitude Dynamics

Launch Vehicle (Pitch/Yaw/Roll) -

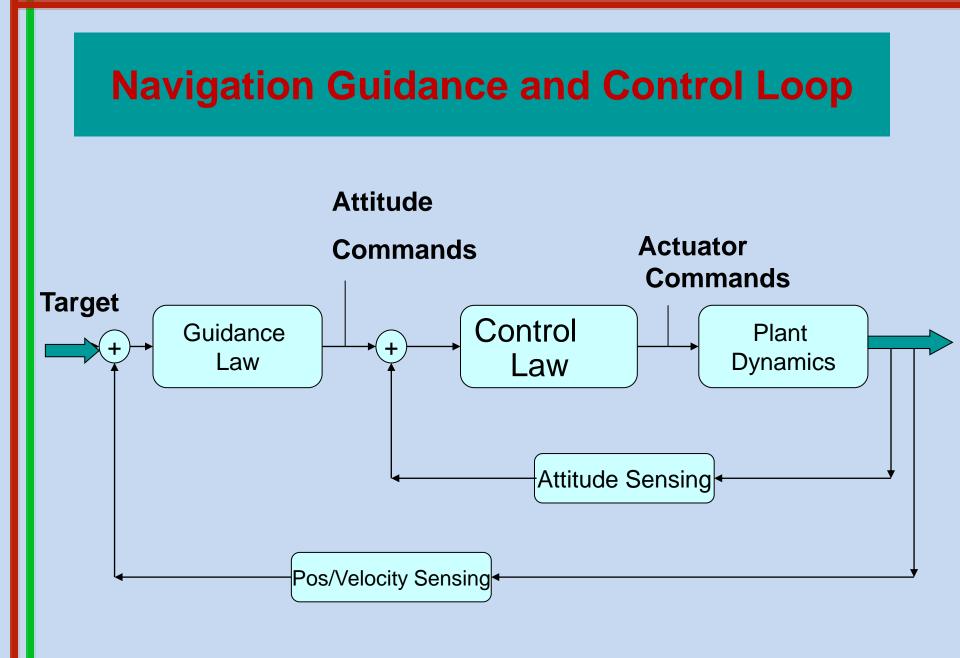
- Rigid Body
- Slosh
- Flexibility
- Engine dynamics (Actuator + Nozzle)

RLV-

- Longitudinal Dynamics
- Lateral/ Directional

Digital Auto-Pilot (DAP)

- Launch Vehicle Autopilot is an inner loop of the Navigation,
 Guidance and Control (NGC) subsystem.
- ***** Controls the Attitude of the vehicle in Pitch, Yaw and Roll channels from lift-off till end of flight.
- It ensures the stabilisation of the attitude in the presence of disturbing forces and moments caused by various sources.
 Steers the vehicle along a desired trajectory, maintaining the structural integrity.



Inputs for the Design

- Model of the System to be controlled
 - *Plant* : Rigid body, Flexibility, Slosh Dynamics
 - Actuators : SITVC, EGS, FNC, RCS
 - *Sensors* : RGP, RESINS, LAP

Disturbances

Thrust misalignment, CG offset, Differential Thrust, Winds

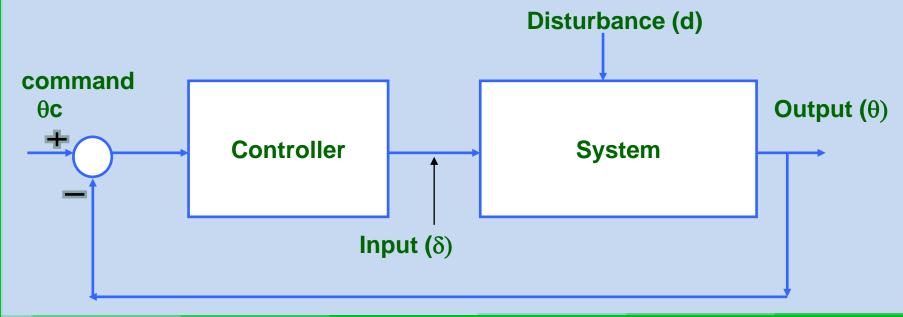
Tracking Commands

Generated by Guidance Law

Specifications

Design Problem

- Behavior of the output in presence of the disturbance may not be satisfactory
- Controller has to ensure satisfactory response of the system rejecting the disturbance
- ***** System will be modeled by using differential equations
- * The controller will process the input signal to achieve satisfactory output.



Design Specifications

- **Primary Specification**-Tracing Error < 1 Degree
- Robustness Specifications
- Rigid body

Aero margin > 6 dB Phase margin > 30 Degree Gain margin > 6 dB

Bending modes

Phase Margin > 40 Deg. : Phase Stabilisation

Attend. margin > 6 dB : *Gain Stabilisation*

Slosh modes

Phase margin > 30 Degree

Design Methodology

Classical Design Technique

Tracking Error Specification -Bandwidth / Damping Gain Design- PID

- Frequency Domain Design Roll off, Notch, Lag-Lead filter
- Analysis using Root Locus, Bode plot, Nyquist plot

Control Configuration

Control Power Plant

Physical Location / Alignment Control Force / Moment Dynamics

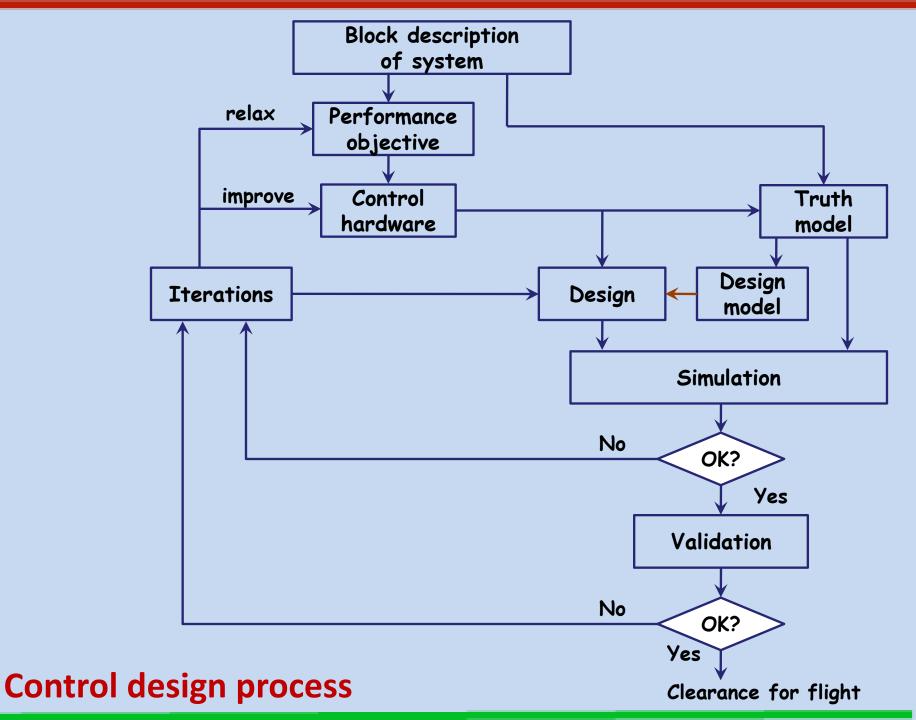
• Sensors

Placement Dynamics

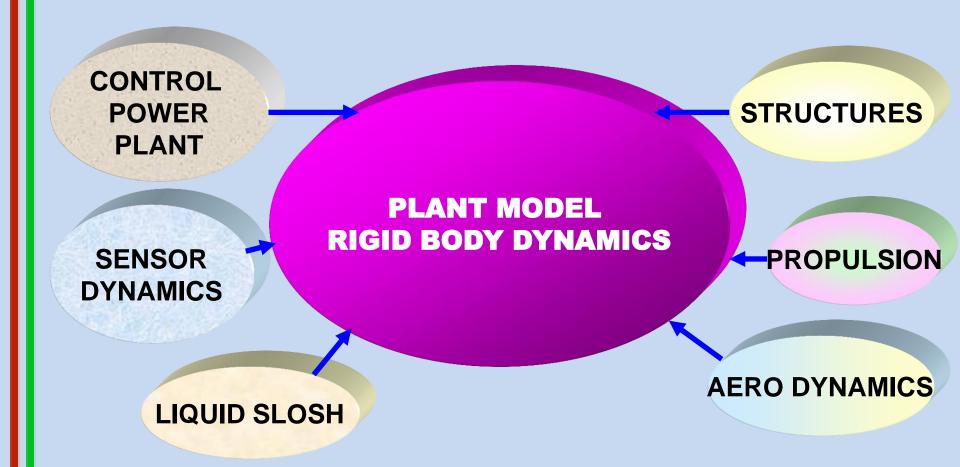
• Baffles

Placement Characteristics Design and development of Autopilot consists following important elements.

i). Mathematical model of vehicle dynamics
ii). Design to meet specifications
iii). On-board implementation of Autopilot Algorithm
iv). Validation



LAUNCH VEHICLE MODELLING



Launch Vehicle Modelling

Input Data:

Plant Model :Mass, Length, Diameter, CG, MI of vehicle Control Power Plant :Actuator model (transfer function), Nozzle mass, length, Inertia **Sensor Dynamics** :Attitude & body rate transfer functions **Liquid Slosh** :Pendulum Mass, Length, Distance of pendulum hinge point from CG, Undamped natural frequency, Damping ratio **Structures** :Bending mode Frequency, Generalized mass, Mode shape, Mode slope, **Damping** ratio

Launch Vehicle Modelling

Input Data:

- **Propulsion** :Thrust
- Aerodynamic :Aerodynamic (Lateral/Side) force coefficients,
 Center of Pressure
- Trajectory :Altitude, Mach Number, Inertial velocity
- Atmosphere :Density
- **Dispersion level** :Specified Uncertainty bounds

(example: Aero coefficients ±3%,

Bending mode frequency ±10% etc.)

Launch Vehicle Modeling

Assumptions:

Time Slice Approach:

Time varying mass and inertia properties are frozen over a short period of time (Short Period Dynamics)

Small Angle Approximation:

Deviations from Reference trajectories are small so that trigonometric nonlinearity, and higher order term's contributions are neglected.

Decoupling of Attitude Dynamics:

Due to axis symmetry of launch vehicles, Pitch/Yaw/Roll motions are assumed to be decoupled.

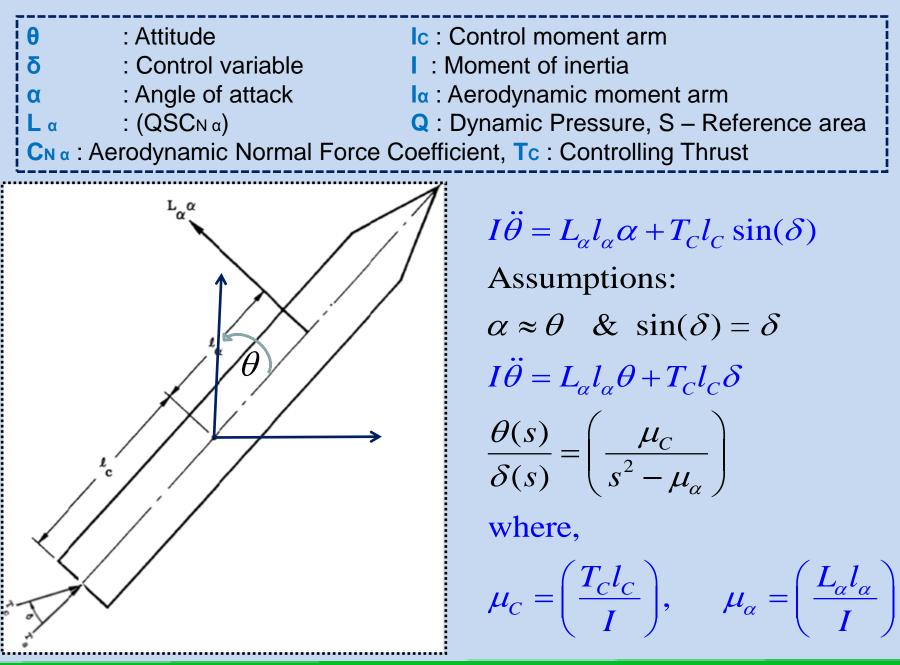
NOTE: There is significant amount of coupling in Yaw/Roll motion for aircraft.

Linear Time Invariant :

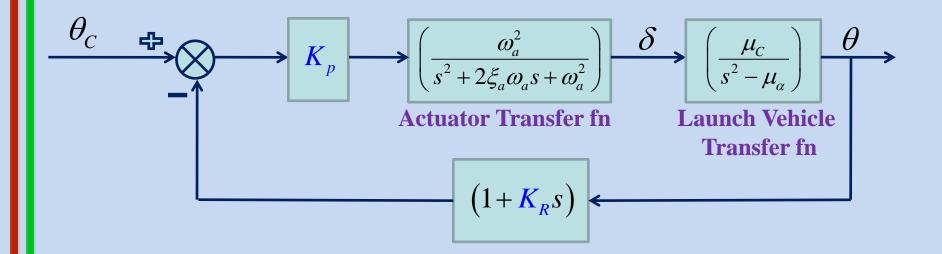
Non-linearity of actuator/sensors (Dead-zone, slew rate etc.) are neglected at design phase.

(All above assumptions lead to LTI systems properties.)

Rigid Body Rotational Dynamics

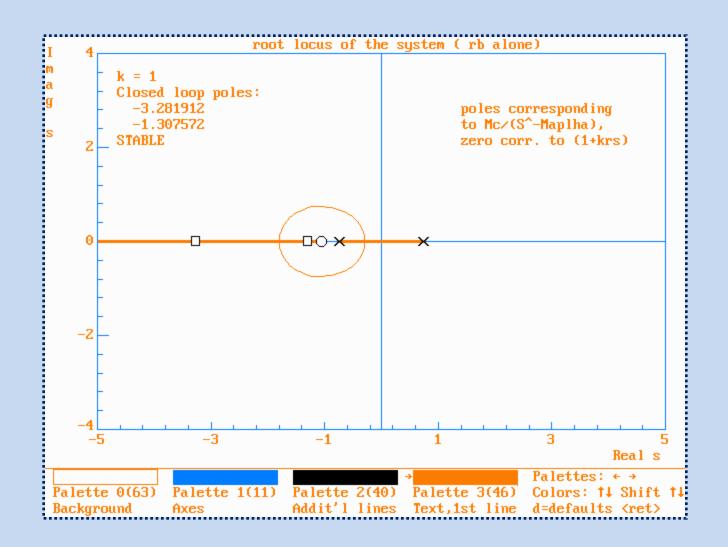


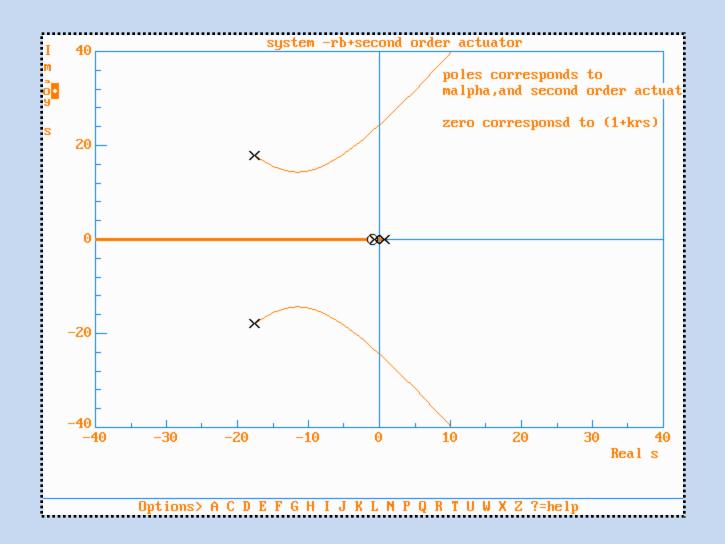
Rigid Body : Close loop system

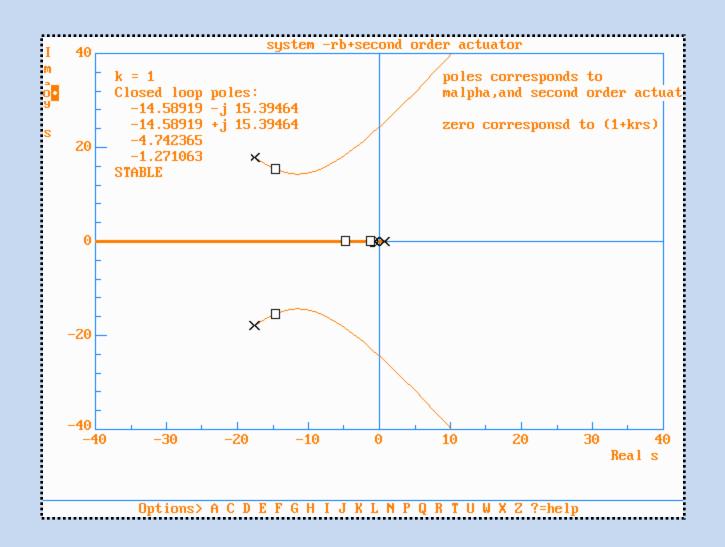


Block Diagram: Close loop system (Rigid Body Only)

Root locus analysis

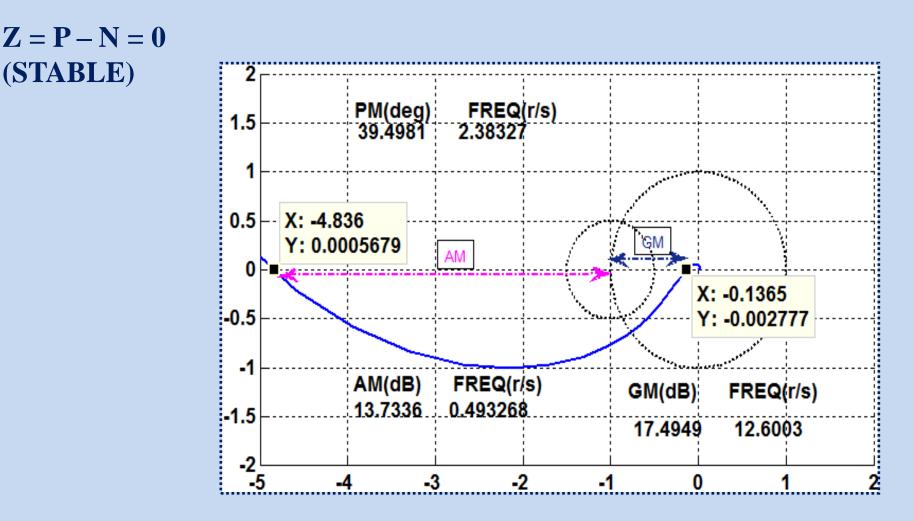






Nyquist Plot @Ign. + T sec

No. of open loop poles in RHP : P = 1 # counter-clockwise encirclement : N =1



Gain Design Method-1:

Characteristic equation:
$$1 + K_P \left(\frac{\omega_a^2}{s^2 + 2\xi_a \omega_a s + \omega_a^2} \right) \left(\frac{\mu_C}{s^2 - \mu_\alpha} \right) (1 + K_R s) = 0$$

Reference equation : $(s^2 + 2\xi_n\omega_n s + \omega_n^2)(s^2 + as + b) = 0$

Known variables : ξ_a , ω_a , μ_C , μ_α , ξ_n , ω_n

Unknown variables : K_p , K_R , a, b

degree of ch. polynomial : 4

Rigid Body gain : K_P & K_R

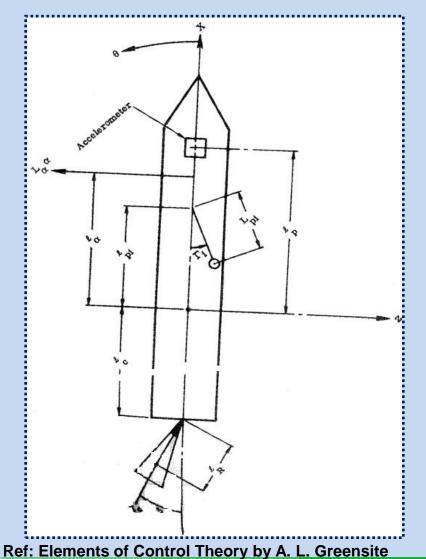
a, b : information of rest poles locations

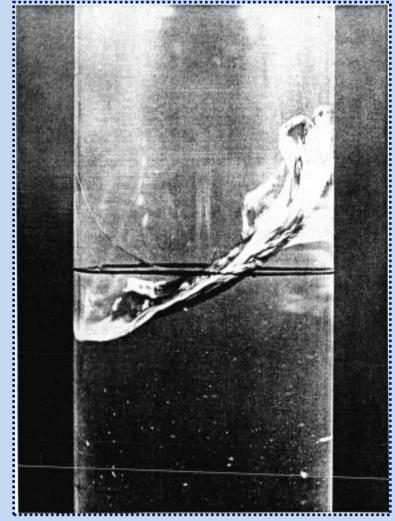
<u>Slosh</u>

- Lateral oscillations of liquids in tank is slosh
- Modelled by replacing liquid mass with rigid mass and a harmonic oscillator such as spring or pendulum
- Pendulum parameters are function of tank shape and liquid level

Modeling Liquid Slosh

The Force & Moments produced by sloshing of the liquid fuel is analyzed by an equivalent Mass and Pendulum Or an equivalent Spring Mass Analogy.





Ref: NASA SP-106

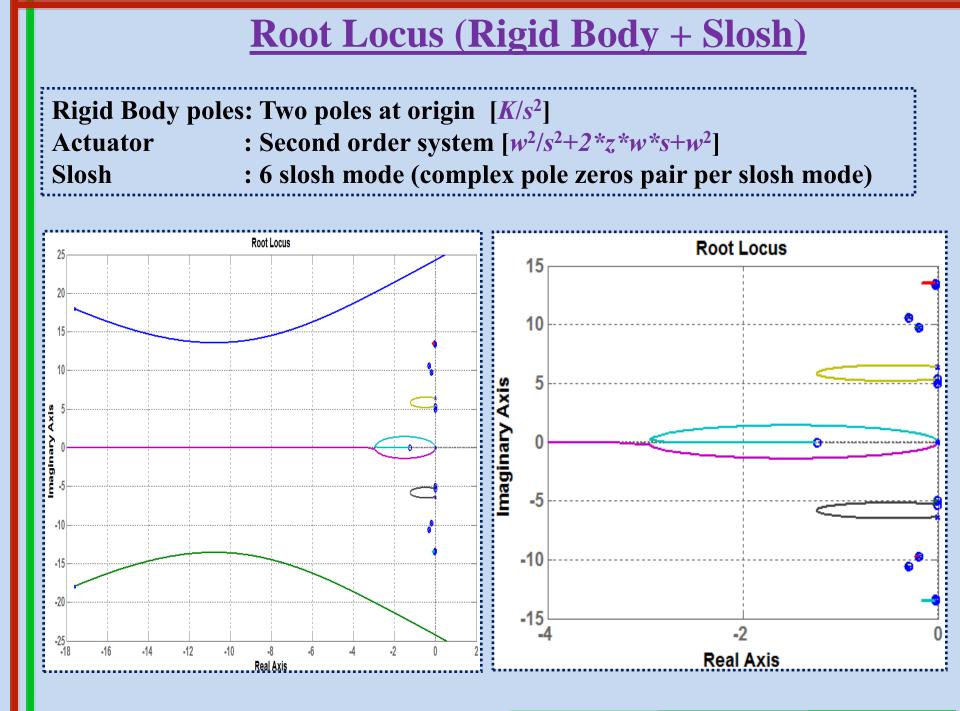
Slosh Dynamics

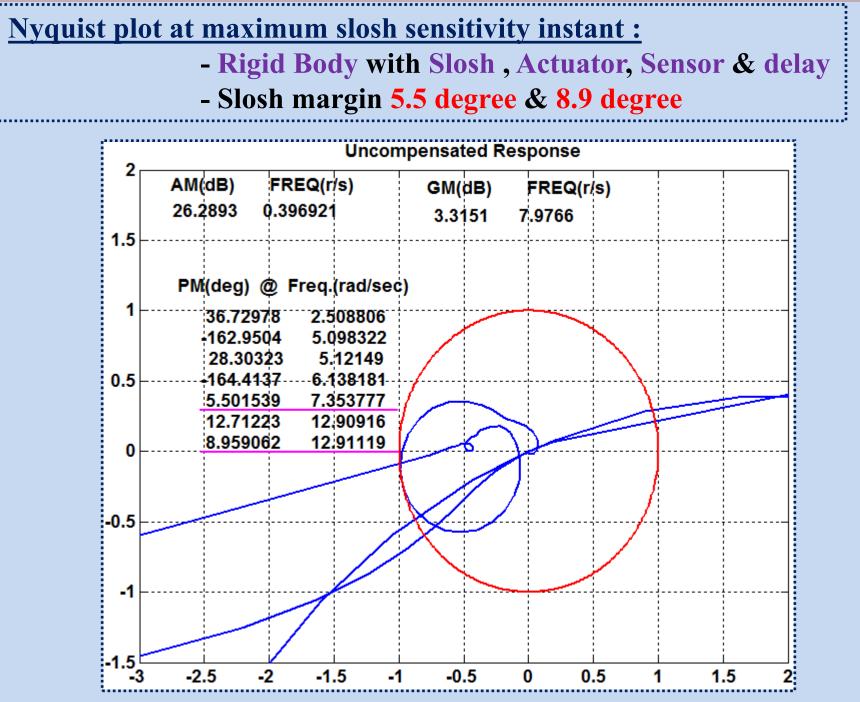
$$L_{pi}(s^2 + 2\zeta_{pi}\omega_{pi}s + \omega_{pi}^2)\Gamma_i = -(\dot{w} - U_0\dot{\theta}) + (\ell_{pi} - L_{pi})\ddot{\theta}$$

where,

- L_{pi} : Length of ith pendulum
- ℓ_{pi} : distance of ith pendulum hinge point from body cg
- ζ_{pi} : damping of ith Pendulum
- ω_{pi} : Undamped natural Frequency of ith Pendulum
- Γ_i : Pendulum angle
- \dot{w} : Lateral acceleration
- U_0 : Forward inertial velocity
- $\dot{\theta}$: attitude rate

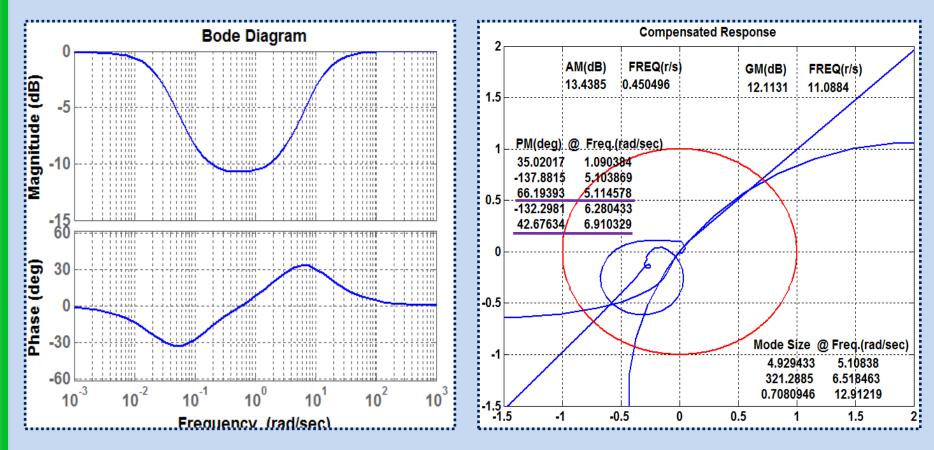
NOTE: Complex Pole-zero pair is introduced in Rigid body dynamics by each Slosh mode.

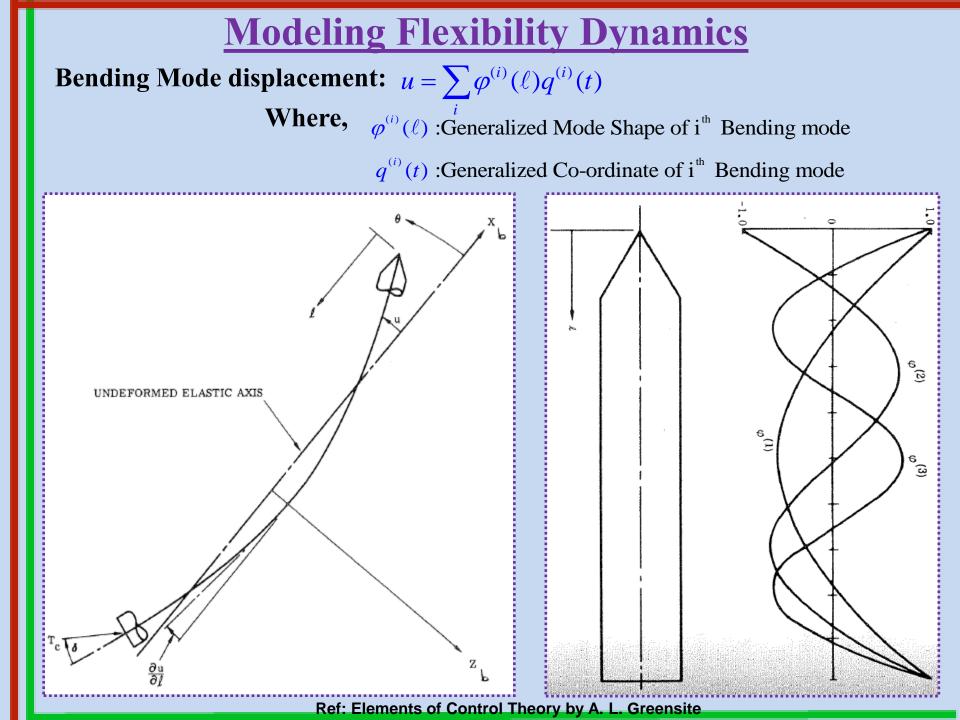




Lag-lead compensator (phase margin improvement)

Lag-Lead Compensator Bode plot





Flexibility Dynamics

1. Generalized mode shape is a function of vehicle length and mass distribution etc. Since mass of vehicle is rapidly decreasing, Mode shape is changing w.r.t. time. (Predicted with uncertainty bounds)

2. Generalized Co-ordinate dynamics is represented by second order differential equation.

$$(s^{2}+2\zeta^{(i)}\omega^{(i)}s+[\omega^{(i)}]^{2})q^{(i)}=-\frac{T_{c}}{M^{(i)}}\delta, \quad i=1, 2, 3...$$

3. Flexibility deflection is picked-up by attitude sensor & Flexible-deflection rate is picked-up by rate sensor.

$$\dot{\theta} = \dot{\theta}_{R} + \sum_{i} \sigma_{RG}^{(i)} \dot{q}(i)$$
$$\theta = \theta_{R} + \sum_{i} \sigma_{PG}^{(i)} q(i)$$
here, $\sigma^{(i)} = -\frac{\partial \varphi^{(i)}}{\partial \ell}$

w

4. Complex Pole-zero pair is introduced in Rigid body dynamics by each Generalized Co-ordinate.

Bending Mode Stabilization

Gain Stabilization:

Attenuate control loop gain at desired frequency, to ensure stability regardless of control loop phase uncertainty. (Second/Higher BM are usually Gain stabilized)

Phase Stabilization:

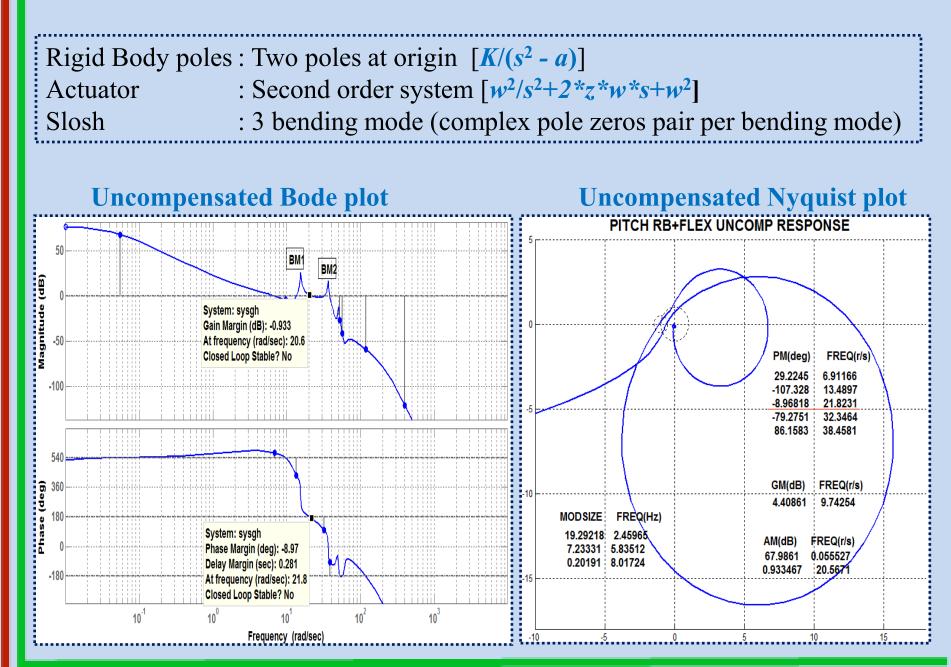
Provide proper phase characteristics at desired frequency to obtain a close loop damping, that is greater than the passive damping.

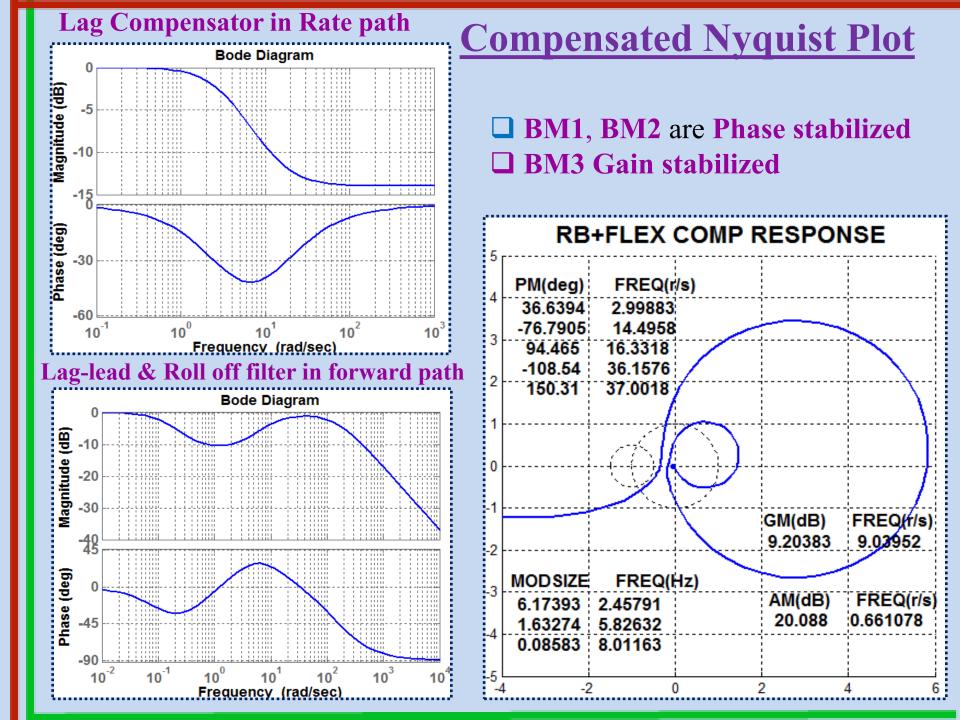
(First/Second BM are usually Gain stabilized)

<u>Gain-Phase Stabilization:</u>

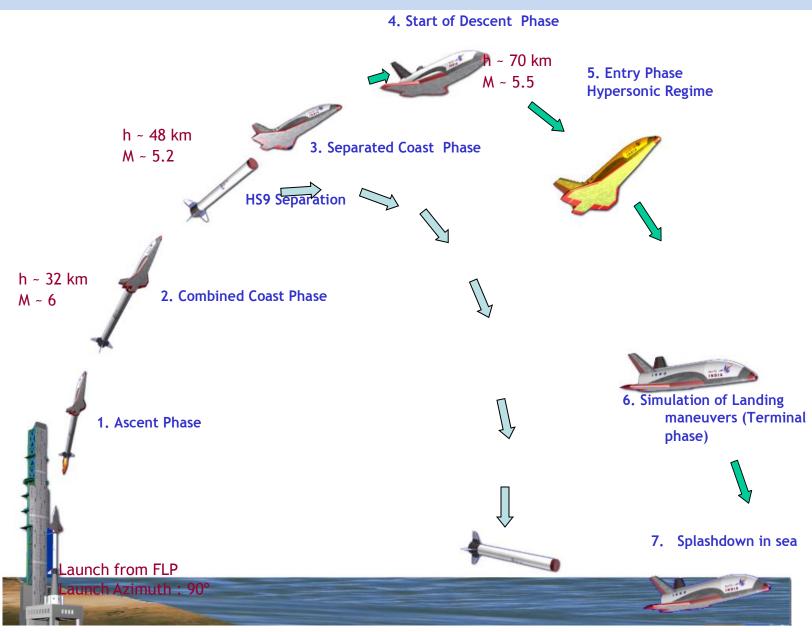
A Rigid body/Flexible mode is said to be gain-phase stabilize if it is close loop stable with finite gain and phase margin.

<u>Rigid Body + Flexibility</u>

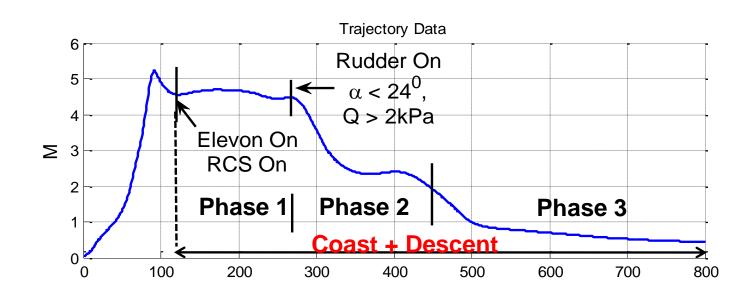


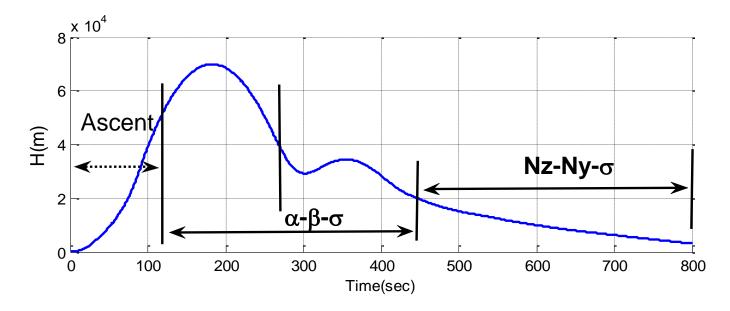


HEX-1 MISSION PROFILE

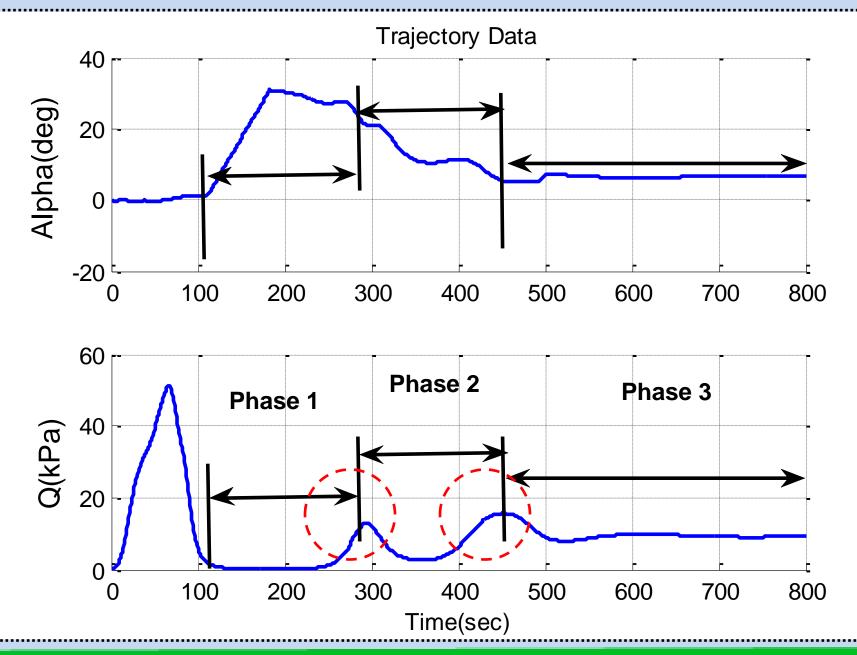


Different Phases of RLV during TDV alone Flight





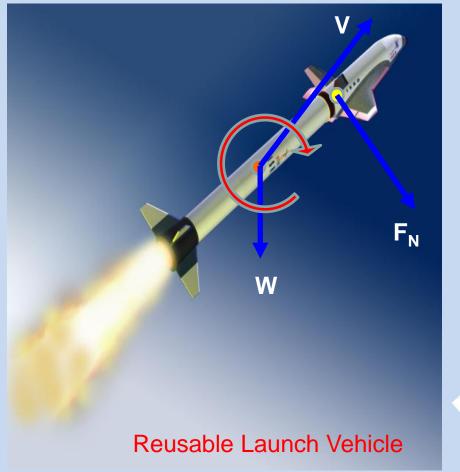
Critical Regions of Flight during TDV alone Phase



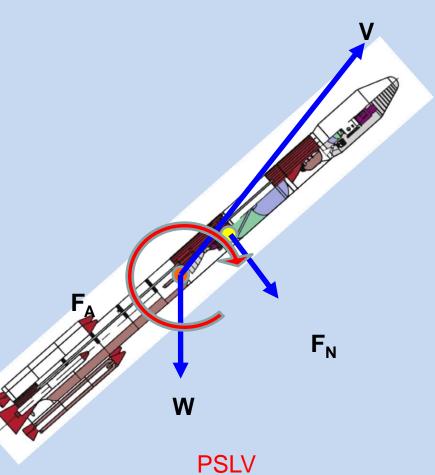
Aerodynamic instability and Control requirement

Higher the aerodynamic instability faster is the divergence: requires quicker Control

$$\mu_{\alpha} = 16, T_d = 0.33 \,\mathrm{s}$$



 $\mu_{\alpha} = 0.75, T_d = 1.52 \text{ s}$

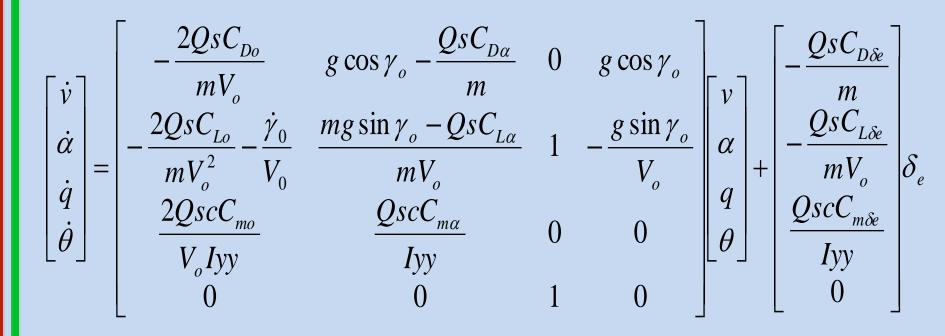


Rigid body and Actuator Bandwidth requirements for various launch vehicles						ements for
		Vehicle	μ_{lpha}	Time to double	Rigid body BW (ω _c)	Actuator BW $(6\omega_c)$
		PSLV	0.75	1.52	2.96 rad/s (0.47 hz)	2.8 hz (6.5 hz)
		GSLV	0.7	1.57	1.92 rad/s (0.31 hz)	1.86 hz (4 hz)
। B B C T T T		MK III	3.6	0.694	3.18 rad/s (0.51 hz)	3.06 (4 hz)
		RLV	30.8	stable	11.1 rad/s (1.76 hz)	10.56 hz (6.5hz)
		TSTO Orbiter	5.2	0.5775	4.56 rad/s (0.7247 hz)	4.34 hz (> 4 hz)
Datase films		Shuttle	3.4	0.7142	3.68 rad/s (0.5869 hz)	3.52 hz (6.5 hz)

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RLV-TD Pitch Dynamics

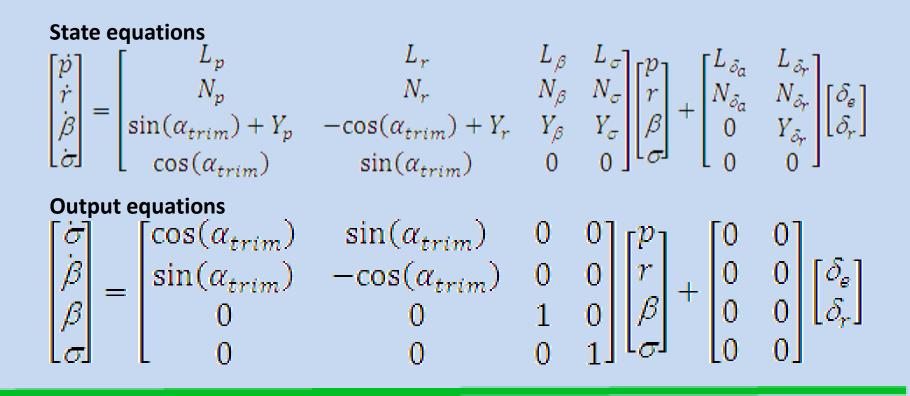


Longitudinal Dynamics characteristic equations

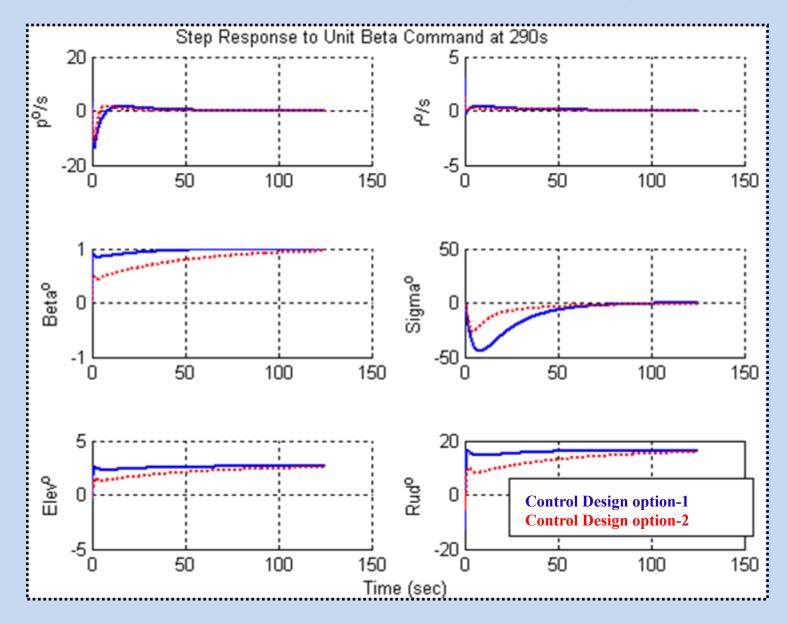
$$\Delta(s) = (s^2 + 2\varsigma_s \omega_s s + \omega_s^2)(s^2 + 2\varsigma_p \omega_p s + \omega_p^2) = 0$$

RLV-TD Yaw-Roll Dynamics

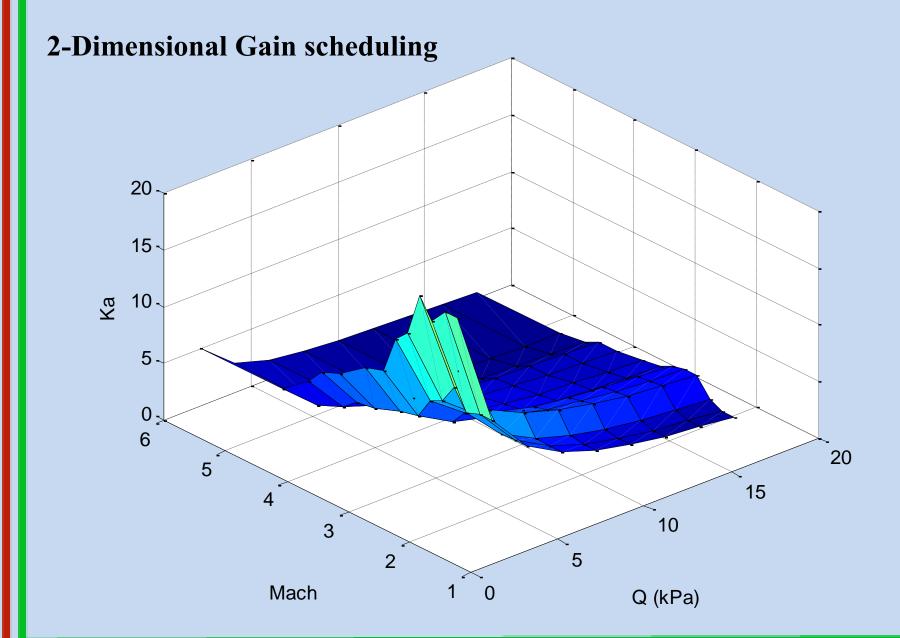
- State space model:
- States: *p* (roll rate), *r* (yaw rate), β (side-slip angle) and σ (bank angle)
- **Outputs:** σ (bank rate), β (side-slip rate), β (side-slip angle) and σ (bank angle)
- Inputs: Differential deflection of elevons (δ_e) and symmetric deflection of rudders (δ_r)



Yaw Roll Dynamics coupling

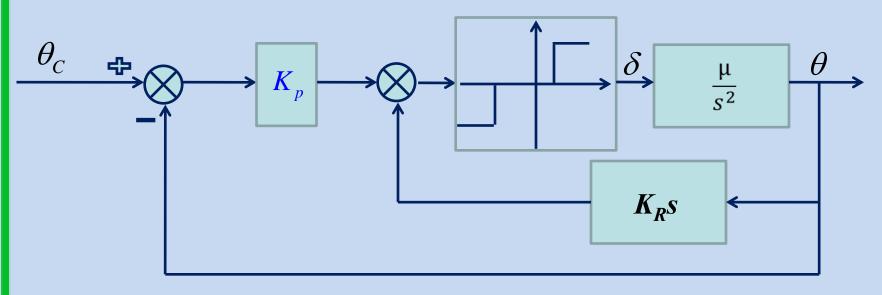


Forward Path Gain



Non-Linear Control

- Integrator limit
- Rate Control Limit
- Dead-zone



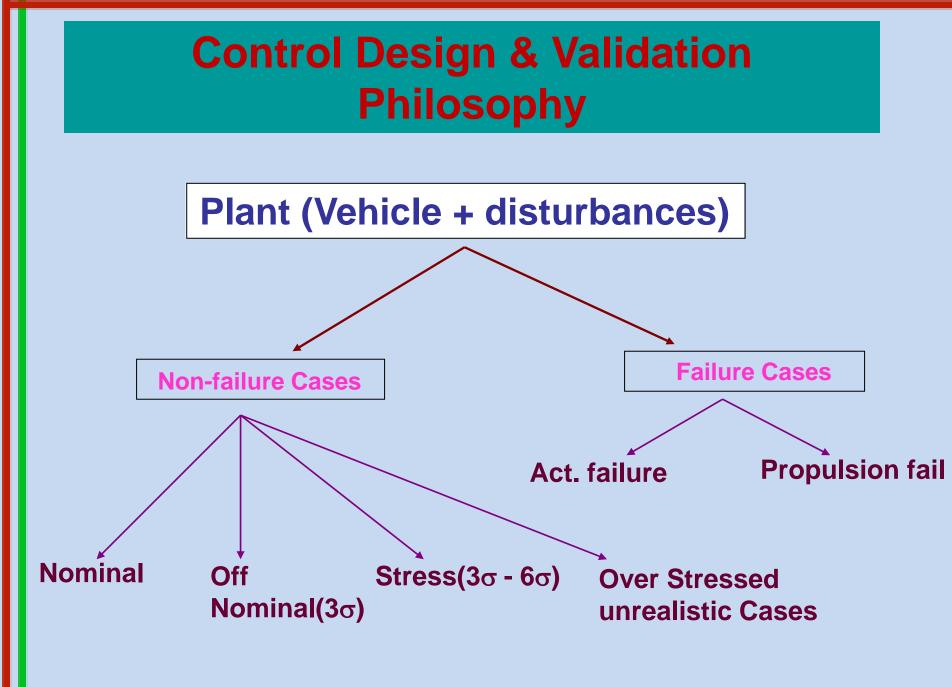
Block Diagram : ON-OFF Control with Dead-zone

Design parameters

- Control Law- Error computation
- Gain Schedule
- Filters
- Integrator
- Nonlinear control Logics

Implementation Aspects

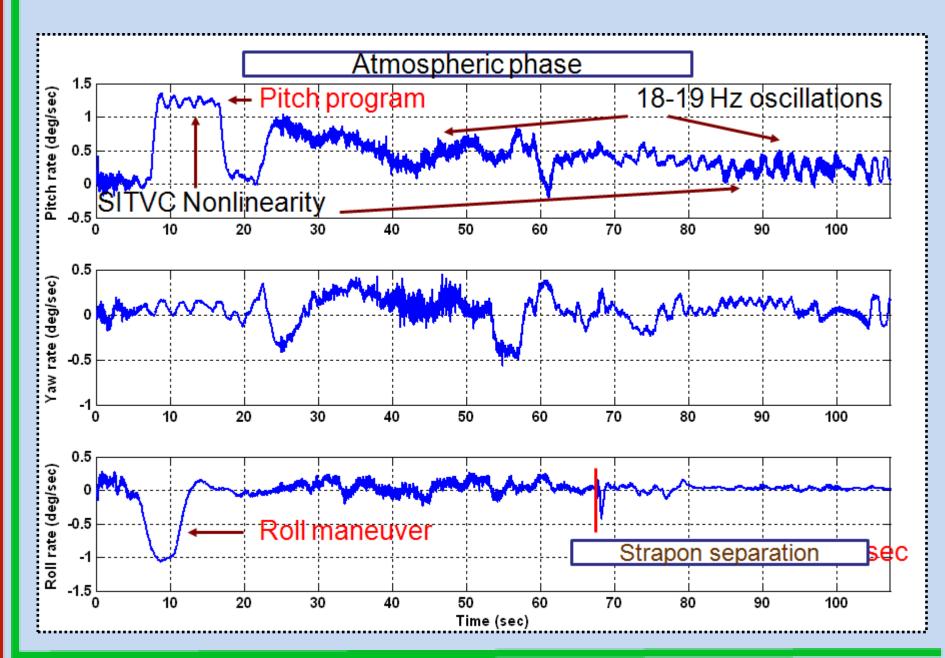
- Finite Word length Machine
- Memory and Execution Time
- Fixed point representation
- Accuracy and Scaling
- Overflow problems
- Transportation and computational delays



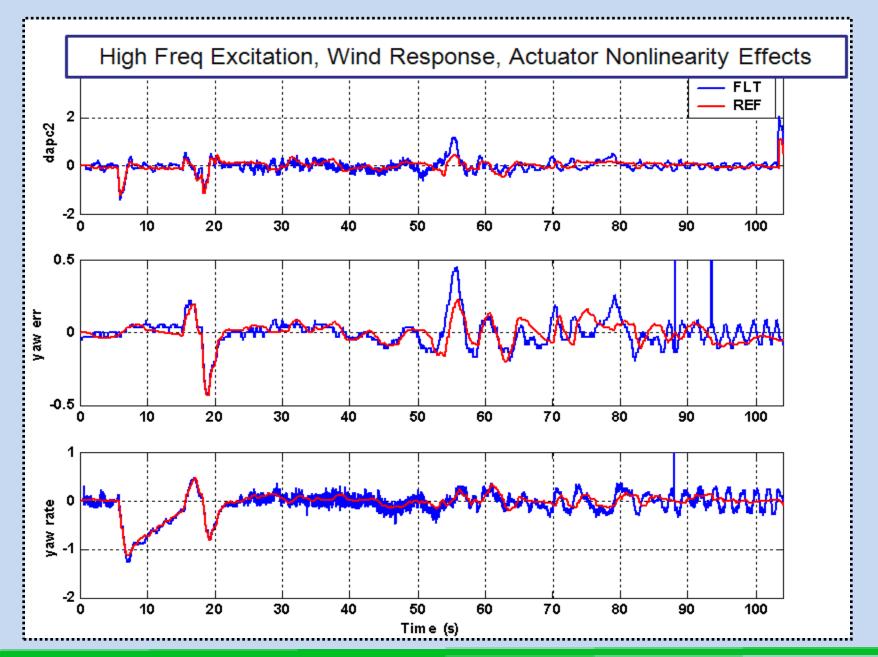
Validation

- Simulated Input Profile (SIP)
- OBC In Loop Simulation (OILS)
- Hardware In Loop Simulation (HLS)
- Actuator In Loop Simulation (ALS)
- Flight Test
- Post flight analysis Disturbance calculationmodel matching
- Model Update / Design Update

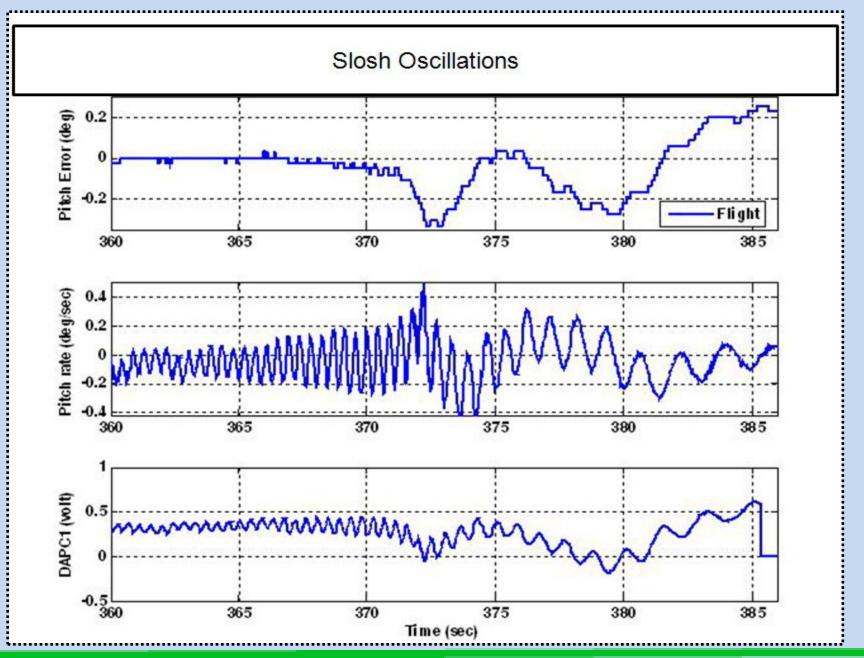
Post Flight Analysis



Post Flight Analysis



Post Flight Analysis



Challenges in Design

- Complexity of the model
- Robust Design Requirement
- Fault tolerance
- SISO to MIMO
- Unified Design Approach
- Design Automation
- Code Automation

Acknowledgement

I would like to acknowledge my colleagues from Control Design division, CGDG, VSSC for their support in preparation of this course material.

Thank You