

## **Modeling &Control of Launch Vehicles**

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**Perspectives In Dynamical Systems & Control**

## **Outline**

#### **ISRO Missions**

#### **ISRO Launch Vehicles**

- Structure Configuration (PSLV / GSLV / RLV)
- Propulsion Configuration
- Aerodynamics
- Actuation Systems
- Navigation systems
- Trajectory Design Guidance & Control

### **Digital Auto-Pilot (DAP)**

- Inputs for design
- Design problem
- Design specification
- Design methodology
- Control Configuration

#### **Launch Vehicle Modelling**

- □ Input Data
- **□** Assumptions
- □ Rigid Body rotational dynamics
- □ Slosh
- $\Box$  Flexibility

## **Outline**

#### **RLV-TD (HEX) Mission**

- **Nission profile**
- **-** Different phase during descent
- **RLV-TD dynamics**
- **Non-linear Control**
- **Design parameters**
- **Implementation aspect**
- **Control design & validation philosophy**
- **Post flight analysis**
- **Challenges in design**

## **ISRO Missions**

- **Sun Synchronous Polar Orbit (SSPO)**
- **Eastward Missions – GTO - Elliptical Orbits(Moon Mission/Mars Mission)**
- **Space Capsule Recovery**
- **RLV – Technology Demonstrator**

### **ISRO Launch Vehicles**

#### **GSLV-M<sub>k</sub> III** Lift-off weight: 629 tonne Payload : 4 tonne **PSLV** into GTO GSLV Mk | & II Height: 42 Metre Lift-off Lift-off weight : 295 tonne weight : 414 tonne Payload: 1600 Kg into Payload : 2 to 2.5 tonne 620 KM Polar Orbit, into GTO τ. 1060 Kg into Height: 49 Metre Geosynchronous GSLV Transfer Orbit (GTO)  $111$ Height: 44 Metre **Barrett**  $SUV-3$ **ASLV** N S D Lift-off Lift-off R ï INDIA weight : 39 tonne weight: 17 tonne A  $\bf{0}$ Payload: 150 Kg (LEO)<br>Height: 23.5 Metre Payload: 40 Kg to Low Earth Orbit (LEO) W 哥 Height: 22 Metre ₹ 뵹  $\overline{a}$  $12$

## **PSLV Configuration**



*<b><i>* Sensors

- **Inertial navigation system**
- **Gyros(Attitude)**
- **Accelerometers**

*<b>* Actuators **SITVC**

 **(Secondary injection Thrust Vector Control)**

- **Engine Gimbal Control**
- **Flex Nozzle control**

## **GSLV-MK2 Configuration**



#### **Definition (4L40+S139)+L37.5+C12.5**



**Sensors : RESINS at EB ,** 

 **RGP at ½ M** 

**Actuators: EGC(L40) EGC(L37.5),** 

 **CSCE, OSS**



## **Propulsion/Configuration**

- **SLV-3:** Core  $(S9) + 2^{nd}$  **stage solid** + 3<sup>rd</sup> **stage solid**
- **ASLV:** Core (S9) **+ 2 Strapons (S9) + Solid Upper Stage**
- **PSLV: Core S139 (Solid) + 6 Strapons + PS2 (L37.5) + PS3 (Solid) + PS4 (L2.5)**
- **GSLV: Core S139 (Solid) + 4 L40 + Cryo (C12)**
- **Mk3: Core S200 (Solid) + 2 L110 + Cryo (C25)**
- **RLV: Core + TDV (No Propulsion)**

## **Aerodynamics**

- **SLV-3: Core with Fins**
- **ASLV: Core with 2 Strapons in 1st stage**
- **PSLV: Core alone & (Core + 6 Strapons)**
- **GSLV: Core + 4 liquid Strapons**

## **Actuation Systems :Thrust Vector Control**

- **SITVC (Secondary Injected Thrust Vector Control)**
- **Engine Gimbal Control**
- $\diamond$  **Flex Nozzle Control**
- **Vernier Engine Control**
- **☆ Reaction Control System (On-Off Control)**
- **Aerodynamic Surfaces**

## **Navigation System**

- **RESINS: Redundant Strap-down Inertial Navigation System**
- **RGP: Rate Gyro Package**
- **LAP: Lateral Accelerometer Package**

## **Trajectory Design – Guidance & Control**

#### **Guidance : Point Mass Trajectory**

– **Maximizing the payload**

**Atmospheric Phase Flight**

- **Dynamic Pressure Curve**
- **Structural Loads**
- **Heating Constraints**
- **Range Safety**

## **Control:**

### **Attitude Dynamics**

### **Launch Vehicle (Pitch/Yaw/Roll)** –

- Rigid Body
- **❖ Slosh**
- **❖** Flexibility
- $\triangle$  Engine dynamics (Actuator + Nozzle)

### **RLV-**

- Longitudinal Dynamics
- Lateral/ Directional

## **Digital Auto-Pilot (DAP)**

- **Launch Vehicle Autopilot is an inner loop of the Navigation, Guidance and Control (NGC) subsystem.**
- **Controls the Attitude of the vehicle in Pitch, Yaw and Roll channels from lift-off till end of flight.**
- **It ensures the stabilisation of the attitude in the presence of disturbing forces and moments caused by various sources. Steers the vehicle along a desired trajectory, maintaining the structural integrity.**



## **Inputs for the Design**

- **Model of the System** to be controlled
	- *Plant* **:** Rigid body, Flexibility, Slosh Dynamics
	- *Actuators* **:** SITVC, EGS, FNC, RCS
	- *Sensors* **:** RGP,RESINS, LAP
- **Disturbances**

Thrust misalignment, CG offset, Differential Thrust, Winds

- **Tracking Commands** Generated by Guidance Law
- **Specifications**

## **Design Problem**

- **Behavior of the output in presence of the disturbance may not be satisfactory**
- **Controller has to ensure satisfactory response of the system rejecting the disturbance**
- **System will be modeled by using differential equations**
- **The controller will process the input signal to achieve satisfactory output.**



## **Design Specifications**

- **Primary Specification-**Tracing Error < 1 Degree
- **Robustness Specifications**
- **Rigid body**

Aero margin > 6 dB Phase margin > 30 Degree Gain margin > 6 dB

**Bending modes**

Phase Margin > 40 Deg. : *Phase Stabilisation*

Attend. margin > 6 dB : *Gain Stabilisation*

**Slosh modes**

Phase margin > 30 Degree

# **Design Methodology**

• **Classical Design Technique**

Tracking Error Specification - Bandwidth / Damping Gain Design- PID

- **Frequency Domain Design** Roll off, Notch, Lag-Lead filter
- **Analysis using –** Root Locus, Bode plot, Nyquist plot

## **Control Configuration**

### • **Control Power Plant**

 Physical Location / Alignment Control Force / Moment Dynamics

## • **Sensors**

Placement

Dynamics

## • **Baffles**

Placement Characteristics Design and development of Autopilot consists following important elements.

i). Mathematical model of vehicle dynamics ii). Design to meet specifications iii). On-board implementation of Autopilot Algorithm iv). Validation



#### **LAUNCH VEHICLE MODELLING**



## **Launch Vehicle Modelling**

### **Input Data:**

 **Plant Model** :Mass, Length, Diameter, CG, MI of vehicle **Control Power Plant** :Actuator model (transfer function), Nozzle mass, length, Inertia **Sensor Dynamics** :Attitude & body rate transfer functions **Liquid Slosh** :Pendulum Mass, Length, Distance of pendulum hinge point from CG, Un damped natural frequency, Damping ratio ■ **Structures** :Bending mode Frequency, Generalized mass, Mode shape, Mode slope, Damping ratio

## **Launch Vehicle Modelling**

### **Input Data:**

- **Propulsion** :Thrust
- **Aerodynamic** :Aerodynamic (Lateral/Side) force coefficients, Center of Pressure
- **Trajectory** :Altitude, Mach Number, Inertial velocity
- **Atmosphere** :Density
- **Q Dispersion level : Specified Uncertainty bounds**

(example: Aero coefficients ±3%,

Bending mode frequency ±10% etc.)

## **Launch Vehicle Modeling**

### **Assumptions:**

#### **Time Slice Approach:**

**Time varying mass and inertia properties are frozen over a short period of time (Short Period Dynamics)** 

#### **Small Angle Approximation:**

**Deviations from Reference trajectories are small so that trigonometric nonlinearity, and higher order term's contributions are neglected.**

#### **Decoupling of Attitude Dynamics:**

**Due to axis symmetry of launch vehicles, Pitch/Yaw/Roll motions are assumed to be decoupled.** 

**NOTE: There is significant amount of coupling in Yaw/Roll motion for aircraft.**

#### **Linear Time Invariant :**

**Non-linearity of actuator/sensors (Dead-zone, slew rate etc.) are neglected at design phase.** 

#### **(All above assumptions lead to LTI systems properties.)**

## **Rigid Body Rotational Dynamics**



### **Rigid Body : Close loop system**



#### **Block Diagram: Close loop system (Rigid Body Only)**

# Root locus analysis







## **Nyquist Plot @Ign. + T sec**

**No. of open loop poles in RHP**  $: P = 1$ **# counter-clockwise encirclement : N =1** 



## **Gain Design Method-1**:

**1.21** Characteristic equation: 
$$
1 + K_P \left( \frac{\omega_a^2}{s^2 + 2\xi_a \omega_a s + \omega_a^2} \right) \left( \frac{\mu_c}{s^2 - \mu_a} \right) (1 + K_R s) = 0
$$
  
Reference equation: 
$$
\left( s^2 + 2\xi_n \omega_n s + \omega_n^2 \right) \left( s^2 + as + b \right) = 0
$$

Reference equation :  $(s^2 + 2\xi_n \omega_n s + \omega_n^2)(s^2 + as + b)$  $\int_{a}^{b} (s^2 + 2\xi_a \omega_a s + \omega_a^2) (s^2 - \mu_a^2)$ <br> $2\xi_n \omega_n s + \omega_n^2 (s^2 + as + b) = 0$  $\left(s^2 + 2\xi_n\omega_n s + \omega_n^2\right)\left(s\right)$ <br> $\xi_a, \omega_a, \mu_c, \mu_a, \xi_n,$  $s^2 + 2\xi_a \omega_a s + \omega_a^2 \left| s^2 \right|$ <br> $s^2 + 2\xi_n \omega_n s + \omega_n^2 (s^2 + as + b^2))$  $\left(s^2 + 2\xi_n\omega_n s + \omega_n^2\right)\left(s^2 + as + b\right) = 0$ <br>  $\xi_a, \omega_a, \mu_c, \mu_\alpha, \xi_n, \omega_n$ 

Known variables :  $\xi_a$ ,  $\omega_a$ ,  $\mu_c$ ,  $\kappa_R$ , a, b  $\mathcal{L}_a$ ,  $\omega_a$ ,  $\mu_c$ ,  $\mu_a$ ,  $\xi_n$ ,  $\omega_n$  $\alpha$ 

 $_p$ ,  $K_R$ Unknown variab les :

degree of ch. polynomial : 4

4<br> $K_{\rm P}$  &  $K_{\rm R}$ Rigid Body gain :

 $a, b:$  information of rest poles locations

## **Slosh**

- **Lateral oscillations of liquids in tank is slosh**
- **Modelled by replacing liquid mass with rigid mass and a harmonic oscillator such as spring or pendulum**
- **<sup>❖</sup>** Pendulum parameters are function of tank shape **and liquid level**

## **Modeling Liquid Slosh**

**The Force & Moments produced by sloshing of the liquid fuel is analyzed by an equivalent Mass and Pendulum Or an equivalent Spring Mass Analogy.**

![](_page_34_Figure_2.jpeg)

![](_page_34_Picture_3.jpeg)

Ref: NASA SP-106

**Slosh Dynamics**  

$$
L_{pi}(s^2 + 2\zeta_{pi}\omega_{pi}s + \omega_{pi}^2)\Gamma_i = -(\dot{w} - U_0\dot{\theta}) + (\ell_{pi} - L_{pi})\ddot{\theta}
$$

where ,

- th  $e^{i\theta}$ :  $e^{i\theta}$ <br>  $e^{i\theta}$ : *Length* of i<sup>th</sup> pendulum *pi* where,<br> $L_{pi}$ : Length
- th : Length of i<sup>th</sup> pendulum<br>: distance of i<sup>th</sup> pendulum hinge point from body cg *pi*
- th : distance of i<sup>th</sup> pendulum<br>: damping of i<sup>th</sup>Pendulum  $\mathcal{L}_{pi}$
- th : damping of i<sup>th</sup>Pendulum<br>: Undamped natural Frequency of i  $\omega_{pi}$ : Undamped natural Frequency of i<sup>th</sup> Pendulum  $\sum_{i}$ : Undamped natu<br>: Pendulum angle
- *i*
- : Lateral acceleration *w*
- U<sub>0</sub>: Forward inertial velocity
- $\dot{\theta}$ : attitude rate

**NOTE: Complex Pole-zero pair is introduced in Rigid body dynamics by each Slosh mode.**

![](_page_36_Figure_0.jpeg)

![](_page_37_Figure_0.jpeg)

### **Lag-lead compensator (phase margin improvement)**

#### **Lag-Lead Compensator Bode plot**

![](_page_38_Figure_2.jpeg)

![](_page_39_Figure_0.jpeg)

## **Flexibility Dynamics**

**1. Generalized mode shape is a function of vehicle length and mass distribution etc. Since mass of vehicle is rapidly decreasing, Mode shape is changing w.r.t. time. (Predicted with uncertainty bounds)**

**2. Generalized Co-ordinate dynamics is represented by second order differential equation.**

equation.  
\n
$$
(s^{2} + 2\zeta^{(i)}\omega^{(i)}s + [\omega^{(i)}]^{2})q^{(i)} = -\frac{T_{c}}{M^{(i)}}\delta, \quad i = 1, 2, 3...
$$

**3. Flexibility deflection is picked-up by attitude sensor & Flexibledeflection rate is picked-up by rate sensor.**

$$
\dot{\theta} = \dot{\theta}_R + \sum_i \sigma_{RG}^{(i)} \dot{q}(i)
$$

$$
\theta = \theta_R + \sum_i \sigma_{PG}^{(i)} q(i)
$$
where,  $\sigma^{(i)} = -\frac{\partial \phi^{(i)}}{\partial \ell}$ 

**4. Complex Pole-zero pair is introduced in Rigid body dynamics by each Generalized Co-ordinate.**

## **Bending Mode Stabilization**

#### **Gain Stabilization:**

**Attenuate control loop gain at desired frequency, to ensure stability regardless of control loop phase uncertainty. (Second/Higher BM are usually Gain stabilized)**

#### **Phase Stabilization:**

**Provide proper phase characteristics at desired frequency to obtain a close loop damping, that is greater than the passive damping. (First/Second BM are usually Gain stabilized)**

#### **Gain-Phase Stabilization:**

**A Rigid body/Flexible mode is said to be gain-phase stabilize if it is close loop stable with finite gain and phase margin.**

## **Rigid Body + Flexibility**

![](_page_42_Figure_1.jpeg)

![](_page_43_Figure_0.jpeg)

## **HEX-1 MISSION PROFILE**

![](_page_44_Figure_1.jpeg)

## **Different Phases of RLV during TDV alone Flight**

![](_page_45_Figure_1.jpeg)

![](_page_45_Figure_2.jpeg)

## **Critical Regions of Flight during TDV alone Phase**

![](_page_46_Figure_1.jpeg)

## **Aerodynamic instability and Control requirement**

**Higher the aerodynamic instability faster is the divergence: requires quicker Control** 

$$
\mu_{\alpha} = 16, T_d = 0.33 \text{ s}
$$

![](_page_47_Figure_3.jpeg)

 $\mu_{\alpha} = 0.75, T_d = 1.52 \text{ s}$ 

![](_page_47_Picture_5.jpeg)

![](_page_48_Picture_153.jpeg)

AND MARKET

win <mark>.</mark><br>Hill 瓣

## **RLV-TD Pitch Dynamics**

![](_page_49_Figure_1.jpeg)

Longitudinal Dynamics characteristic equations

$$
\Delta(s) = (s^2 + 2\varsigma_s \omega_s s + \omega_s^2)(s^2 + 2\varsigma_p \omega_p s + \omega_p^2) = 0
$$

## **RLV-TD Yaw-Roll Dynamics**

- State space model:
- **States:**  $p$  (roll rate),  $r$  (yaw rate),  $\beta$  (side-slip angle) and  $\sigma$  (bank angle)
- **Outputs:**  $\sigma'$ (bank rate),  $\beta'$ (side-slip rate),  $\beta$  (side-slip angle) and  $\sigma$  (bank angle)
- $\cdot$  **Inputs:** Differential deflection of elevons  $(\delta_e)$  and symmetric deflection of rudders  $(\delta_{\rm r})$

![](_page_50_Figure_5.jpeg)

$$
\begin{bmatrix} \dot{p} \\ \dot{r} \\ \dot{\beta} \\ \dot{\beta} \\ \dot{\gamma} \end{bmatrix} = \begin{bmatrix} L_p & L_r & L_{\sigma} & L_{\sigma} \\ N_p & N_r & N_{\sigma} & N_{\sigma} \\ \sin(\alpha_{trim}) + Y_p & -\cos(\alpha_{trim}) + Y_r & Y_{\beta} & Y_{\sigma} \\ \cos(\alpha_{trim}) & \sin(\alpha_{trim}) \end{bmatrix} \begin{bmatrix} p \\ r \\ \beta \\ 0 \\ 0 \end{bmatrix} + \begin{bmatrix} L_{\delta_a} & L_{\delta_b} \\ N_{\delta_a} & N_{\delta_b} \\ 0 \\ 0 \end{bmatrix} \begin{bmatrix} \delta_e \\ \delta_r \\ \delta_r \end{bmatrix}
$$
  
-74.5  
139.8

### **Yaw Roll Dynamics coupling**

![](_page_52_Figure_1.jpeg)

## **Forward Path Gain**

![](_page_53_Figure_1.jpeg)

## **Non-Linear Control**

- Integrator limit
- Rate Control Limit
- Dead-zone

![](_page_54_Figure_4.jpeg)

## **Design parameters**

- Control Law- Error computation
- Gain Schedule
- Filters
- Integrator
- Nonlinear control Logics

## **Implementation Aspects**

- Finite Word length Machine
- Memory and Execution Time
- Fixed point representation
- Accuracy and Scaling
- Overflow problems
- Transportation and computational delays

![](_page_57_Figure_0.jpeg)

## **Validation**

- Simulated Input Profile (SIP)
- OBC In Loop Simulation (OILS)
- Hardware In Loop Simulation (HLS)
- Actuator In Loop Simulation (ALS)
- Flight Test
- Post flight analysis Disturbance calculationmodel matching
- Model Update / Design Update

## **Post Flight Analysis**

![](_page_59_Figure_1.jpeg)

## **Post Flight Analysis**

![](_page_60_Figure_1.jpeg)

## **Post Flight Analysis**

![](_page_61_Figure_1.jpeg)

## **Challenges in Design**

- Complexity of the model
- Robust Design Requirement
- Fault tolerance
- SISO to MIMO
- Unified Design Approach
- Design Automation
- Code Automation

### • **Acknowledgement**

**I would like to acknowledge my colleagues from Control Design division, CGDG, VSSC for their support in preparation of this course material.**

## **Thank You**