

Lecture 22: Extreme Stars: White Dwarfs & Neutron Stars

Readings: 22-2, 22-4, 23-1, 23-3, 23-4, 23-5, 23-8, 23-9

Key Ideas

White Dwarf

- Remnant of a low-mass star
- Supported by Electron Degeneracy Pressure
- Maximum Mass $\sim 1.4 M_{\text{Sun}}$ (Chandrasekhar Mass)

Neutron Star

- Remnant of a massive star
- Supported by Neutron Degeneracy Pressure
- Pulsar=rapidly spinning neutron star
- Maximum Mass $\sim 2-3 M_{\text{Sun}}$

The Stellar Graveyard

Question:

What happens to the cores of dead stars?

Answer:

They continue to collapse until either:

- A new pressure law halts further collapse & they settled into hydrostatic equilibrium

- If too massive, they collapse to zero radius and become a black hole.

Degenerate Gas Law

At high density, a new gas law takes over:

- Pack many electrons into a tiny volume
- These electrons fill all low-energy states
- Only high-energy=high-pressure states left

Result is a degenerate gas

- Pressure is independent of temperature
- Compression does not lead to heating
- Compression does give higher density=greater pressure

Allows cold objects to exist in hydrostatic equilibrium

White Dwarfs

Remnant cores of stars with $M < 8 M_{\text{Sun}}$

Held up by Electron Degeneracy Pressure

$M < 4M_{\text{Sun}}$: C-O white dwarfs

M between 4-8 M_{Sun} : O-Ne-Mg white dwarfs

Properties

Mass $< 1.4 M_{\text{Sun}}$ (reflects large amount of mass loss in planetary nebula phase)

Radius $\sim R_{\text{earth}}$ ($< 0.02 R_{\text{Sun}}$)

Density $\sim 10^{5-8} \text{ g/cc}$

Escape Speed: $0.02 c$ (2% speed of light)

Shine by residual heat: no fusion or contraction

Example: Sirius B

$M = 1.0 M_{\text{Sun}}$

$R = 5800 \text{ km}$

$V_{\text{esc}} = 0.02c$

Chandrasekhar Mass

Mass-Radius Relation for White Dwarfs

Larger Mass = Smaller Radius

Different than Normal Matter, such as Chocolate Cake

Larger Mass = Higher Gravitational Force = Larger Pressure = Higher

Density = Smaller Volume

Chandrasekhar Mass

Maximum Mass for White Dwarf

$M_{\text{Sun}} = 1.4 M_{\text{Sun}}$

Calculated by S. Chandrasekhar in the 1930s

Above this mass, electron degeneracy fails and the star collapses

Evolution of White Dwarfs

White dwarfs shine by leftover heat

No sources of new energy (no fusion)

Cool off and fade away slowly

Ultimate State: A *Black Dwarf*

Old, cold white dwarf

Takes ~ 10 Trillion years to cool off

Age of Universe ~ 13.7 billion years < 10 trillion years, so
Galaxy is not old enough for Black Dwarfs

Not to be confused with “Black Holes”

Black dwarfs are black=do not shine because they are the same temperature
as their surroundings

Black holes do not shine because light cannot escape.

Path of White Dwarfs on H-R Diagram: Cool quickly at first , then gradually
approach the temperature of empty space

The Other Supernova

What happens mass is added to the white dwarf and $M > 1.4M_{\text{Sun}}$

Electron degeneracy falls, star collapses

Ignites C-O fusion at high density

Generates heat, but no pressure because degeneracy pressure is independent
of temperature

Greater heat=greater fusion=greater heat.....

Runaway nuclear explosion:

Fusion of light elements into Iron & Nickel

White Dwarf detonates as a Type Ia Supernova

Leaves behind no remnant (total disruption)

Mass Transfer in a Binary

See Figure 21-18b

A white dwarf can exceed the Chandrasekhar mass by getting mass from a
companion. If the mass transferred (mostly hydrogen & helium) is less than the
Chandrasekhar mass, a runaway nuclear reaction can happen, but it will be much
less energetic and not disrupt the star. This is a *nova*.

Type I and Type II Supernovae

Type I

White dwarf binary
Runaway fusion of light
elements
Peak $L \sim 10^{10} L_{\text{Sun}}$
Standard Candle

Type II

High Mass Star
Core bounce/neutrino
emission
Peak $L \sim 10^8 - 10^9 L_{\text{Sun}}$
Not standard

Neutron Stars

Remnant cores of massive stars:

$$8 < M < 18 M_{\text{Sun}}$$

Leftover core of core-bounce supernova

Held up by Neutron Degeneracy Pressure:

Mass: $\sim 1.2 - 2 M_{\text{Sun}}$, Radius: $\sim 10 \text{ km}$

Density 10^{14} g/cc

Escape Speed $\sim 0.7c$ (70% speed of light)

Shine by residual heat: no fusion or contraction

Radiation

Very hot at beginning, but very small

Low luminosity

Emit in X-rays

~ 6 isolated neutron stars seen. Otherwise we see them with their supernova remnants.

Structure of a Neutron Star

At densities $> 2 \times 10^{14} \text{ g/cc}$

Nuclei melt into a sea of subatomic particles (protons & neutrons)

Protons & electrons combine into neutrons

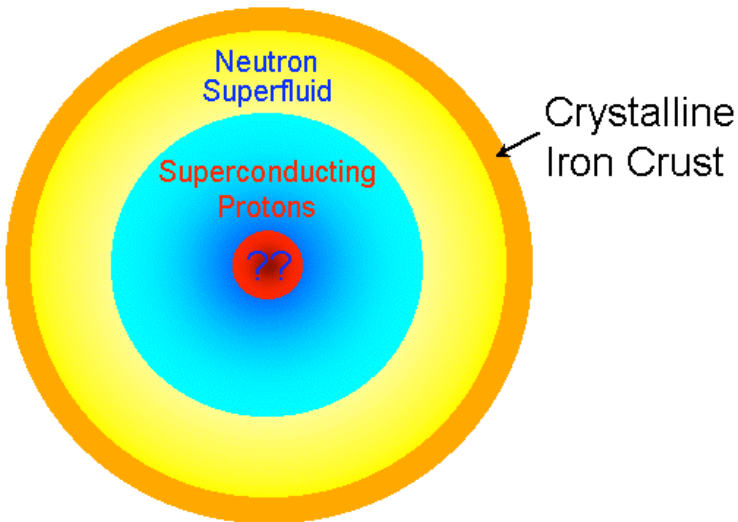
Surface is cooler

Solid crystalline crust

Inside is exotic matter

Superfluid of neutrons, superconducting protons, and weirder stuff.

Subject of much current research



Accidental Discovery of Pulsars

1967:

Jocelyn Bell (Cambridge grad student) & Anthony Hewish (her advisor) discover pulsating radio sources while looking for something else

Pulsars=Pulsating Radio Sources

Emit sharp millisecond-long pulses every second

Cannot be normal stars or white dwarfs. Strong evidence for neutron stars.

Pulsars

Rapidly spinning, magnetized neutron stars

Lighthouse Model:

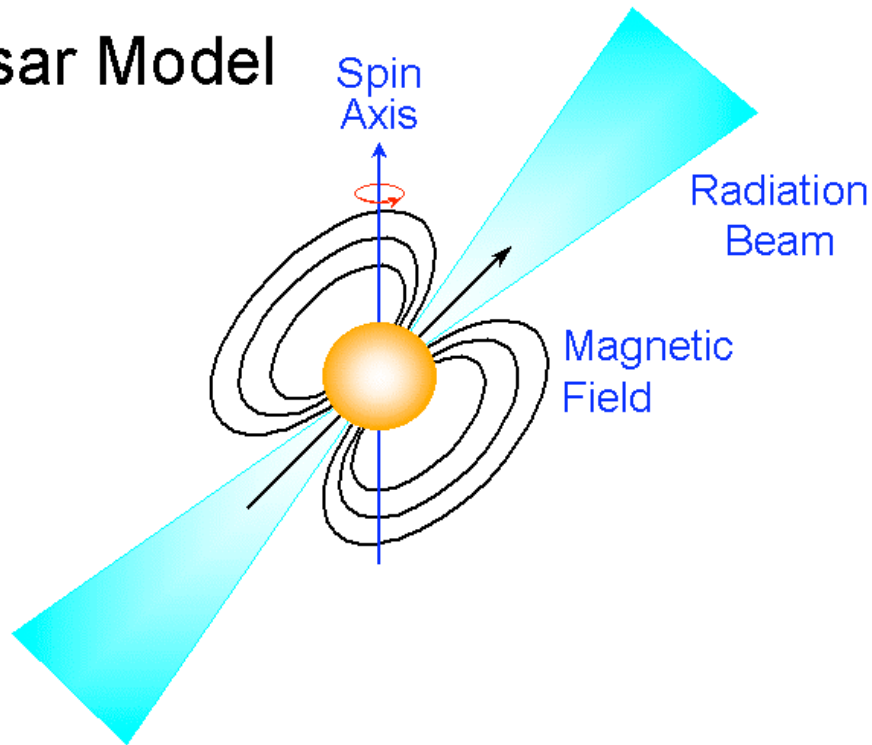
Spinning magnetic field generates a strong electric field.

Electric field rips electrons off the surface

Magnetic field accelerates them along the poles.

Result: twin beams of intense radiation

Pulsar Model



Example: Crab Nebula Pulsar

Pulsar Evolution

Pulsars spin slower as they age

Radiating energy, so that energy must be coming from somewhere (not fusion!)

Lose rotational energy

Young neutron stars

Fast spinning pulsars

Found in supernova remnants (e.g. Crab Pulsar, Vela Pulsar)

Old neutron stars:

Cold and hard to find

Over the top?

What if the remnant core is *very* massive?

$M_{\text{core}} > 2\text{-}3 M_{\text{Sun}}$ (original star had $M > 18 M_{\text{Sun}}$)

First forms neutron star, but material keeps falling on it

Neutron degeneracy pressure fails

Nothing can stop gravitational collapse

Collapse to a singularity: zero radius and infinite density

Becomes a BLACK HOLE, Gravity's final victory.

