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Checking assumptions of Cox model

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Propensity score analysis

Session 8: Survival analysis part 3

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CUNY SPH Biostatistics 2

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Learning objectives

1 Check model assumptions and fit of the Cox model

- residuals analysis
- log-minus-log plot
- 2 Fit and interpret multivariate Cox models
 - perform tests for trend
 - predict survival for specific covariate patterns
 - predict survival for adjusted coefficients
- 3 Explain stratified analysis
- 4 Identify situations of competing risks
- **5** Describe the application of Propensity Score analysis
- Vittinghoff sections 6.2-6.4

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- Competing Risks Data
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- 1 Review
- 2 Assumptions of Cox PH model
- Tests for trend
- 4 Predictions for specific covariate patterns
- 5 Stratification
- 6 Competing risks
- 7 Propensity Score analysis to control for confounding

Outline

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Cox proportional hazards model

- Cox proportional hazard regression assesses the relationship between a right-censored, time-to-event outcome and multiple predictors:
 - categorical variables (e.g., treatment groups)
 - continuous variables

$$og(HR(x_i)) = log \frac{h(t|x_i)}{h_0(t)} = \beta_0 + \beta_1 x_{1i} + \beta_2 x_{2i} + ... + \beta_p x_{pi}$$

- $HR(x_i)$ is the hazard of patient *i* relative to baseline
- h(t|x_i) is the time-dependent hazard function h(t) for patient i
- $h_0(t)$ is the baseline hazard function, and is the negative of the slope of the $S_0(t)$, the baseline survival function.
- Multiplicative model

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Caveats and Assumptions

- Categories with no events
 - can occur when the group is small or its risk is low
 - HRs with respect to such a reference group are infinite
 - hypothesis tests and CIs are difficult / impossible to interpret
- Assumptions of Cox PH model
 - Constant hazard ratio over time (proportional hazards)
 - Linear association between log(HR) and predictors (log-linearity) / multiplicative relationship between hazard and predictors
 - Independence of survival times between individuals in the sample
 - Uninformative censoring: a censored participant is the same as an uncensored participant with the same covariates at still in the risk set after that time

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Residuals analysis

- Residuals are used to investigate the lack of fit of a model to a given subject.
- For Cox regression, there's no easy analog to the usual "observed minus predicted" residual

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```
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```

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```

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```
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```

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```
suppressPackageStartupMessages(library(pensim))
set.seed(1)
mydat <- create.data(
    nvars = c(1, 1),
    nsamples = 500,
    cors = c(0, 0),
    associations = c(0.5, 0.5),
    firstonly = c(TRUE, TRUE),
    censoring = c(0, 8.5)
)$data</pre>
```

Rename variables of simulated data, and make one variable categorical:

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Simulated data to test residuals methods

summary(mydat)

##	Var1	Var2	time	cens
##	low :323	Min. :-2.99695	Min. : 5	Min. :0.000
##	high:177	1st Qu.:-0.79008	1st Qu.: 691	1st Qu.:0.000
##		Median :-0.02126	Median :1970	Median :1.000
##		Mean :-0.04594	Mean :2529	Mean :0.526
##		3rd Qu.: 0.68933	3rd Qu.:3874	3rd Qu.:1.000
##		Max. : 3.05574	Max. :8481	Max. :1.000

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Kaplan-Meier plot of simulated data, stratified by Var1

Strata + Var1=low + Var1=high 1.00 0.75 0.50 0.25 0.00 2000 4000 6000 ò 8000 Time Number at risk Var1=low Var1=high Var1=low 323 172 87 36 7 177 76 32 5 4000 ò 2000 6000 8000 Time

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Martingale residuals

- censoring variable c_i (1 if event, 0 if censored) minus the estimated cumulative hazard function H(t_i, X_i, β_i) (1 survival function)
 - E.g., for a subject censored at 1 year (c_i = 0), whose predicted cumulative hazard at 1 year was 30%, Martingale = 0 - 0.30 = -0.30.
 - E.g. for a subject who had an event at 6 months, and whose predicted cumulative hazard at 6 months was 80%, Margingale = 1 - 0.8 = 0.2.
- Problem: not symmetrically distributed, even when model fits the data well

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Tests for trend Martingale Residuals

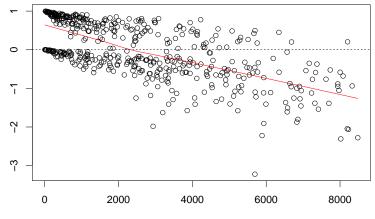
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Martingale residuals in simulated data



Time

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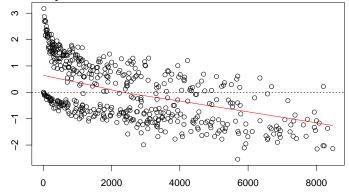
Deviance Residuals

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Deviance residuals in simulated data

- Deviance residuals are scaled Martingale residuals
- Should be more symmetrically distributed about zero?
- Observations with large deviance residuals are poorly predicted by the model



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Schoenfeld residuals

- technical definition: contribution of a covariate at each event time to the partial derivative of the log-likelihood
- intuitive interpretation: the observed minus the expected values of the covariates at each event time.
- a random (unsystematic) pattern across event times gives evidence the covariate effect is not changing with respect to time
- If it is systematic, it suggests that as time passes, the covariate effect is changing.

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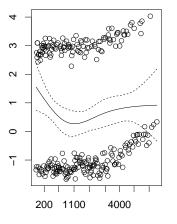
Stratification

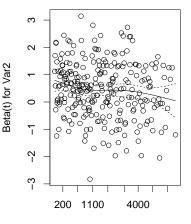
Beta(t) for Var

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Schoenfeld residuals for simulated data









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Schoenfeld test for proportional hazards

- Tests correlation between scaled Schoenfeld residuals and time
- Equivalent to fitting a simple linear regression model with time as the predictor and residuals as the outcome
- Parametric analog of smoothing the residuals against time using LOWESS
- If the hazard ratio is constant, correlation should be zero.
 - Positive values of the correlation suggest that the log-hazard ratio increases with time.

##		chisq	df	р
##	Var1	0.00887	1	0.925
##	Var2	4.92734	1	0.026
##	GLOBAL	5.07415	2	0.079

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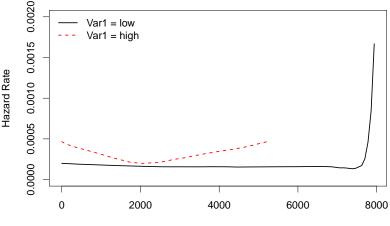
Predictions for specific covariate patterns

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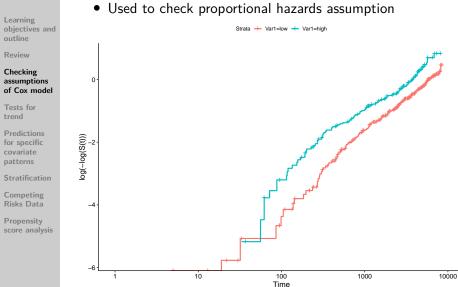
Propensity score analysis

The hazard function h(t), stratified by Var1



Follow-up time

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Log-minus-log plot

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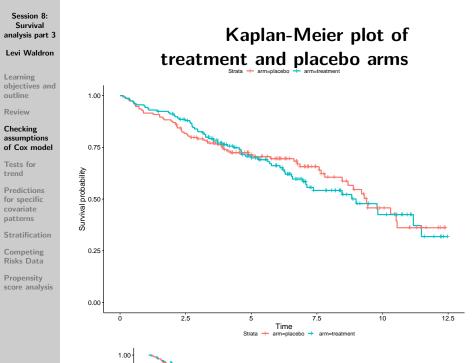
Stratification

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Example: Primary Biliary Cirrhosis (PBC)

- Mayo Clinic trial in primary biliary cirrhosis (PBC) of the liver conducted between 1974 and 1984, n=424 patients.
- randomized placebo controlled trial of the drug D-penicillamine.
 - 312 cases from RCT, plus additional 112 not from RCT.
- Primary outcome is (censored) time to death



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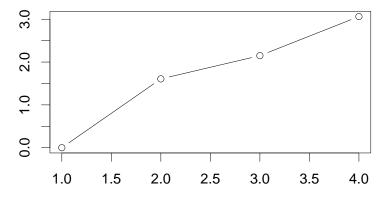
Coefficient, ie In(HR)

Competing Risks Data

Propensity score analysis

What are tests for trend?

- For models including an ordinal variablepush
- Such as PBC stage (1, 2, 3, 4), age category, \ldots
 - Is there a linear / quadratic / cubic relationship between coefficients and their order?
 - Test by LRT or Wald Test



PBC stages 2, 3, 4 (1=ref)

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Fitting a test for trend in R

• Just define stage as an *ordered factor* and tests for trend are done automatically:

```
pbc.os <-
 mutate(pbc.os, stageordered = factor(stage, ordered = TRUE))
fit <- coxph(Surv(time, os) ~ stageordered, data = pbc.os)
summary(fit)
## Call·
## coxph(formula = Surv(time, os) ~ stageordered, data = pbc.os)
##
##
    n= 312, number of events= 125
##
##
                   coef exp(coef) se(coef) z Pr(>|z|)
## stageordered.L 2.1759
                           8.8099 0.6801 3.199 0.00138 **
## stageordered.Q -0.3469 0.7069 0.5248 -0.661 0.50867
## stageordered.C 0.3209 1.3784 0.2990 1.073 0.28316
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
                 exp(coef) exp(-coef) lower .95 upper .95
## stageordered.L 8.8099
                              0.1135
                                       2.3231
                                                 33.410
## stageordered.Q 0.7069 1.4146
                                       0.2527
                                                1.977
## stageordered.C 1.3784 0.7255
                                       0.7671
                                                2.477
##
## Concordance= 0.702 (se = 0.022 )
## Likelihood ratio test= 52.74 on 3 df,
                                         p=2e-11
                      = 43.92 on 3 df.
                                         p=2e-09
## Wald test
## Score (logrank) test = 53.85 on 3 df.
                                         p=1e-11
```

Highly significant tests of overall fit by LRT, Wald, and logrank test.

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How to predict survival from a Cox model?

• The Cox model is a *relative* risk model

- only predicts relative risks between pairs of subjects
- Key is to calculate the overall *S*(*t*), then multiply it by the relative hazard for the specific covariate pattern.
- In this example we plot the baseline survival for all stages together, then for stages 1-4 separately.

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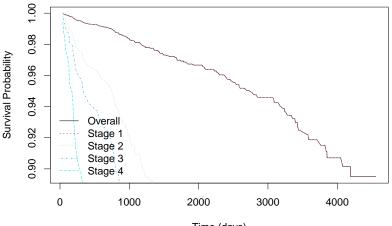
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Predicted survival for specific covariate patterns



Time (days)

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Multivariate regression

- Same coding and objectives as for lm() and glm()
 - controlling for confounding
 - testing for mediation
 - testing for interaction

```
fit <- coxph(Surv(time, os) ~ age + sex + edema
 Session 8:
                              + stage + arm, data = pbc.os)
  Survival
                 summary(fit)
analysis part 3
Levi Waldron
                 ## Call:
                 ## coxph(formula = Surv(time, os) ~ age + sex + edema + stage +
                 ##
                        arm, data = pbc.os)
Learning
                 ##
objectives and
                 ##
                      n= 312, number of events= 125
                 ##
                 ##
                                      coef exp(coef) se(coef)
                                                                    z \Pr(|z|)
                 ## age
                                  0.027618 1.028003 0.009362 2.950 0.00318 **
                 ## sexf
                                 -0.317540 0.727938 0.248839 -1.276 0.20193
Checking
                 ## edema0.5
                                  0.538715 1.713804 0.275287 1.957 0.05036 .
assumptions
                 ## edema1
                                  2.080422 8.007845 0.276959 7.512 5.84e-14 ***
of Cox model
                 ## stage2
                                 1.535263 4.642546 1.034854 1.484 0.13793
                 ## stage3
                                            7.375893 1.016097 1.967
                                 1.998217
                                                                       0.04923 *
Tests for
                 ## stage4
                                  2.666263 14.386101
                                                     1.016234 2.624 0.00870 **
                 ## armtreatment 0.057946 1.059658 0.189200 0.306 0.75940
Predictions
                 ## ---
                 ## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
for specific
covariate
                 ##
patterns
                 ##
                                 exp(coef) exp(-coef) lower .95 upper .95
                                    1.0280
                                              0.97276
                                                         1.0093
                                                                    1.047
                 ## age
Stratification
                 ## sexf
                                    0.7279
                                              1.37374
                                                         0.4470
                                                                    1.186
                 ## edema0.5
                                    1.7138
                                              0.58350
                                                         0.9992
                                                                    2.940
Competing
                 ## edema1
                                    8.0078
                                            0.12488
                                                         4.6534
                                                                 13.780
Risks Data
                                    4.6425
                                              0.21540
                                                         0.6108
                                                                   35.288
                 ## stage2
                 ## stage3
                                    7.3759
                                              0.13558
                                                         1.0067
                                                                   54.040
Propensity
                 ## stage4
                                   14.3861
                                                         1.9630
                                                                  105.430
                                              0.06951
score analysis
                                    1.0597
                                              0.94370
                                                         0.7313
                                                                    1.535
                 ## armtreatment
                 ##
                 ## Concordance= 0.77 (se = 0.022 )
                 ## Likelihood ratio test= 107.6 on 8 df.
                                                             p=<2e-16
                 ## Wald test
                                         = 120.8 on 8 df,
                                                             p=<2e-16
                 ## Score (logrank) test = 177.1 on 8 df,
                                                             p=<2e-16
```

outline

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Predicted survival for adjusted coefficients

- Can create Kaplan-Meier curves for crude or unadjusted coefficients
 - Section 6.3.2.3 in Vittinghoff
- Idea is to estimate hazard ratio in an unadjusted model:
 unadjfit <- coxph(Surv(time, os) ~ stage, data = pbc.os)
 coef(unadjfit)

stage2 stage3 stage4
1.607014 2.149500 3.062775

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##

2.6662626

Predicted survival for adjusted coefficients (cont'd)

```
    and in an adjusted model:

adjfit <- coxph(Surv(time, os) ~ age + sex + edema
                 + stage + arm, data = pbc.os)
coef(adjfit)
                                   edema0.5
                                                   edema1
##
                         sexf
            age
                                                                 stag
      0.0276179
                   -0.3175396
                                  0.5387152
                                                2.0804217
                                                              1.53526
##
##
         stage4 armtreatment
```

0.0579460

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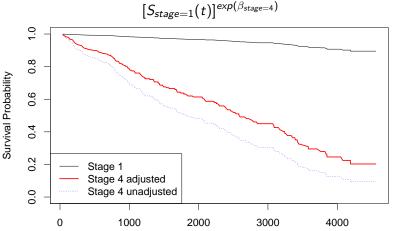
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Predicted survival for adjusted coefficients (cont'd)

• The survival function will be calculated for a "baseline" group, say stage 1, then exponentiated with the adjusted coefficient, e.g.:



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What is stratification?

- relevant to all kinds of regression, not just survival analysis
- when analysis is separated into groups or strata
 - must have an adequate number of events in each stratum (at least 5 to 7)
 - can be used to adjust for variables with strong impact on survival
 - can help solve proportional hazards violations
- Strata have different baseline hazards
- Coefficients / Hazard Ratios are calculated within stratum then combined.
- Vittinghoff 6.3.2

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How to stratify Example - in R, strata() can be added to any model

summary(mycox)

```
## Call:
```

```
## coxph(formula = Surv(time, os) ~ trt + strata(stage), data = p
##
## n= 312, number of events= 125
##
## coef exp(coef) se(coef) z Pr(>|z|)
```

```
## coef exp(coef) se(coef) z Pr(>|z|)
## trt -0.1063 0.8992 0.1814 -0.586 0.558
##
## exp(coef) exp(-coef) lower .95 upper .95
```

trt 0.8992 1.112 0.6302 1.283
##

```
## Concordance= 0.494 (se = 0.025 )
## Likelihood ratio test= 0.34 on 1 df, p=0.6
## Wald test = 0.34 on 1 df, p=0.6
## Score (logrank) test = 0.34 on 1 df, p=0.6
```

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What are competing risks?

- Example from Vittinghoff 6.5: The MrOS study (Orwoll et al. 2005) followed men over 65 to examine predictors of bone fracture and low BMD (subclinical bone loss)
- At end of study participants had:
 - developed fracture (outcome of interest),
 - remained alive without fracture (incomplete follow-up), or
 - died prior to fracture (incomplete follow-up)

Orwoll, E. *et al.* (2005). Design and baseline characteristics of the osteoporotic fractures in men (MrOS) study–a large observational study of the determinants of fracture in older men. Contemporary Clinical Trials, 26(5), 569–585.

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Why not treat died prior to fracture and alive without fracture as censored?

- Recall the independent censoring assumption (Vittinghoff 6.6.4):
 - censored people are similar to those who remain at risk in terms of developing the event of interest;
 - censoring is independent of the event of interest.
 - For patients who died this assumption is highly suspect

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Reasons for right censored data

- Cut-off date of analysis (administrative censoring):
 - Censoring usually independent
- Loss to follow-up
 - Independence may be problematic if sicker individuals discontinue participant in study (lack of energy, too ill, return to home country)
 - or if healthier individuals discontinue participation (don't feel the need to continue, start new life in other country)
- Competing risks:
 - Often informative.
 - In competing risks analysis, independence between competing risks is not required

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Very brief summary of competing risk methods

- 1-to-1 mapping between hazard and cumulative incidence function is lost in competing risks
- Standard Kaplan-Meier estimator is biased for competing risks data
 - Aalen-Johansen estimator is better choice
- Gary's test is analogous to log-rank test
- cause-specific standard Cox PH model might be useful for prognostic (causal) testing, but not estimating a population Hazard Ratio

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Resources for competing risk methods

- Z. Zhang, Survival analysis in the presence of competing risks, Ann Transl Med. 2017 Feb; 5(3): 47. PMID: 28251126
- cmprsk package
- riskRegression package

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What is propensity score analysis?

• an alternative to multivariate regression to control for hypothesized confounders in observational studies:

outcome ~ exposure + counfounder1 + confounder2

- a stratification approach that is more practical than stratifying on multiple hypothesized confounders
- an approach to summarizing many covariates into a single score
- a convenient approach to controlling for many hypothesized confounders

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Propensity score analysis

Propensity score approach to correction for confounders

• *Step 1*: fit the propensity score model (no outcome) that predicts propensity for exposure based on confounders:

exposure ~ counfounder1 + confounder2

- *Step 2*: use propensity predictions to match or stratify participants with similar propensity (for example, stratifying on quintiles of propensity)
- *Step 3*: check adequacy of matching or stratification, ie by comparing attributes of matched participants
- Step 4: test hypothesis among matched participants:

outcome ~ exposure

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Propensity score references

- P.C. Austin (2011), An Introduction to Propensity Score Methods for Reducing the Effects of Confounding in Observational Studies. Multivariate Behavioral Research, 46:3, 399-424, DOI: 10.1080/00273171.2011.568786
- R. d'Agostino (1998), Tutorial in Biostatistics: propensity score methods for bias reduction in the comparison of a treatment to a non-randomized control group. Stat. Med. 17, 2265-2281. http:

//www.stat.ubc.ca/~john/papers/DAgostinoSIM1998.pdf

• You don't need any special package to do basic propensity score matching (e.g. stratifying by quintiles), but the Matchlt package provides multiple matching approaches, diagnostics, good documentation