

Collision Detection

contact generation and GPU acceleration

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<http://bulletphysics.org>

In a nutshell

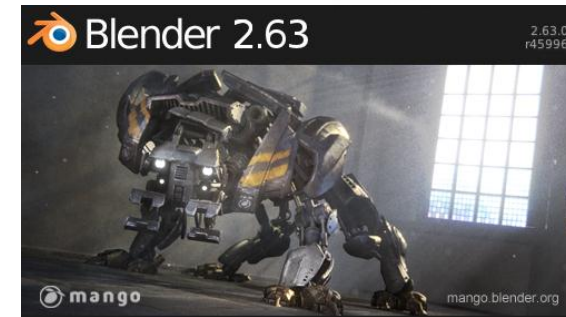
- Intro to the Bullet physics engine
- Broadphase acceleration
 - Parallel sweep and prune broadphase
 - Dynamic AABB tree general purpose acceleration structure
- Midphase acceleration
- Narrowphase collision detection
 - Separating Axis Test
 - Contact Generation
 - GJK closest points, EPA , CCD Conservative Advancement

Bullet physics engine

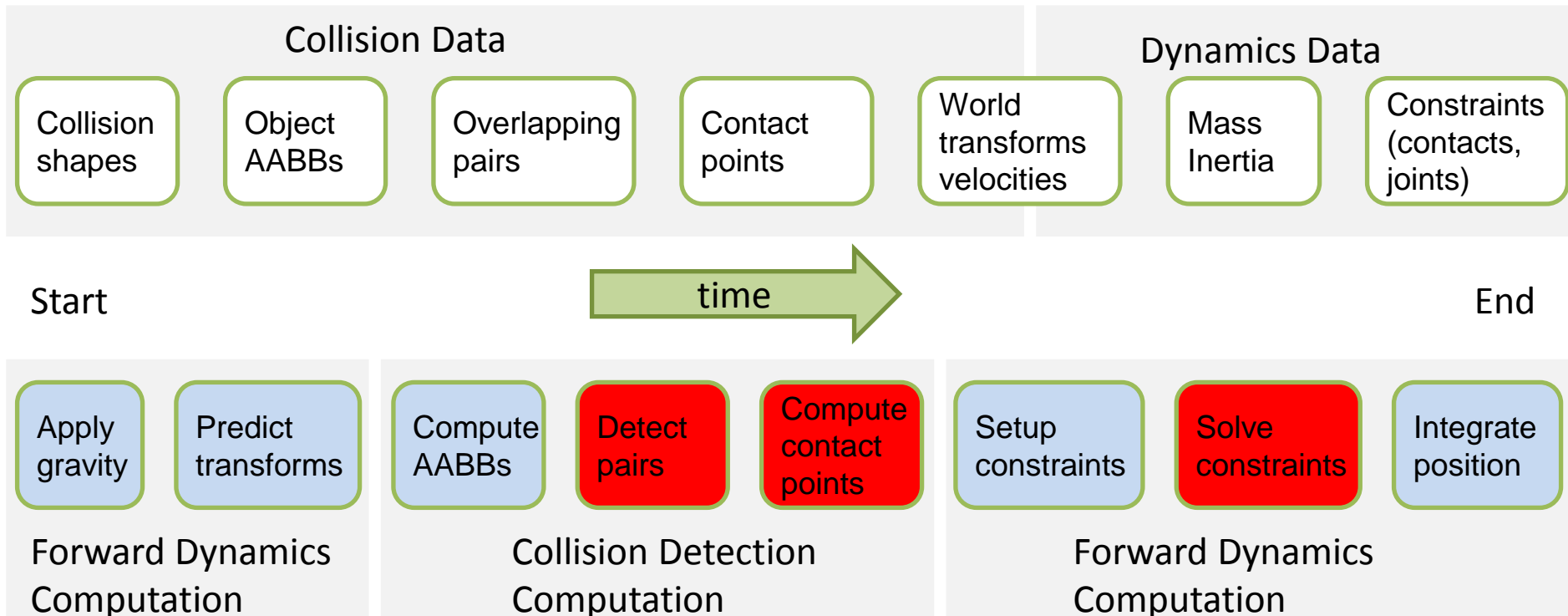
- Simulate Rigid Body, Cloth, Deformables
- Discrete and Continuous Collision Detection
- Open source using the Zlib license
- Free for commercial use
- Written in C++
- OpenCL and Direct Compute for GPU

Bullet Authoring tools

- Maya 2013
- Dynamica (open source)
- Cinema 4D
- Lightwave
- Blender
- Houdini Plugin



Physics Simulation Pipeline



Collision Detection Pipeline

Collision Data

Collision shapes

Object AABBs

Overlapping concave pairs

Local AABB Tree

Overlapping convex pairs

Contact points

World transforms & velocities

Start

time

End

Compute AABBs

Detect (swept) pairs

Broadphase (world space)
Collision Detection

Detect overlapping triangles (trimesh)

Detect overlapping child shapes (compound)

Midphase (object space)
Collision Detection

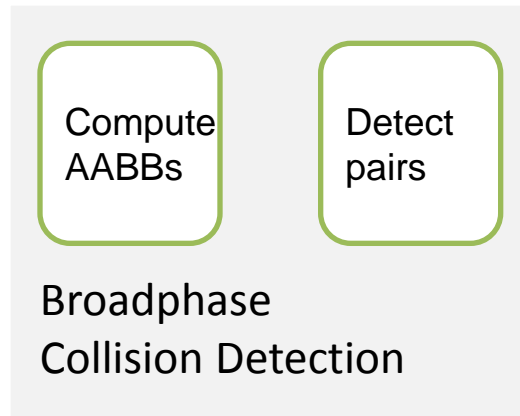
Compute closest points & TOI

Generate full contact manifold

Narrowphase
Collision Detection

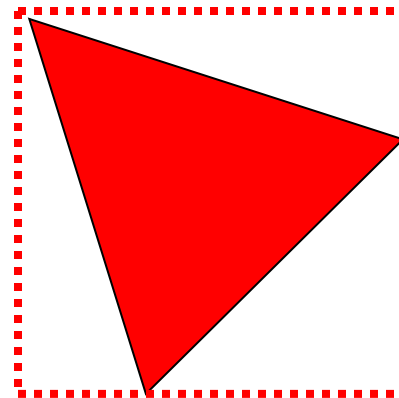
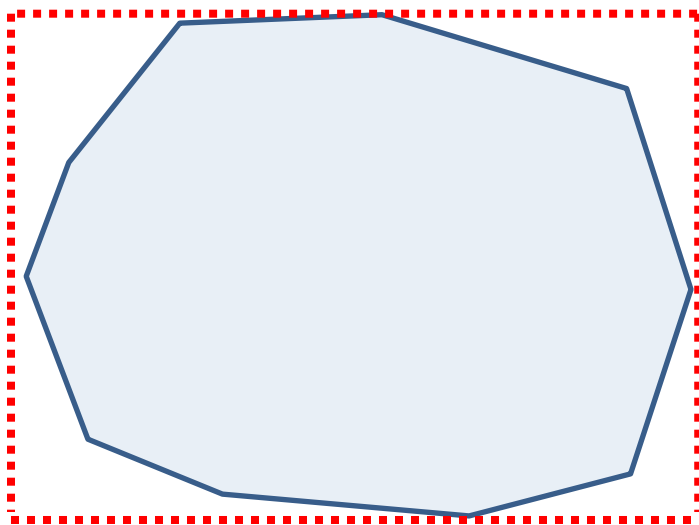
culling using acceleration structures

Broadphase N-body problem



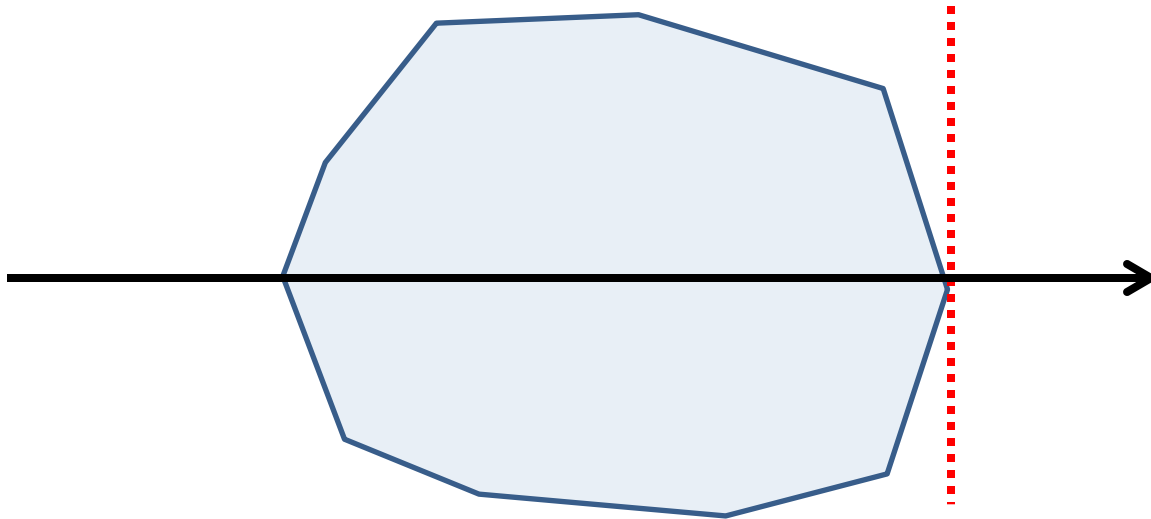
- Input: world space BVs and unique IDs
- Output: array of potential overlapping pairs
 - also ray intersection , swept volumes and CCD

Axis Aligned Bounding Boxes



Support Mapping

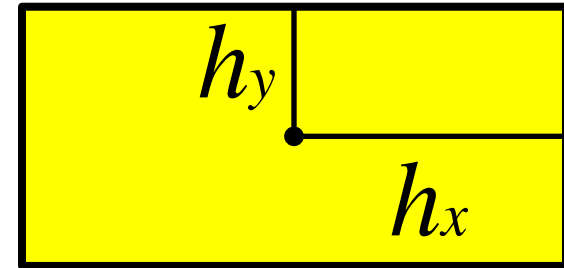
$$S_c(v) = \max\{v \cdot x : x \in C\}$$



Support mapping for primitives

- Box with half extents h

$$S_{box}(v) = (\text{sign}(v_x)h_x, \text{sign}(v_y)h_y, \text{sign}(v_z)h_z)$$

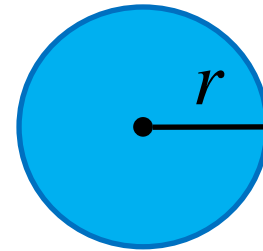


- Sphere with radius r

$$S_{sphere}(v) = \frac{r}{|v|} v$$

- Affine transform

$$S_{Bx+c}(v) = B(S(B^t v) + c)$$

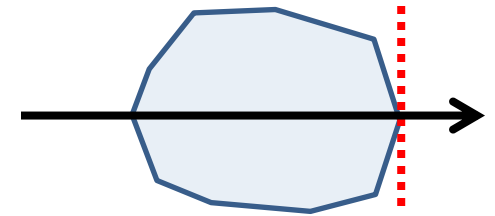


See the book "Collision Detection in Interactive 3D Environments", 2004, Gino Van Den Bergen

Support mapping: convex polyhedra

- Brute force search
 - $O(n)$, cache friendly, SIMD
 - Best for < 200 vertices

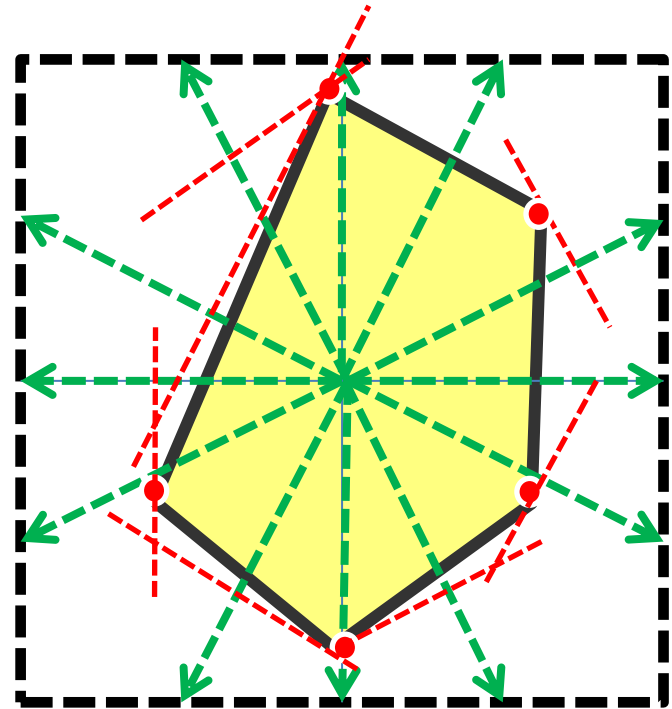
$$S_c(v) = \max\{v \cdot x : x \in C\}$$



- Dobkin-Kirkpatrick Hierarchy
 - $O(\log n)$, see 7.10 in "Computational Geometry in C" by Joseph O'Rourke

Support mapping approximation

- Cube map
 - $O(1)$, approximate

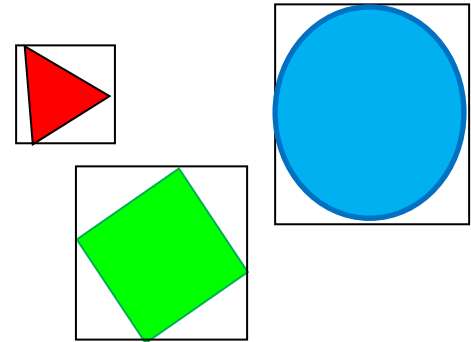


- Software or GPU cube mapping hardware

Brute force overlap test

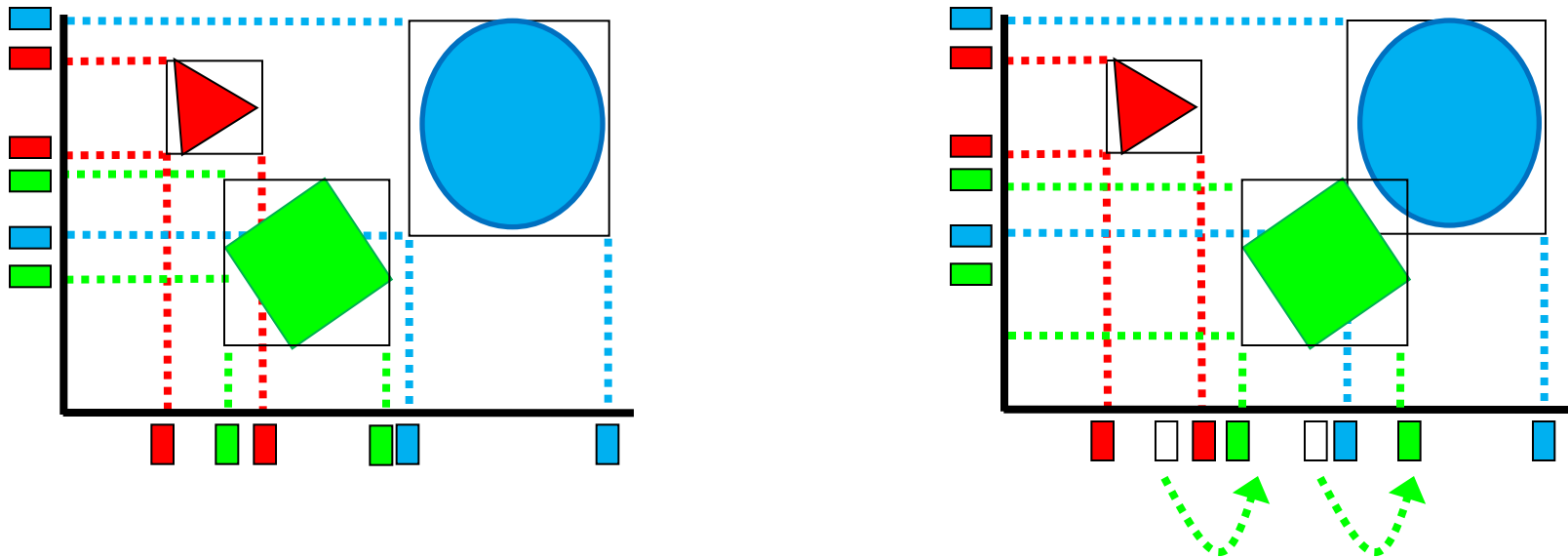
```
bool TestAabbAgainstAabb (__global const btAabbCL* aabb1, __global const btAabbCL* aabb2) {
    bool overlap = true;
    overlap = (aabb1->m_min.x > aabb2->m_max.x || aabb1->m_max.x < aabb2->m_min.x) ? false : overlap;
    overlap = (aabb1->m_min.z > aabb2->m_max.z || aabb1->m_max.z < aabb2->m_min.z) ? false : overlap;
    overlap = (aabb1->m_min.y > aabb2->m_max.y || aabb1->m_max.y < aabb2->m_min.y) ? false : overlap;
    return overlap;
}

__kernel void computePairsBruteForceKernel(__global const btAabbCL* aabbs, volatile __global int2* pairsOut,
                                           volatile __global int* pairCount, int numObjects, int axis, int maxPairs)
{
    int i = get_global_id(0);
    if (i>=numObjects)
        return;
    for (int j=i+1;j<numObjects;j++)
    {
        if (TestAabbAgainstAabb (&aabbs[i],&aabbs[j]))
        {
            int2 myPair;
            myPair.x = aabbs[i].m_minIndices[3];
            myPair.y = aabbs[j].m_minIndices[3];
            int curPair = atomic_inc (pairCount);
            if (curPair<maxPairs)
            {
                pairsOut[curPair] = myPair; //flush to main memory
            }
        }
    }
}
```



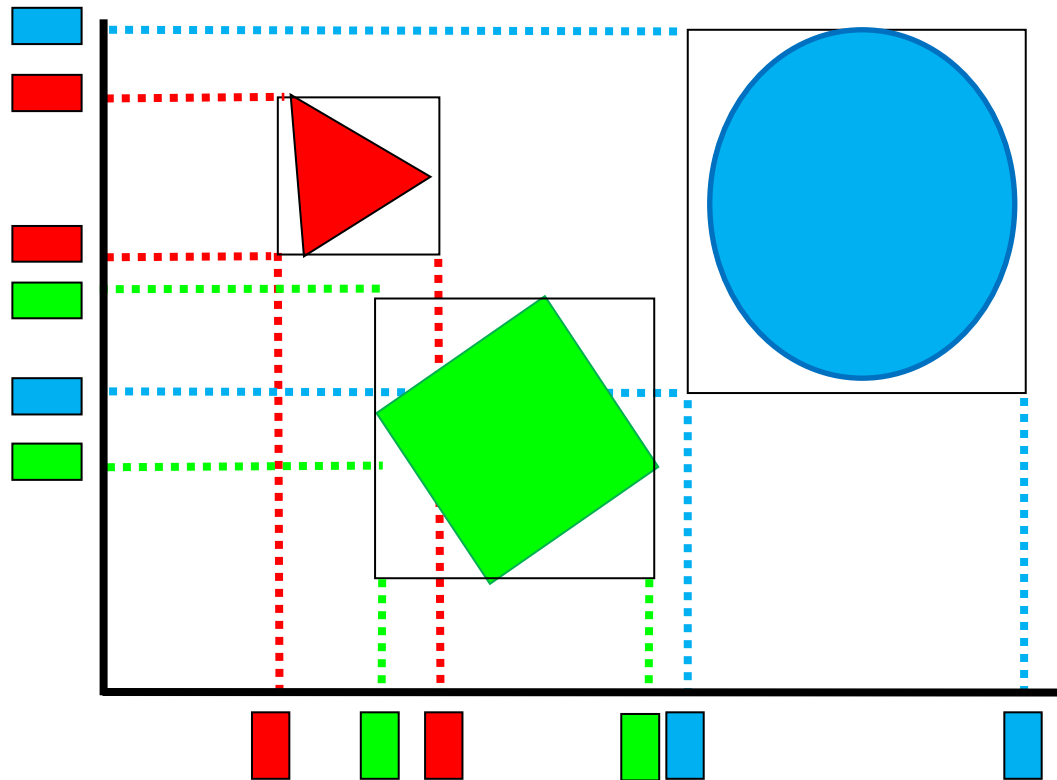
Incremental sweep and prune

- Update 3 sorted axis and overlapping pairs



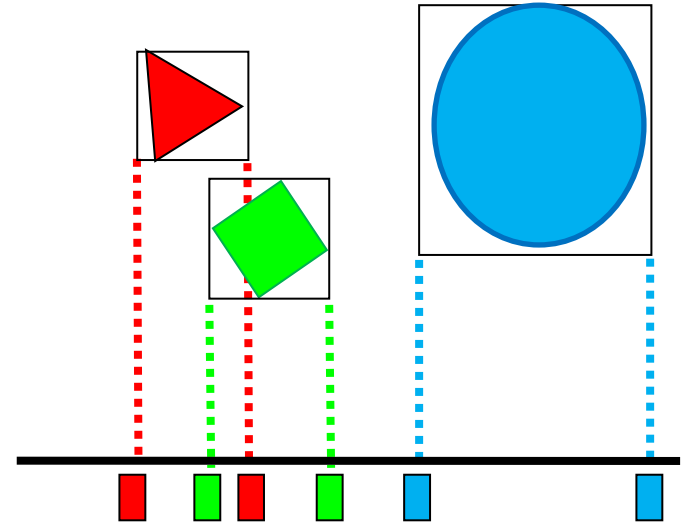
- Performs best if most objects hardly move
- Difficult to parallelize

3-axis SAP ray query/swept AABB



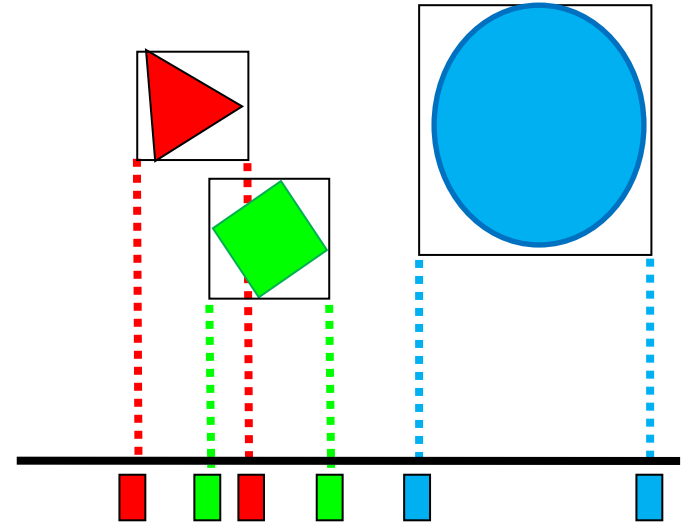
1-axis Sweep and Prune (SAP)

- Find best projection axis
- Sort aabbs along this axis
- For each object, find and add overlapping pairs



GPU parallel SAP

- Find best projection axis
 - Parallel prefix sum
 - Principal Component Analysis
- Sort aabbs along this axis
 - Parallel radix sort
- For each object, find and add overlapping pairs
 - One work item (thread) per object



Parallel SAP implementation

```
__kernel void computePairsSAPKernel( __global const btAabbCL* aabbs, volatile __global int2* pairsOut,
                                     volatile __global int* pairCount, int numObjects, int axis, int maxPairs)
{
    int i = get_global_id(0);
    if (i>=numObjects)
        return;
    for (int j=i+1;j<numObjects;j++)
    {
        if(aabbs[i].m_maxElems[axis] < (aabbs[j].m_minElems[axis]))
            break;
        if (TestAabbAgainstAabb2GlobalGlobal(&aabbs[i],&aabbs[j]))
        {
            int2 myPair;
            myPair.x = aabbs[i].m_minIndices[3];
            myPair.y = aabbs[j].m_minIndices[3];
            int curPair = atomic_inc (pairCount);
            if (curPair<maxPairs)
            {
                pairsOut[curPair] = myPair; //flush to main memory
            }
        }
    }
}
```

See https://github.com/erwincoumans/experiments/blob/master/openc1/broadphase_benchmark/sap.cl

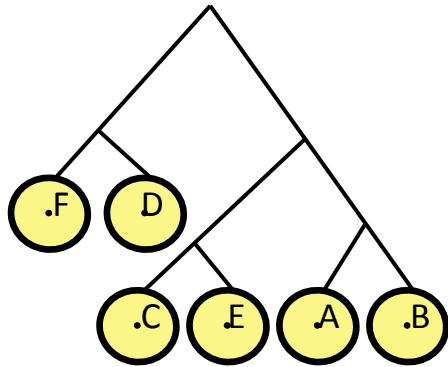
Further GPU SAP optimizations

- Shared sliding window of AABBs per workgroup
 - store 128 AABBs in local memory
- Buffer the output pairs in private memory
 - reduce the use of global atomics (atomic_add)
- Load balancing
 - split work of large objects into multiple work items

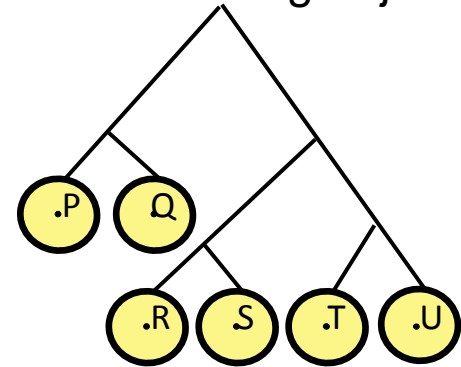
See <http://graphics.ewha.ac.kr/gSaP>

Dynamic AABB tree broadphase

S: static/sleeping objects



M: moving objects



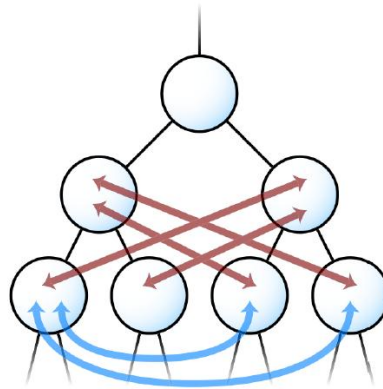
- Find overlapping pairs:
 - overlap M versus M and Overlap M versus S

Incremental tree update

- If new AABB is contained by old do nothing
- Otherwise remove and re-insert leaf
 - Re-insert at closest ancestor that was not resized during remove
- Expand AABB with margin
 - Avoid updates due to jitter or small random motion
- Expand AABB with velocity
 - Handle the case of linear motion over n frames

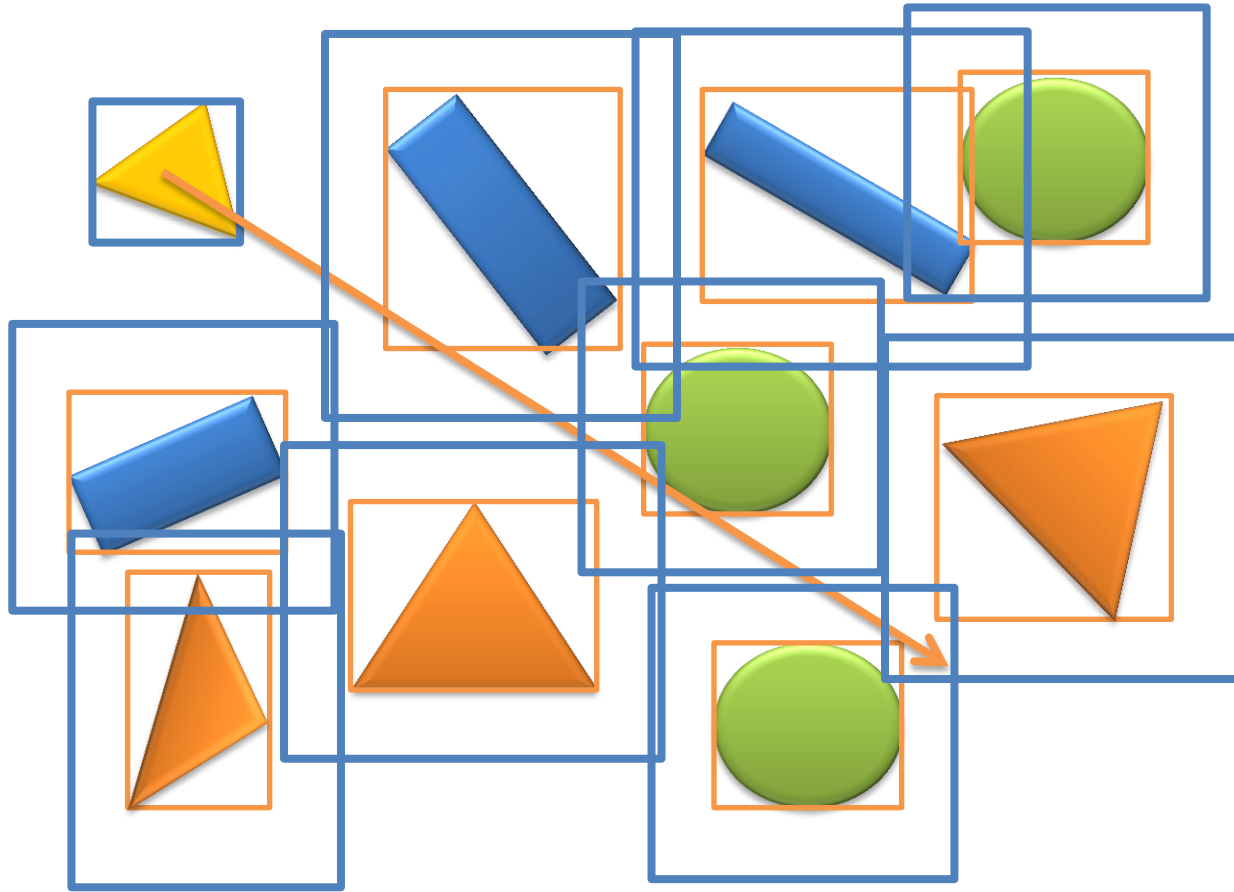
Tree balancing

- Incrementally optimize tree
 - removal/re-inserting small percentage of nodes each step
- Could use tree rotations instead



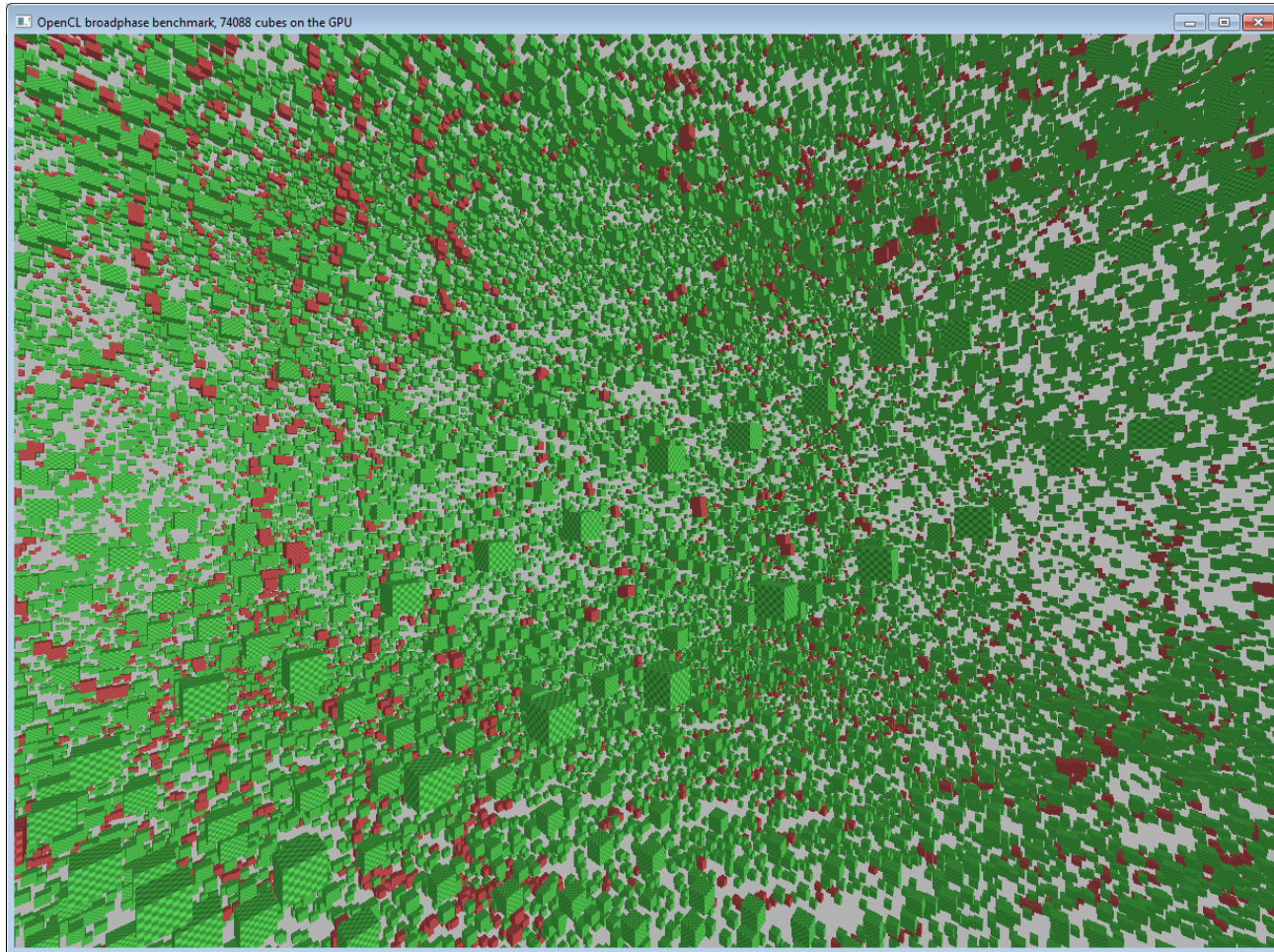
- See "Fast, Effective BVH Updates for Animated Scenes", Kopta, I3D 2012

AABB tree swept query



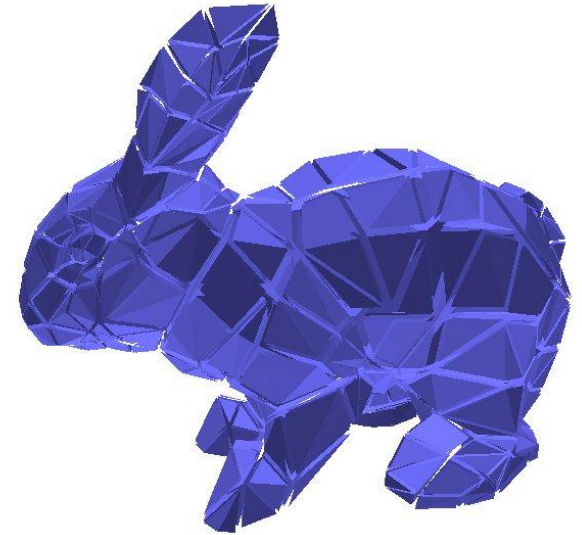
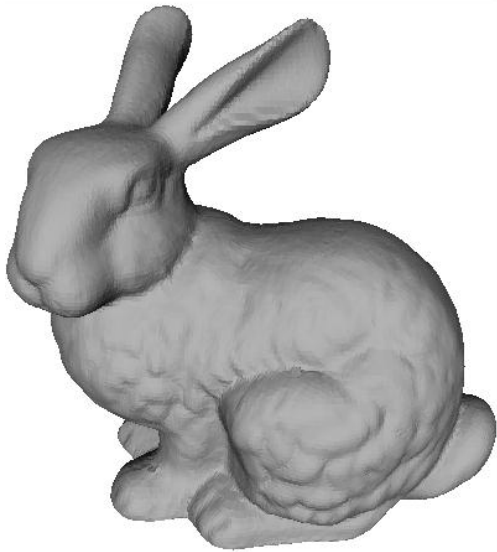
- See Bullet's `btDbvtBroadphase::aabbTest`

Broadphase benchmark (GPU)



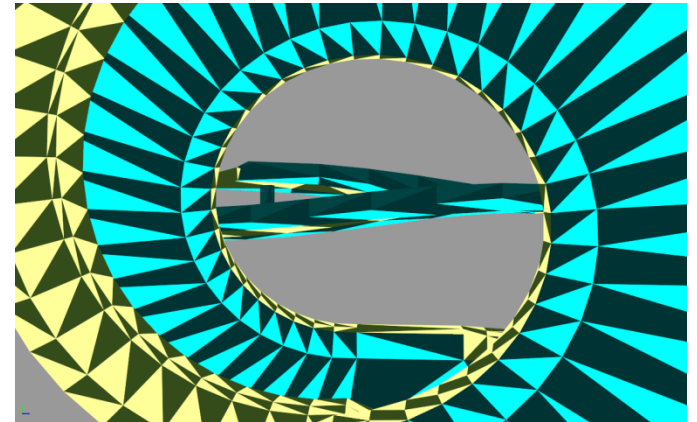
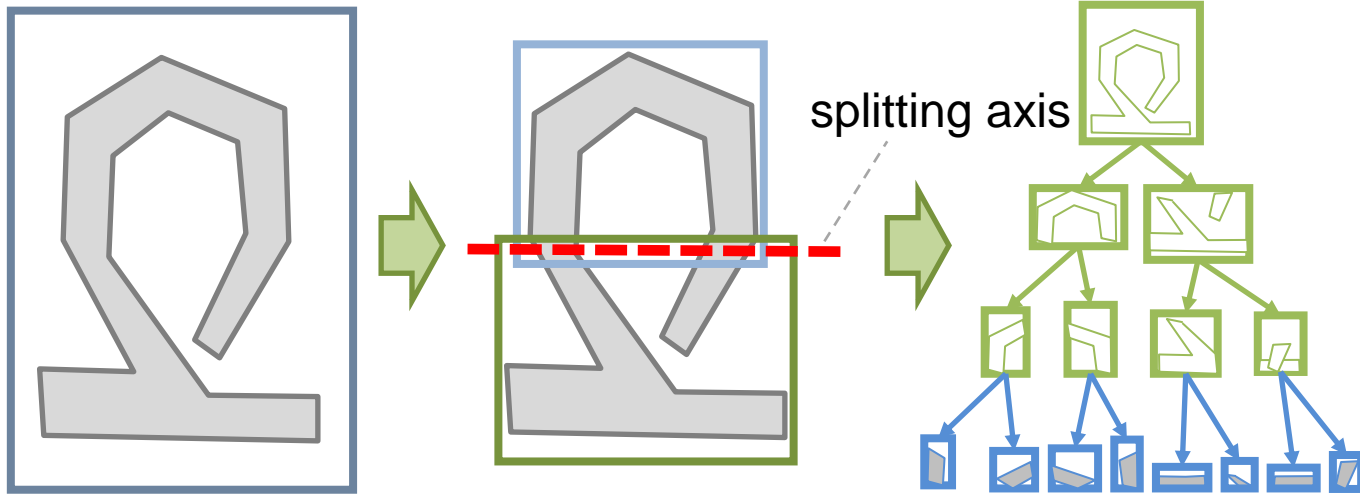
Midphase

- An object-space acceleration structure to cull parts of a complex/concave model



- See Hierarchical Approximate Convex Decomposition, K. Mamou, ICIP 2009 <http://sourceforge.net/projects/hacd>

Midphase: concave triangle meshes

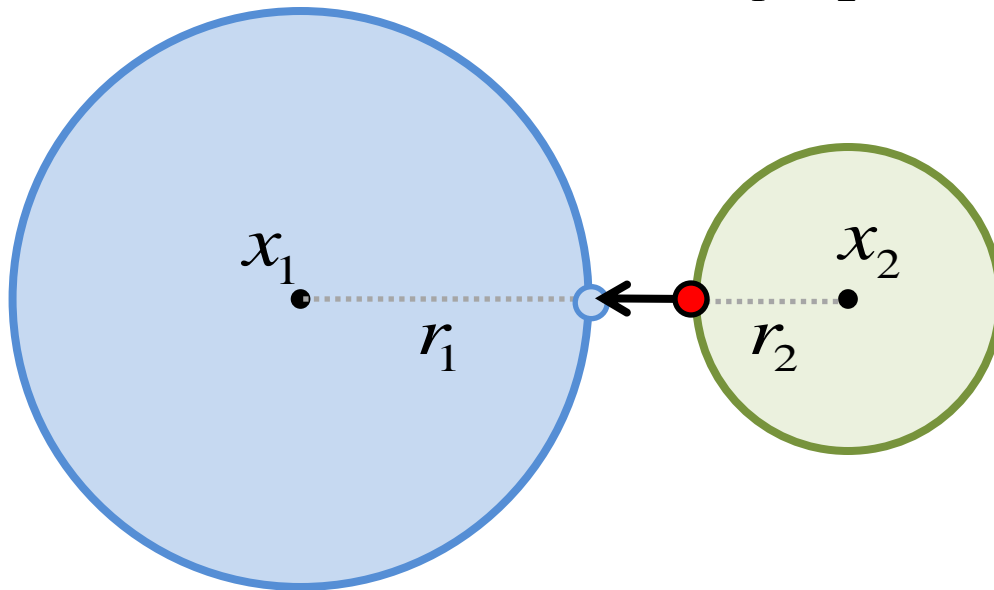


Narrowphase

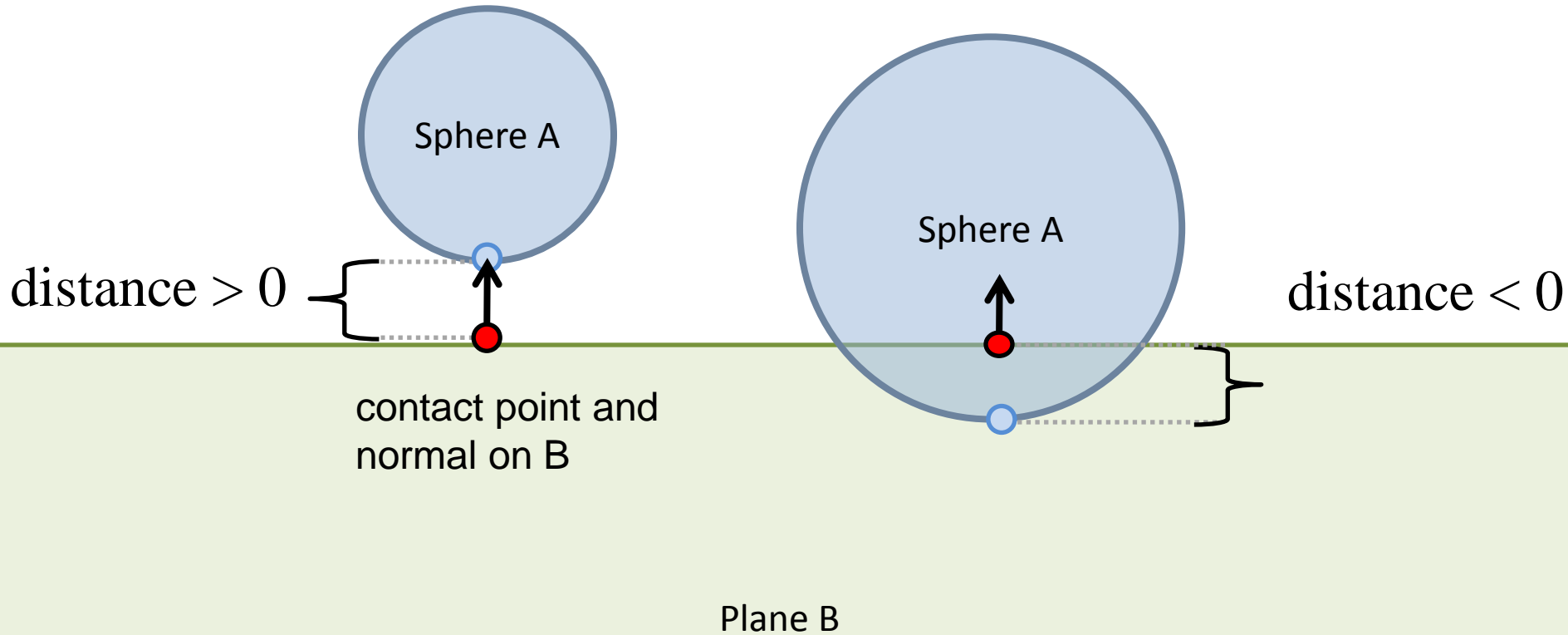
- closest point, normal, distance/penetration
- contact (manifold) generation
- time of impact computation

Closest points

$$C(x_1, x_2) = \|x_1 - x_2\| - (r_1 + r_2)$$

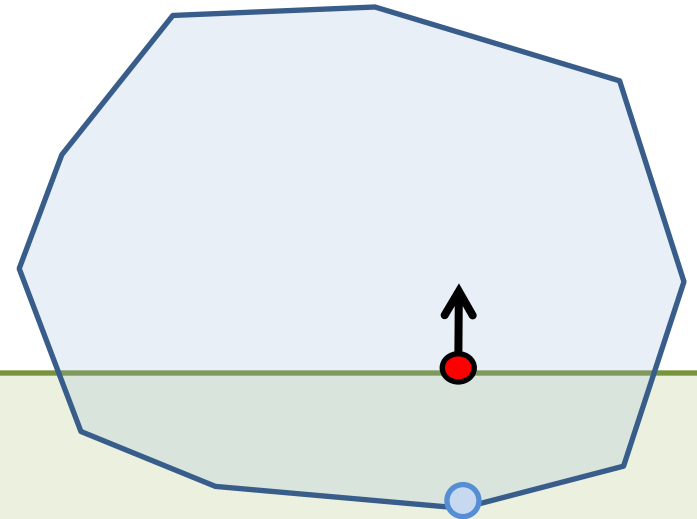
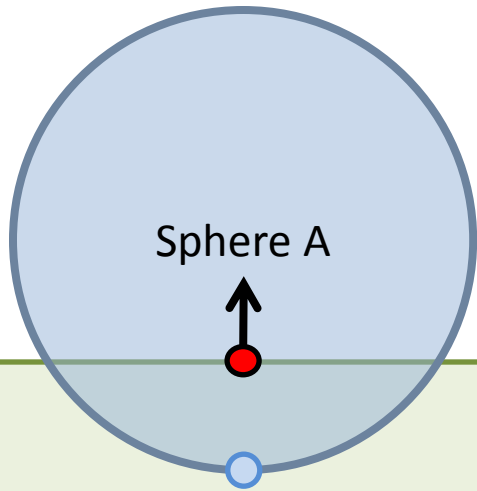


Closest points and penetration



Support mapping

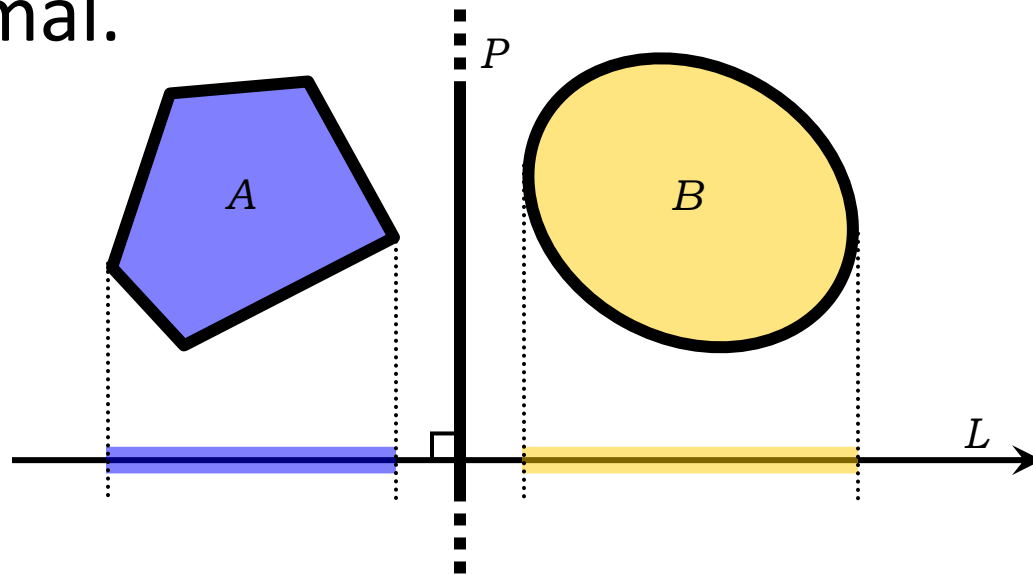
$$S_c(v) = \max\{v \cdot x : x \in C\}$$



Plane B

Separating Axis

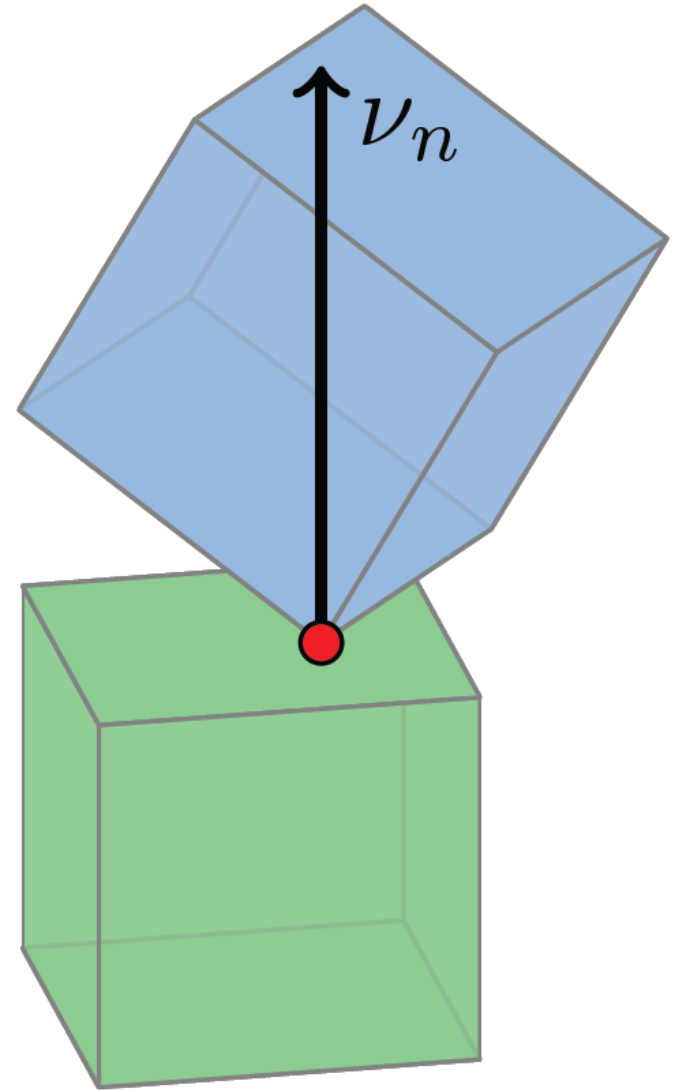
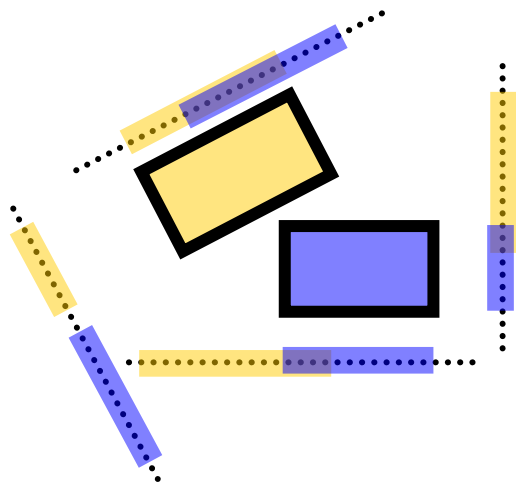
- Separation w.r.t a plane $P \Leftrightarrow$ separation of the orthogonal projections onto any line L parallel to plane normal.



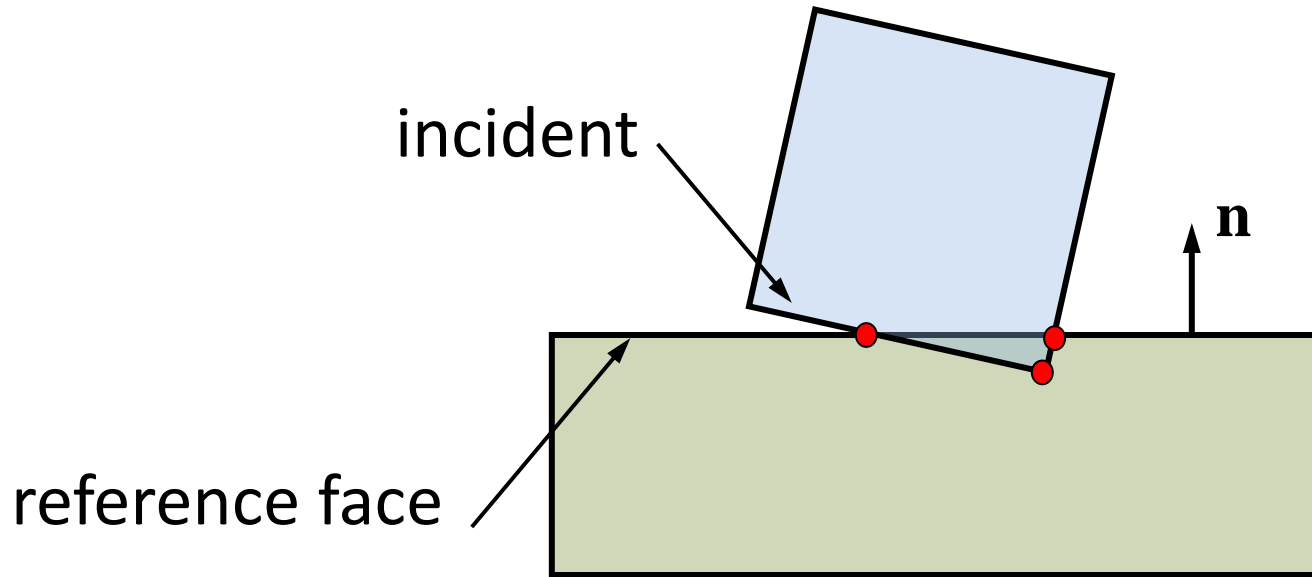
- We can use the support mapping for this projection

Separating Axis for Convex Polyhedra

- Face normal A
- Face normal B
- Edge-Edge normal
- Four axes for two 2D OBBs:

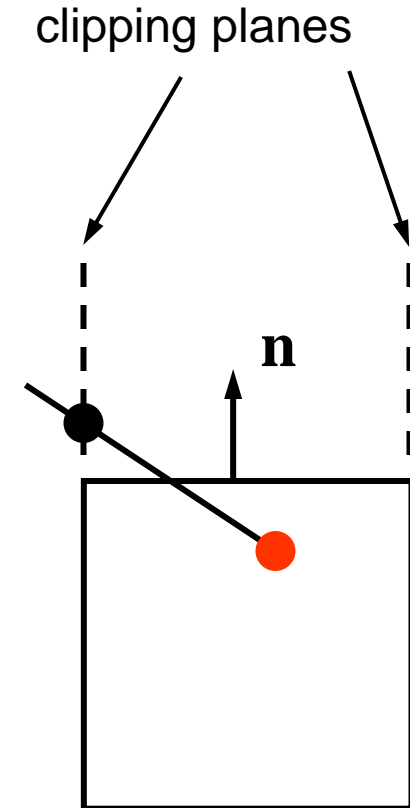
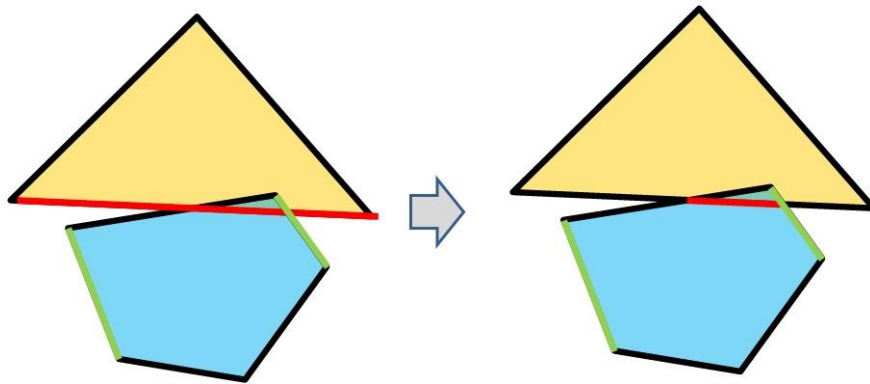


Multiple Contact Points



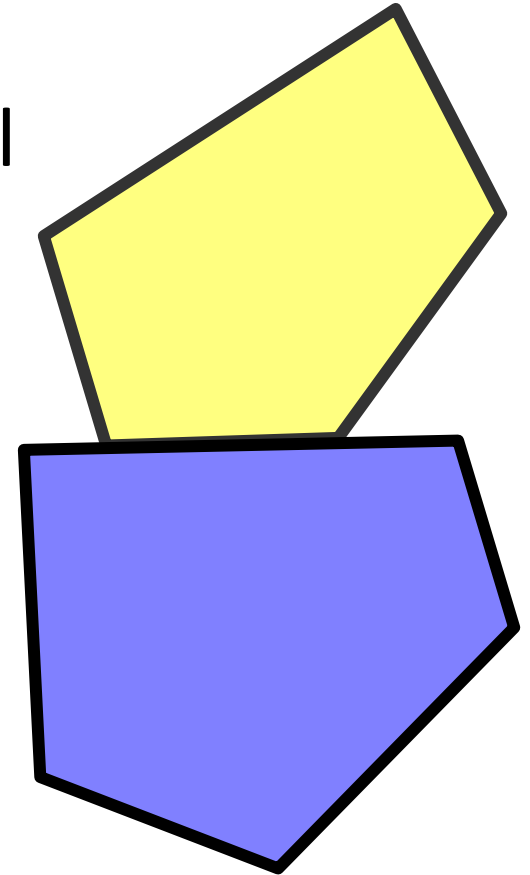
Sutherland Hodgman clipping

- Clip incident face against reference face side planes
- Consider clip points with positive penetration



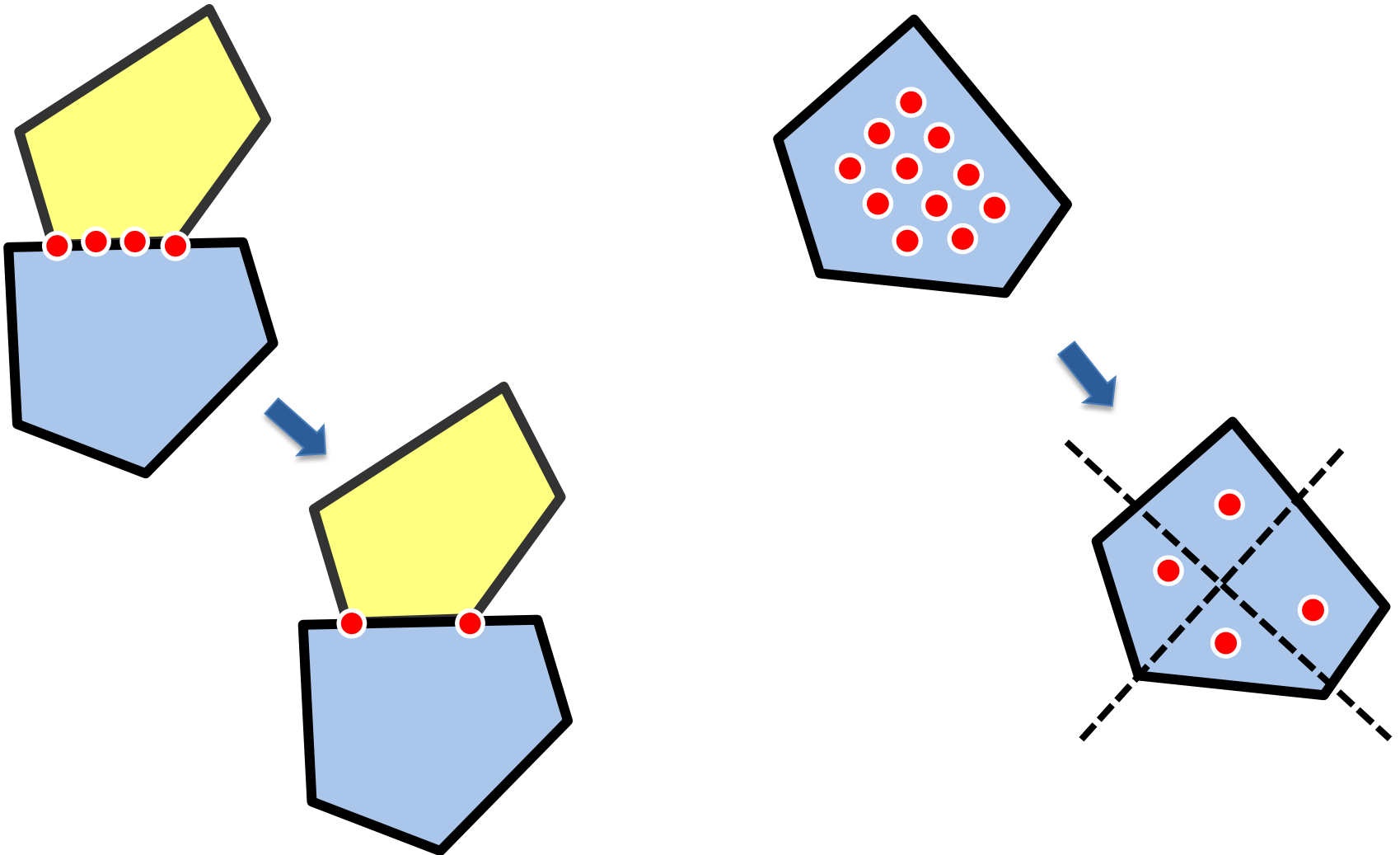
GPU parallel SAT implementation

- Test all separating axis in parallel
 >90% of time spend here
- Clip features in parallel
- Parallel contact reduction

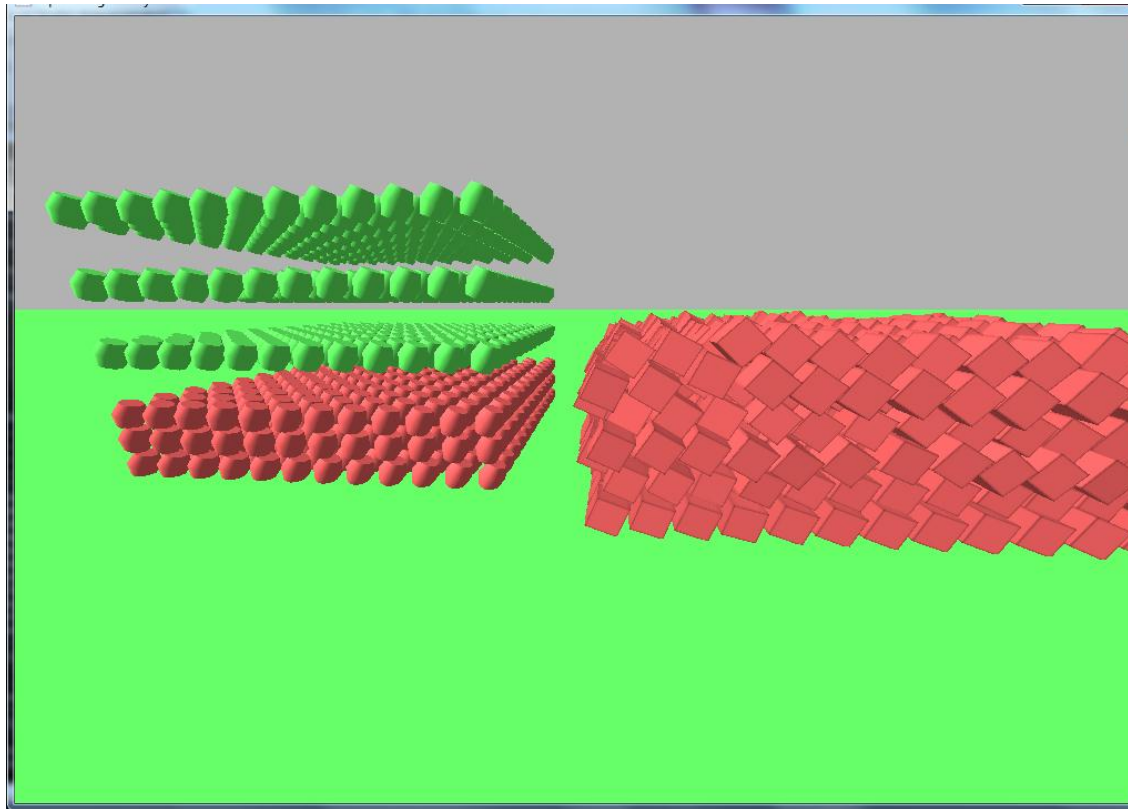


- See https://github.com/erwincoumans/experiments/blob/master/opencl/gpu_rigidbody_pipeline2/sat.cl

Contact Reduction

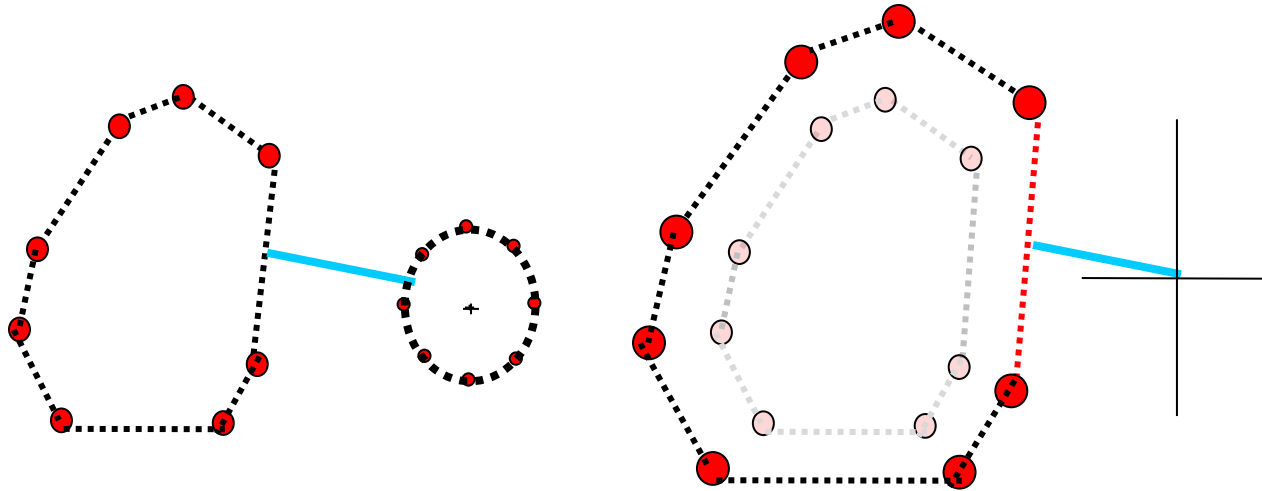


GPU SAT collision detection



- Full source code and windows precompiled executable at <https://github.com/erwincoumans/experiments>

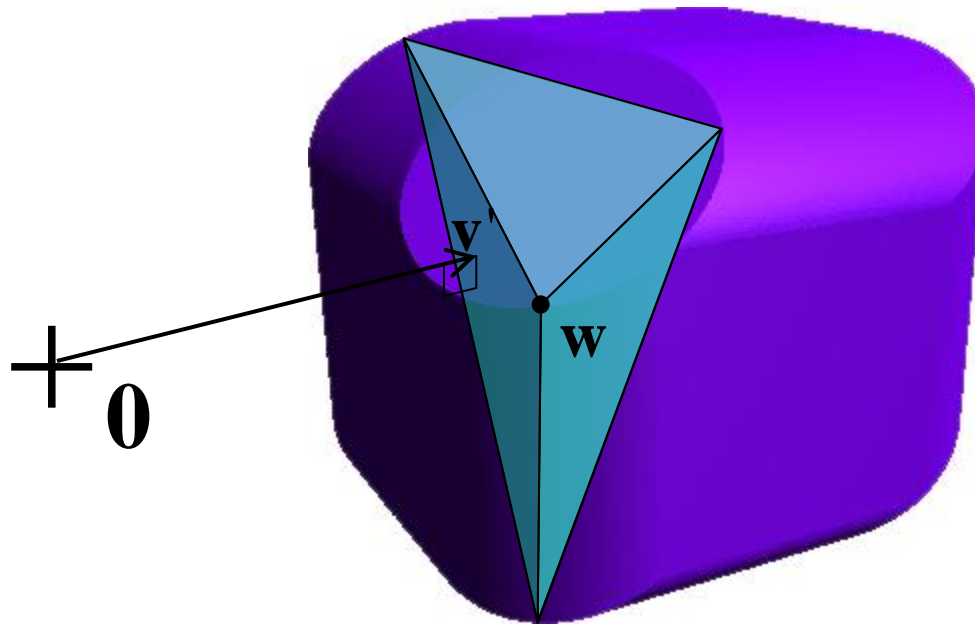
GJK and Minkowski Sum



$$S_{A+B}(\mathbf{v}) = S_A(\mathbf{v}) + S_B(\mathbf{v})$$

$$S_{A-B}(\mathbf{v}) = S_A(\mathbf{v}) - S_B(-\mathbf{v})$$

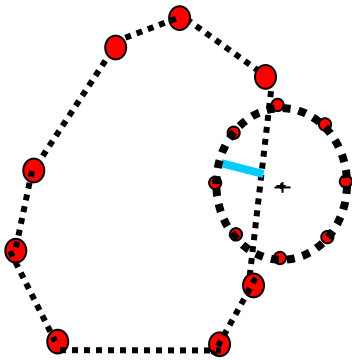
GJK closest point computation



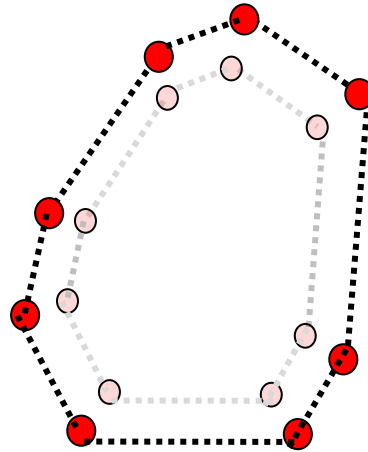
- Slide taken from "gdc2006_vandenBergen_Gino_Physics_Tut.ppt"
See <http://dtecta.com>

Expanding Polytope Algorithm (EPA)

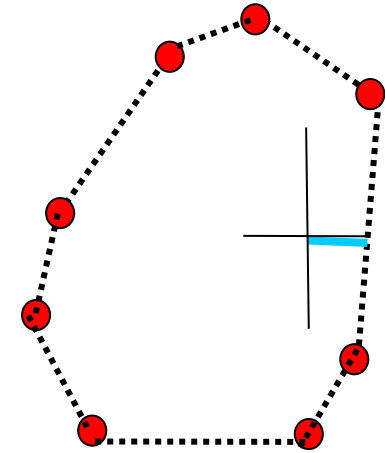
Overlapping objects



Minkowski Sum

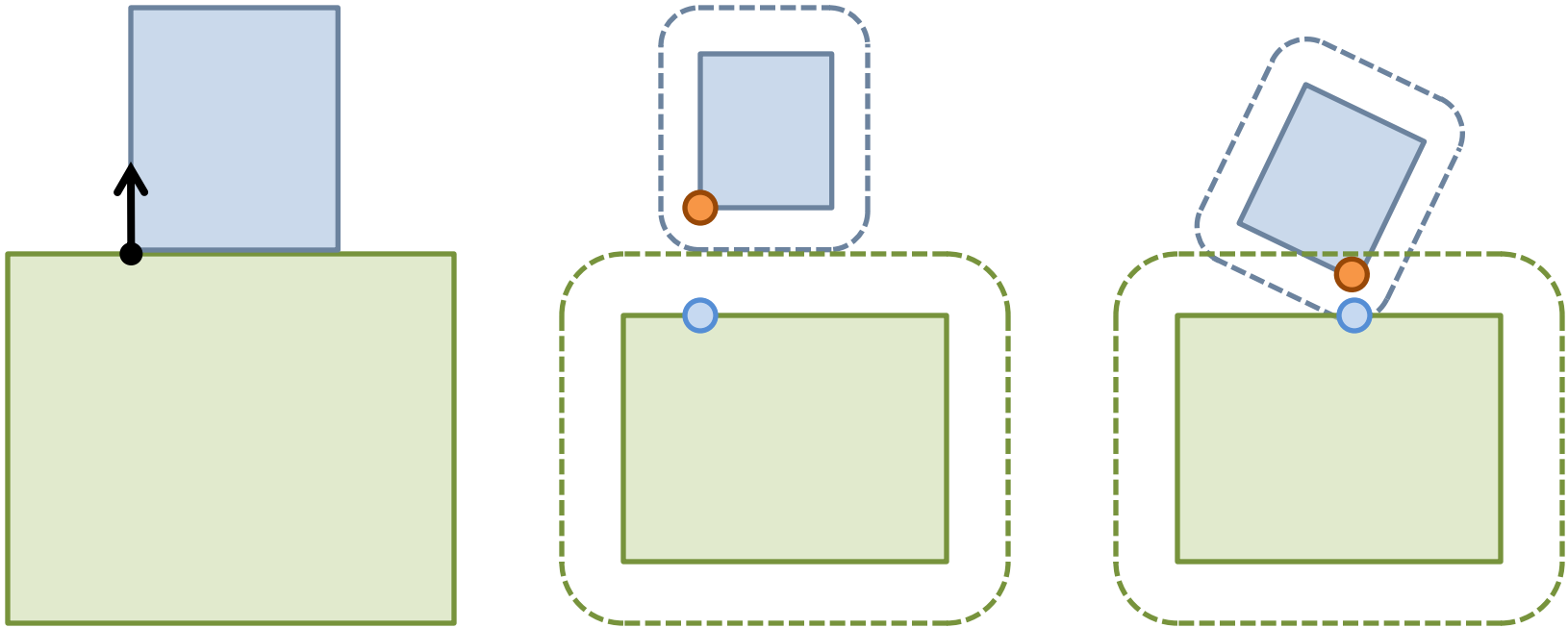


Minimal Translational Distance

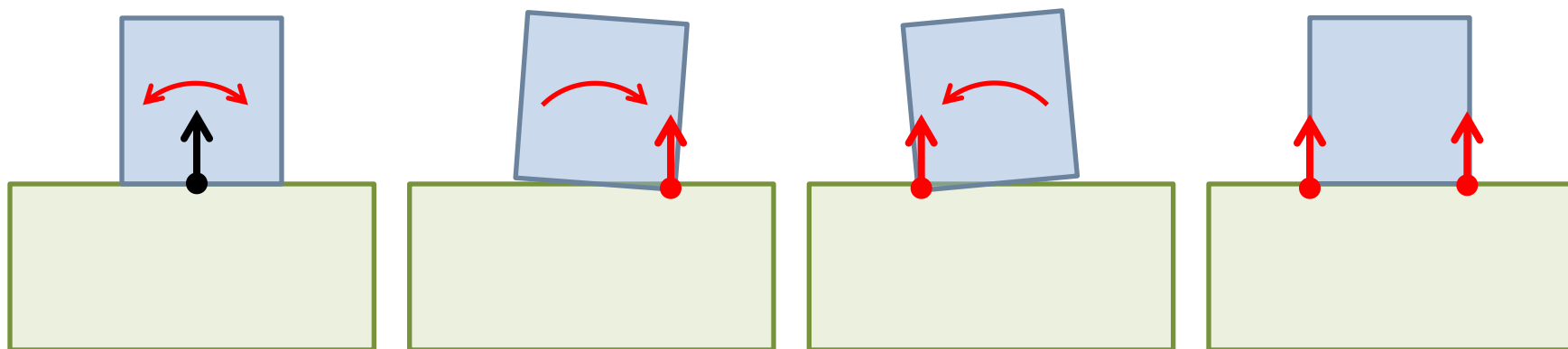


Collision margins

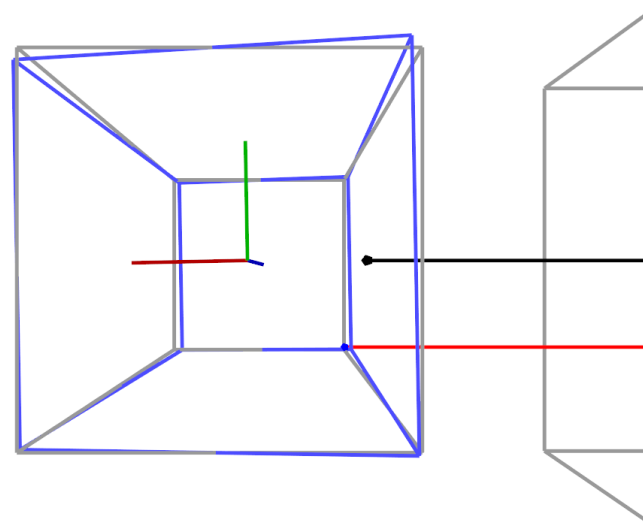
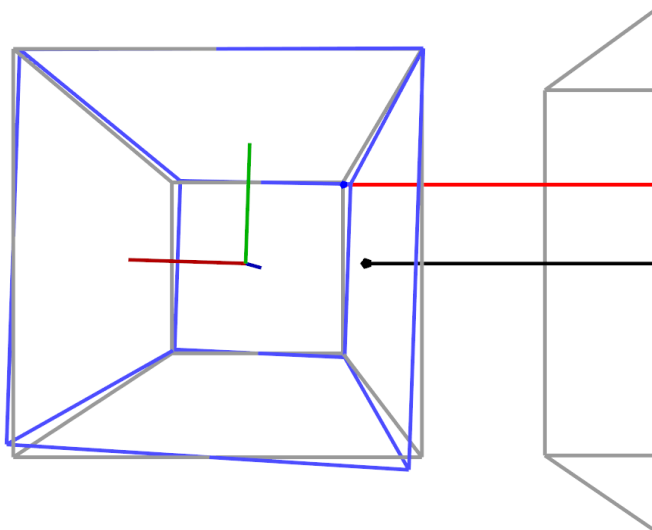
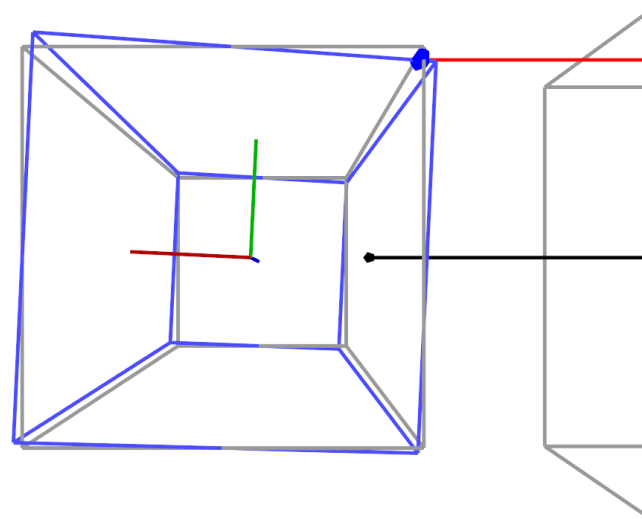
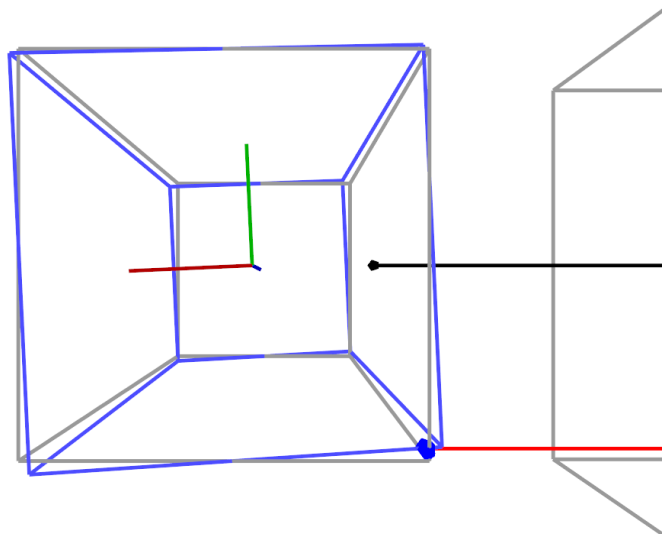
- GJK doesn't work in penetrating cases
 - and penetration depth calculation is a bit slower



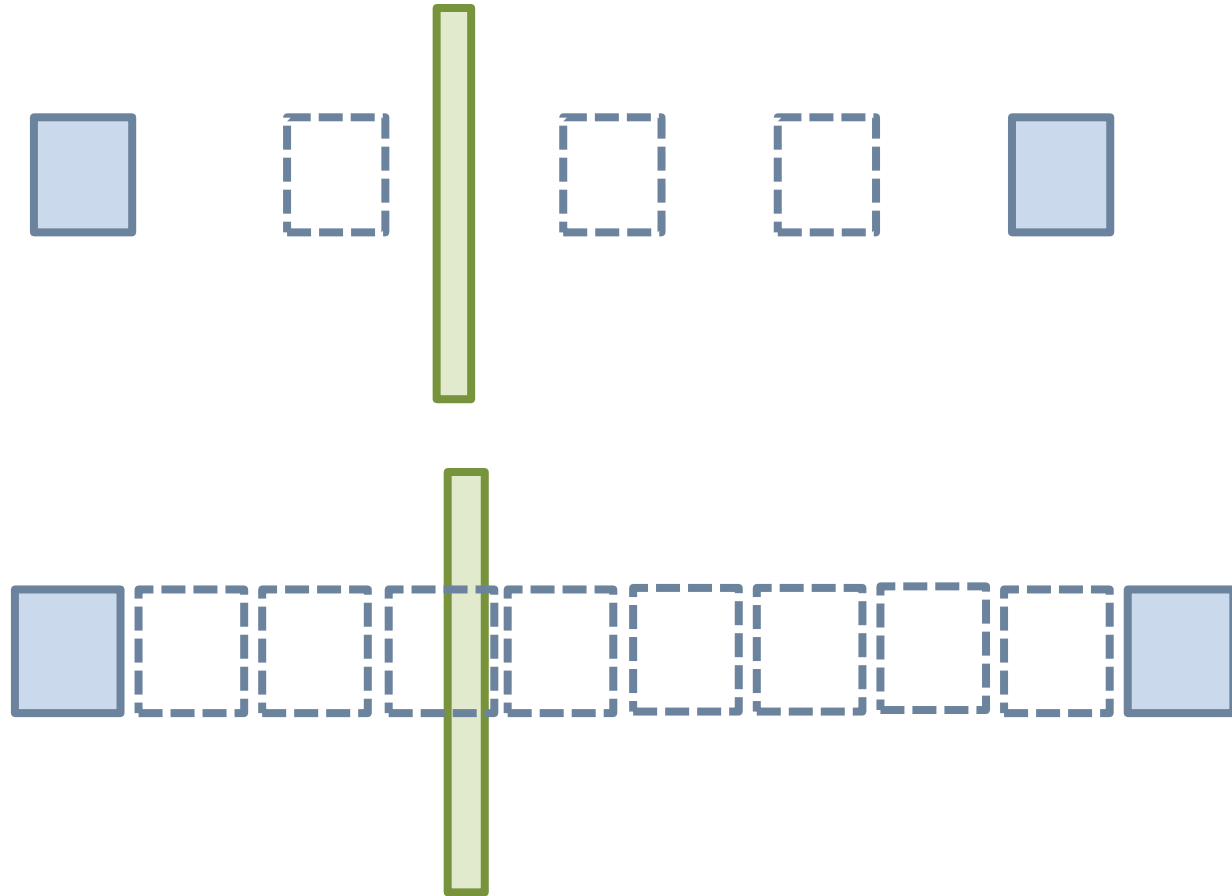
Contact caching and perturbation



Perturbating in 3D

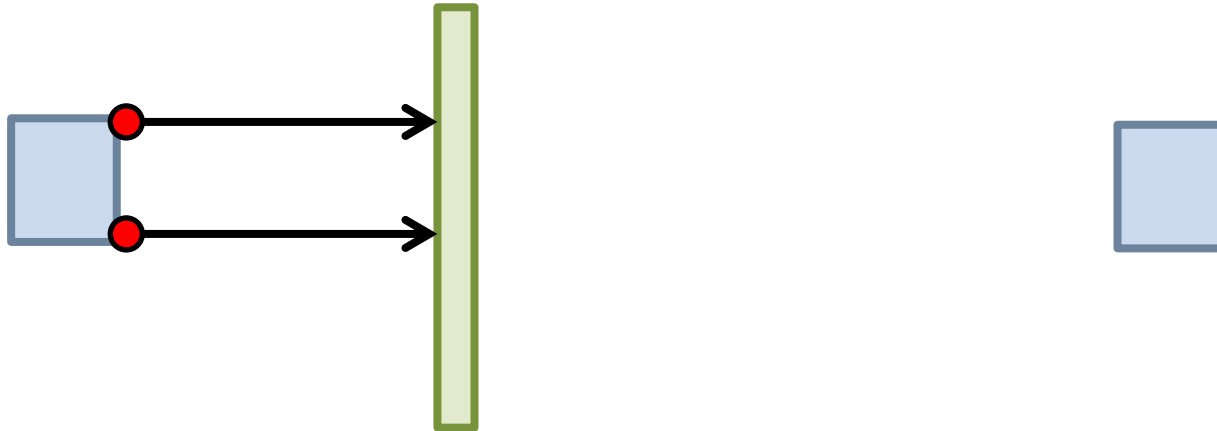


Tunneling in Discrete Physics

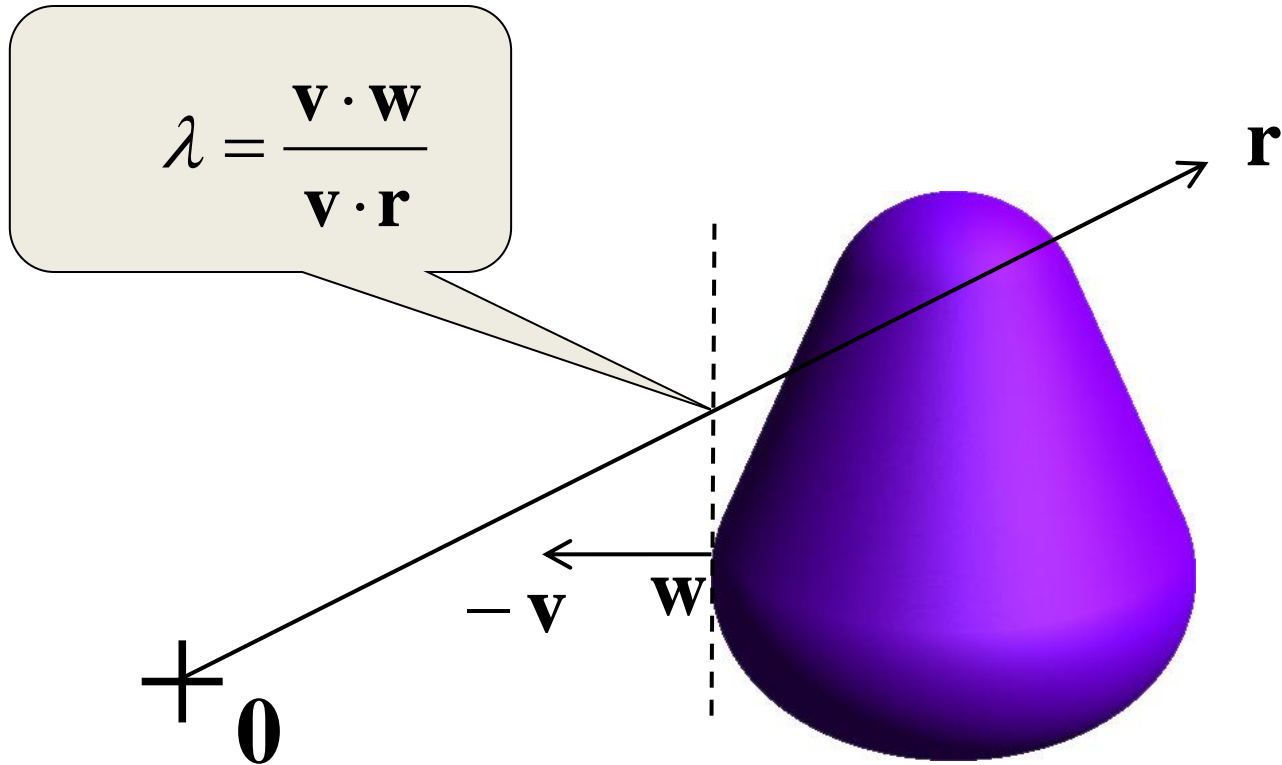


Continuous Collision Detection

- Add potential (future) contact constraints



Ray Clipping

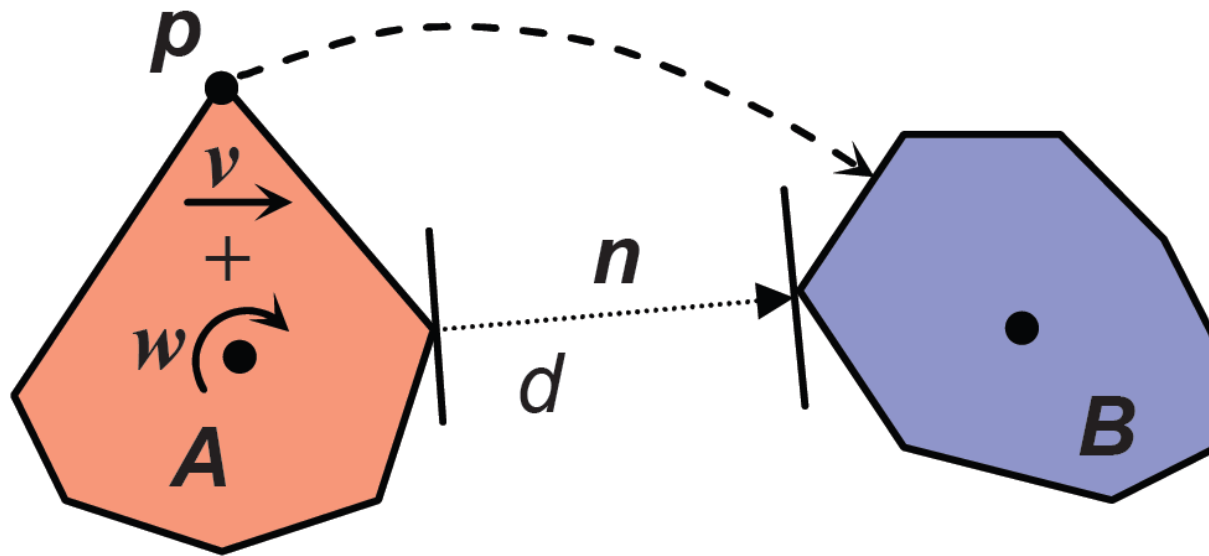


Slide taken from "gdc2006_vandenBergen_Gino_Physics_Tut.ppt"

See <http://dtecta.com>

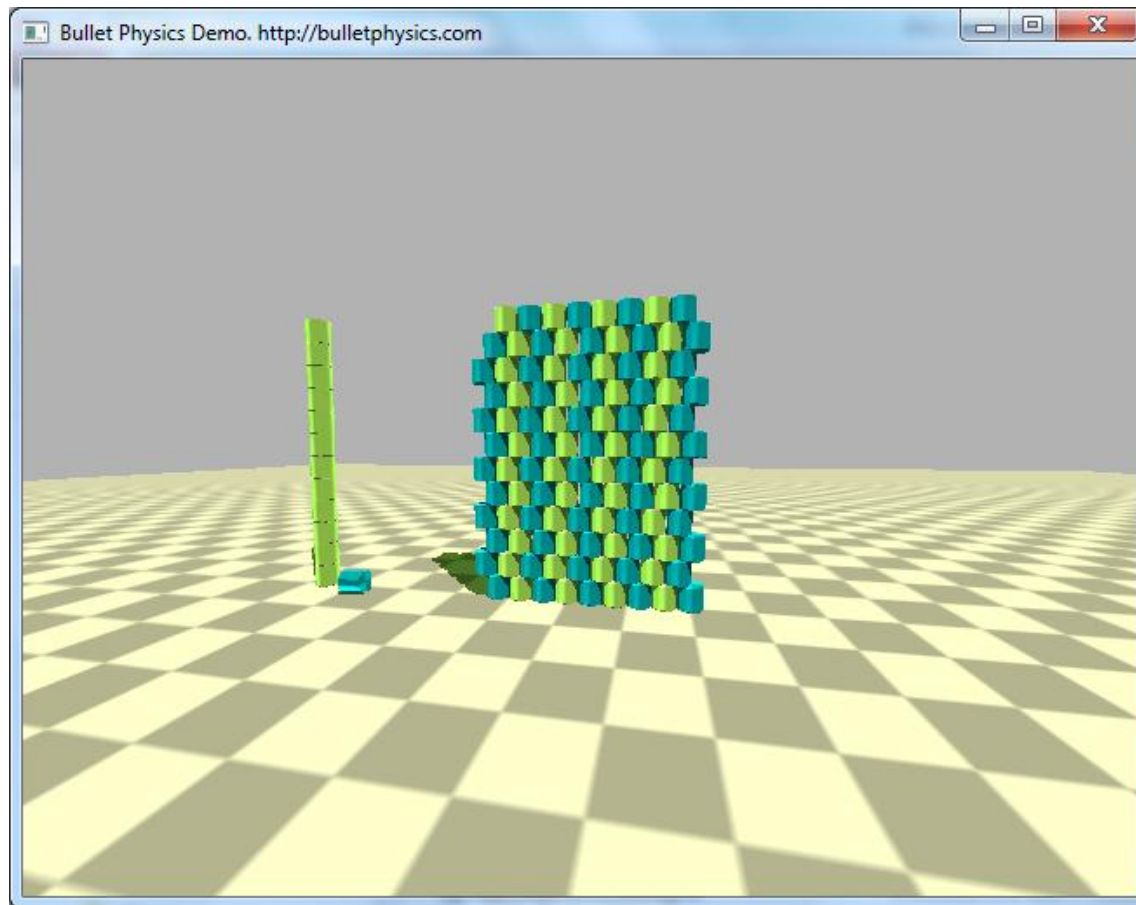
<http://code.google.com/p/bullet/source/browse/trunk/src/BulletCollision/NarrowPhaseCollision/btGjkConvexCast.cpp>

Conservative Advancement



- See <http://graphics.ewha.ac.kr/CATCH/>
- <http://code.google.com/p/bullet/source/browse/trunk/src/BulletCollision/NarrowPhaseCollision/btContinuousConvexCollision.cpp>

Demo



Thanks!

Contact

- erwin.coumans@gmail.com
- <http://bulletphysics.org>
- GPU research: <http://github.com/erwincoumans/experiments>

References

- Game Physics Pearls, Gino van den Bergen, A.K. Peters
- Real-time Collision Culling of a Million Bodies on Graphics Processing Units, <http://graphics.ewha.ac.kr/gSaP>
- <http://graphics.ewha.ac.kr/CATCH/>