The Experimental Ideal

EC 607, Set 02

Edward Rubin

Prologue

Schedule

Last time

Research basics, our class, and `R`

Today

Material: The Rubin causal model (not mine), Chapter 2 MHE.

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Future

Lab: Meet Kyu and start deepening R knowledge.

Long run: Deepen understandings/intuitions for causality and inference.

Review

Research fundamentals

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Research fundamentals

Angrist and Pischke provide four **fundamental questions for research:**

1. What is the **causal relationship of interest**?
2. How would an **ideal experiment** capture this causal effect of interest?
3. What is your **identification strategy**?
4. What is your **mode of inference**?

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Research fundamentals

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3. What is your **identification strategy**?
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Seemingly straightforward questions can be fundamentally unanswerable.

General research recommendations

More unsolicited advice:

- Be curious.
- Ask questions.
- Attend seminars.
- Meet faculty (UO + visitors).
- Focus on learning—especially intuition.†
- **Be kind and constructive.**

† *Learning* is not always the same as getting good grades.

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What's so great about experiments?

Science widely regards **experiments as the gold standard** for research.

But why? The costs can be substantial.

Costs

- slow and expensive
- heavily regulated by (risk-averse?) review boards
- can abstract away from the actual question/setting

Benefits

So the benefits need to be pretty large, right?

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Example: Hospitals and health

Imagine we want to know the **causal effect of hospitals on health**.

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Research question

Within the population of poor, elderly individuals, does visiting the emergency room for primary care improve health?

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Empirical exercise

1. Collect data on *health status* and *hospital visits*.
2. Summarize health status by hospital-visit group.

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Example: Hospitals and health

Our empirical exercise from the 2005 National Health Inteview Survey:

Group	Sample Size	Mean Health Status	Std. Error
Hospital	7,774	3.21	0.014
No hospital	90,049	3.93	0.003

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Potential outcomes framework

Let's develop a framework to better discuss the problem here.

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Let's develop a framework to better discuss the problem here.

- Binary treatment variable (*e.g.*, hospitalized): $\mathbf{D}_i = \mathbf{0}, \mathbf{1}$
- Outcome for individual i (*e.g.*, health): $\mathbf{Y}_i$

This framework has a few names...

- Neyman potential outcomes framework
- Rubin causal model
- Neyman-Rubin `"potential outcome"|"causal" "framework"|"model"`

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Research question: Does $\mathbf{D}_i$ affect $\mathbf{Y}_i$?

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The difference between these two outcomes gives us the **causal effect of hospital treatment**, *i.e.*,

$$\tau_i = \mathrm{Y}_{1i} - \mathrm{Y}_{0i}$$

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#problems

This simple equation

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Accordingly, our methods try to address the related question

> For each Y_{1i}, what is a (reasonably) good counterfactual?

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Problem We cannot directly calculate $\tau_i = \text{Y}_{1i} - \text{Y}_{0i}$.

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Compare outcomes for people who visited the hospital $(\mathbf{Y}_{1i} \mid \mathbf{D}_i = \mathbf{1})$
to outcomes for people who did not visit the hospital $\big(\mathbf{Y}_{0j} \mid \mathbf{D}_j = \mathbf{0}\big)$.

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which gives us the *observed difference in health outcomes*.

Q This comparison will return *an* answer, but is it *the* answer we want?

The experimental ideal

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Q What does $E[\mathrm{Y}_i \mid \mathrm{D}_i = 1] - E[\mathrm{Y}_i \mid \mathrm{D}_i = 0]$ actually tell us?

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Now write out our expectation, apply this definition, do creative math.

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The **first term** is *good variation*—essentially the answer that we want.

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The **average causal effect** of hospitalization *for hospitalized individuals*.

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$$E[Y_{0i} \mid D_i = 1] - E[Y_{0i} \mid D_i = 0]$$

The difference in the average untreated outcome between the treatment and control groups.

Selection bias The extent to which the "control group" provides a bad counterfactual for the treated individuals.

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Angrist and Pischke (MHE, p. 15),

> The goal of most empirical economic research is to overcome selection bias, and therefore to say something about the causal effect of a variable like $\mathbf{D}_i$.

The experimental ideal

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> The goal of most empirical economic research is to overcome selection bias, and therefore to say something about the causal effect of a variable like $\mathbf{D}_i$.

Q So how do experiments—the gold standard of empirical economic (and scientific) research—accomplish this goal and overcome selection bias?

The experimental ideal

Back to experiments

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The experimental ideal

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Q How do experiments overcome selection bias?

A Experiments break the link between potential outcomes and treatment.

In other words: Randomly assigning $\mathbf{D}_i$ makes $\mathbf{D}_i$ independent of which outcome we observe (meaning $\mathbf{Y}_{1i}$ or $\mathbf{Y}_{0i}$).

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Difference in means with random assignment of D_i

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&\quad = E[\tau_i] && \text{Random assignment of } \mathrm{D}_i \text{ breaks selection bias.}
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The experimental ideal

Randomly assigned treatment

The key to avoiding selection bias: **random assignment of treatment**

The experimental ideal

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The key to avoiding selection bias: **random assignment of treatment** (or *as-good-as random assignment*, *e.g.*, natural experiments).

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Random assignment of treatment gives us

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meaning the control group's mean now provides a good counterfactual for the treatment group's mean.

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meaning the control group's mean now provides a good counterfactual for the treatment group's mean.

In other words, there is no selection bias, *i.e.*,

$$\text{Selection bias} = E[\text{Y}_{0i} \mid \text{D}_i = 1] - E[\text{Y}_{0i} \mid \text{D}_i = 0] = \mathbf{0}$$

The experimental ideal

Randomly assigned treatment

Additional benefit of randomization:

The *average treatment effect* is now representative of the *population average*, rather than the *treatment-group average*.

The experimental ideal

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$$\boldsymbol{E}[\tau_i \mid \mathrm{D}_i = 1] = \boldsymbol{E}[\tau_i \mid \mathrm{D}_i = 0] = \boldsymbol{E}[\tau_i]$$

The experimental ideal

Example: Training programs

Governments subsidize training programs to assist disadvantaged workers.

The experimental ideal

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The experimental ideal

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The experimental ideal

Example: Training programs

Governments subsidize training programs to assist disadvantaged workers.

Q Do these programs have the desired effects (*i.e.*, increase wages)?

A Observational studies—comparing wage data from participants and non-participants—often find that people who complete these programs actually make lower wages.

Challenges Participants self select. **+** Programs target lower-wage workers.

The experimental ideal

Example: Training programs

How do we formalize these concerns in our framework?

The experimental ideal

Example: Training programs

How do we formalize these concerns in our framework?

Observational program evaluations

$$E[\text{Wage}_i \mid \text{Program}_i = 1] - E[\text{Wage}_i \mid \text{Program}_i = 0] =$$

$$\underbrace{E[\text{Wage}_{1i} \mid \text{Program}_i = 1] - E[\text{Wage}_{0i} \mid \text{Program}_i = 1]}_{\text{Average causal effect of training program on wages for participants, } i.e., \bar{\tau}_1} +$$

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The experimental ideal

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$$\underbrace{E[\text{Wage}_{0i} \mid \text{Program}_i = 1] - E[\text{Wage}_{0i} \mid \text{Program}_i = 0]}_{\text{Selection bias}}$$

If the program attracts/selects individuals who, on average, have lower wages without the program (sort of the point of the program), then we have negative selection bias.

The experimental ideal

Example: Training programs

$$E[\text{Wage}_i \mid \text{Program}_i = 1] - E[\text{Wage}_i \mid \text{Program}_i = 0] =$$

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So even if the program, on average, has an positive wage effect (in the participant group), *i.e.*, $\bar{\tau}_1 > \mathbf{0}$, we will detect a lower effect due to the negative selection bias.

The experimental ideal

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So even if the program, on average, has an positive wage effect (in the participant group), *i.e.*, $\bar{\tau}_1 > 0$, we will detect a lower effect due to the negative selection bias.

If the bias is sufficiently large (relative to the treatment effect), our estimate will even get the sign of the effect wrong.

The experimental ideal

Example: Training programs

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So even if the program, on average, has an positive wage effect (in the participant group), *i.e.*, $\bar{\tau}_1 > \mathbf{0}$, we will detect a lower effect due to the negative selection bias.

If the bias is sufficiently large (relative to the treatment effect), our estimate will even get the sign of the effect wrong.

Related While observational studies typically found negative program effects, several experiments found positive program effects.

The experimental ideal

Example: The STAR experiment

The Tennessee STAR experiment is a famous/popular example of an experiment that allows us to answer an important social/policy question.

Research question Do classroom resources affect student performance?

The experimental ideal

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Example: The STAR experiment

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Research question Do classroom resources affect student performance?

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Treatments

1. *Small* classes (13–17 students)
2. *Regular* classes (22–35 students) plus part-time teacher's aide
3. *Regular* classes (22–35 students) plus full-time teacher's aide

The experimental ideal

Example: The STAR experiment

First question Did the randomization balance participants' characteristics across the treatment groups?

The experimental ideal

Example: The STAR experiment

First question Did the randomization balance participants' characteristics across the treatment groups?

Ideally, we would have pre-experiment data on outcome variable.

Unfortunately, we only have a few demographic attributes.

Table 2.2.1, MHE

	Treatment: Class Size			
Variable	**Small**	**Regular**	**Regular + Aide**	**P-value**
Free lunch	0.47	0.48	0.50	0.09
White/Asian	0.68	0.67	0.66	0.26
Age in 1985	5.44	5.43	5.42	0.32
Attrition rate	0.49	0.52	0.53	0.02
K. class size	15.10	22.40	22.80	0.00
K. test percentile	54.70	48.90	50.00	0.00

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Demographics appear balanced across the three treatment groups.

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The three groups differ significantly on attrition rate.

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The randomization generated variation in the treatment.

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The small-class treatment significantly increased test scores.

The experimental ideal

The STAR experiment

The previous table estimated/compared the treatment effects using simple differences in means.

We can make the same comparisons using regressions.

Specifically, we regress our outcome (test percentile) on dummy variables (binary indicator variables) for each treatment group.

The experimental ideal

Example of our three treatment dummies.

i	y_i	Trt_{1i}	Trt_{2i}	Trt_{3i}
1	y_1	1	0	0
2	y_2	1	0	0
$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$
ℓ	y_ℓ	1	0	0
$\ell+1$	$y_{\ell-1}$	0	1	0
$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$
p	y_p	0	1	0
$p+1$	y_{p+1}	0	0	1
$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$
N	y_N	0	0	1

The experimental ideal

Regression analysis

Assume for the moment that the treatment effect is constant[†], *i.e.*,

$$\mathrm{Y}_{1i} - \mathrm{Y}_{0i} = \rho \quad \forall \boldsymbol{i}$$

†You'll often hear econometricians say "homogeneous" (*vs.* "hetergeneous").

The experimental ideal

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then we can rewrite

$$\text{Y}_i = \text{Y}_{0i} + \text{D}_i \left(\text{Y}_{1i} - \text{Y}_{0i} \right)$$

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as

$$\mathrm{Y}_i = \underbrace{\alpha}_{=E[\mathrm{Y}_{0i}]} + \mathrm{D}_i \underbrace{\rho}_{\mathrm{Y}_{1i} - \mathrm{Y}_{0i}} + \underbrace{\eta_i}_{\mathrm{Y}_{0i} - E[\mathrm{Y}_{0i}]}$$

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The experimental ideal

Regression analysis

$$\mathrm{Y}_i = \alpha + \mathrm{D}_i \rho + \eta_i$$

Now write out the conditional expectation of $\mathbf{Y}_i$ for both levels of $\mathbf{D}_i$

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The experimental ideal

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$$Y_i = \alpha + D_i\rho + \eta_i$$

Now write out the conditional expectation of Y_i for both levels of D_i

$$E[Y_i \mid D_i = 1] = E[\alpha + \rho + \eta_i \mid D_i = 1] = \alpha + \rho + E[\eta_i | D_i = 1]$$

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Take the difference…

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The experimental ideal

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Again, our estimate of the **treatment effect** (ρ) is only going to be as good as our ability to shut down the **selection bias**.

Selection bias in regression model: $E[\eta_i | \text{D}_i = 1] - E[\eta_i \mid \text{D}_i = 0]$

Selection bias here should remind you a lot of

The experimental ideal

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There is something in our disturbance η_i that is affecting $\mathbf{Y}_i$ and is also correlated with $\mathbf{D}_i$.

The experimental ideal

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Selection bias here should remind you a lot of **omitted-variable bias.**

There is something in our disturbance η_i that is affecting $\mathbf{Y}_i$ and is also correlated with $\mathbf{D}_i$.

In other metrics-*y* words: Our treatment $\mathbf{D}_i$ is endogenous.

The experimental ideal

Solutions and covariates

Selection bias in regression model: $E[\eta_i | \text{D}_i = 1] - E[\eta_i \mid \text{D}_i = 0]$

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Another potential route to identification is to condition on covariates in the hopes that they "take care of" the relationship between $\mathbf{D}_i$ and whatever is in our disturbance η_i.

Without very clear reasons explaining how you know you've controlled for the "bad variation", clean and convincing identification on this path is going to be challenging.

The experimental ideal

Covariates

That said, covariates can help with two things:

1. Even experiments may need **conditioning/controls**: The STAR experiment was random *within school*—not across schools.

2. Covariates can soak up unexplained variation—**increasing precision.**

The experimental ideal

Covariates

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Now that we've seen regression can analyze experiments, let's estimate the STAR example...

Table 2.2.2, MHE

Explanatory variable	**1**	**2**	**3**
Small class	4.82	5.37	5.36
	(2.19)	(1.26)	(1.21)
Regular + aide	0.12	0.29	0.53
	(2.23)	(1.13)	(1.09)
White/Asian			8.35
			(1.35)
Female			4.48
			(0.63)
Free lunch			-13.15
			(0.77)
School F.E.	F	T	T

The omitted level is *Regular* (with part-time aide).

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Results without other controls are very similar to the difference in means.

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School FEs enforce the experiment's design and increase precision.

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Additional controls slightly increase precision.

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