

# Post-hoc counterfactual generation with supervised autoencoder

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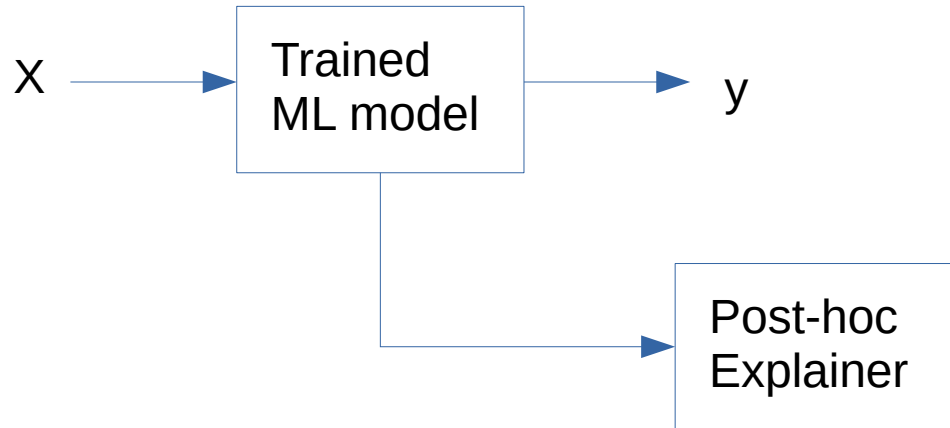
# Context

- Supervised learning classifier

$$f_{pred} : \mathcal{X} \rightarrow \mathcal{Y} \quad \{\mathbf{x}_i, y_i\}_{i=1}^n$$
$$\mathcal{Y} = \{1, 2, \dots, C\}$$

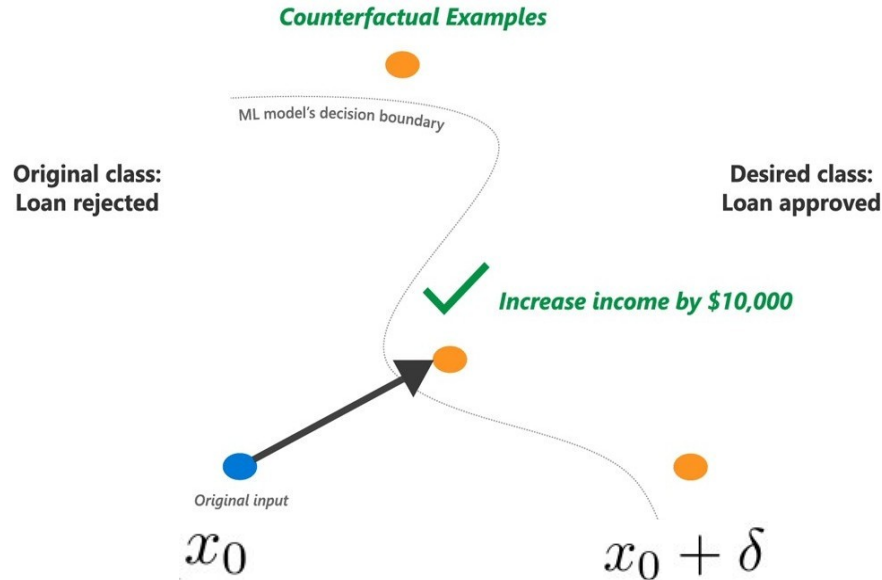
- Post-hoc explanations

*Apply an explainable method on a trained machine learning model*



# Explanation by counterfactuals

Counterfactual explanation for ML models: Smallest change of feature values that changes a prediction to a given output.



Source: Microsoft Research Blog

Sandra Wachter et al, *Counterfactual Explanations without Opening the Black Box: Automated Decisions and the GDPR*, 2018, *Harvard Journal of Law & Technology* .

# Explanation by counterfactuals

Counterfactual examples are most of the time found by minimizing a **cost function**.

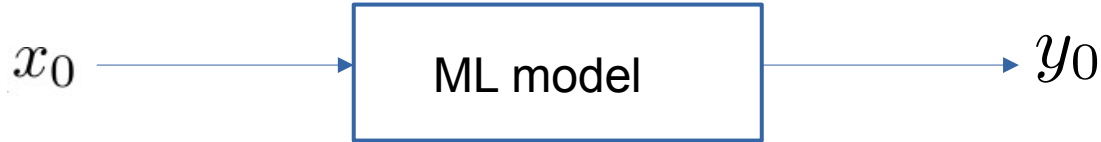
- Generally **2 terms that are related to the definition** (closeness to the example + different predicted class)
- **Many possible cost functions** and implementations of the optimization method, depending of the expected properties of the counterfactual.  
Ex: Sparsity, actionability, closeness to training data, diversity...
- Many open challenges: **no consensus** on what a good counterfactual is and how it can be evaluated.

*Verma, S., Dickerson, J., & Hines, K. (2020). Counterfactual Explanations for Machine Learning: A Review. arXiv preprint arXiv:2010.10596.*

# Interpretable Counterfactual Explanations guided by prototypes

3 steps process:

1)



*Train a machine learning model to predict a given class ( $y_0$ )*

# Interpretable Counterfactual Explanations guided by prototypes

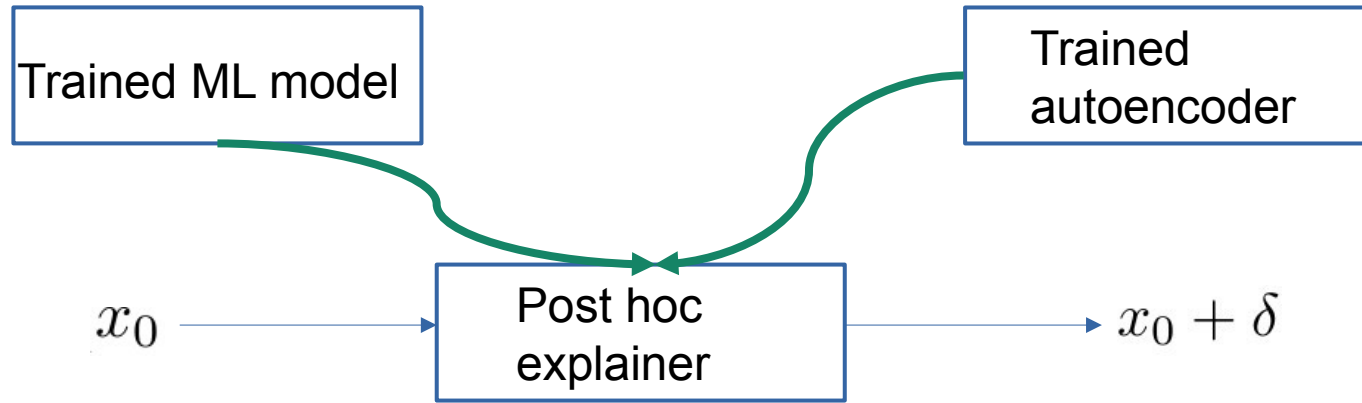
2)



*Train an autoencoder to reconstruct a sample ( $x_0$ )*

# Interpretable Counterfactual Explanations guided by prototypes

3)



*Find a counterfactual ( $x_0 + \delta$ ) by optimizing a cost function that uses the trained autoencoder and the trained ML model*

*Limit: requires the training of 2 models*

# The cost function

$$\min_{\delta} (c \cdot f_{\kappa}(x_0, \delta) + f_{\text{dist}}(\delta) + L_{AE} + L_{\text{proto}})$$

$x_0$ : Example to explain

$x_0 + \delta$ : Counterfactual example



# The cost function

$$\min_{\delta} (\underline{c \cdot f_{\kappa}(x_0, \delta)} + f_{\text{dist}}(\delta) + L_{AE} + L_{\text{proto}})$$

$$f_{\kappa}(x_0, \delta) = \max \left( [f_{\text{pred}}(x_0 + \delta)]_{y_0} - \max_{y_i \neq y_0} [f_{\text{pred}}(x_0 + \delta)]_{y_i}, -\kappa \right)$$

***Term to ensure that the predicted class for counterfactual is different***

# The cost function

$$\min_{\delta} (c \cdot f_{\kappa}(x_0, \delta) + \underline{f_{\text{dist}}(\delta)} + L_{AE} + L_{\text{proto}})$$

$$f_{\text{dist}}(\delta) = \beta \cdot \|\delta\|_1 + \|\delta\|_2^2.$$

***Minimize distance between counterfactual and example / Sparse perturbation***

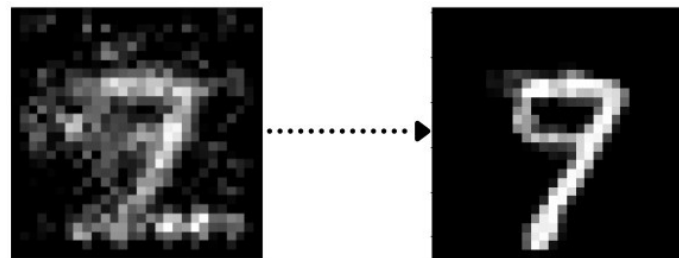
# The cost function

$$\min_{\delta} (c \cdot f_{\kappa}(x_0, \delta) + f_{\text{dist}}(\delta) + \underline{L_{AE}} + L_{\text{proto}})$$

$$L_{AE} = \gamma \cdot \|x_0 + \delta - \text{AE}_D(x_0 + \delta)\|_2^2.$$

***Reconstruction error of counterfactual evaluated by an autoencoder (AE) trained with a data distribution  $D$ .***

***Penalize out of distribution counterfactuals***

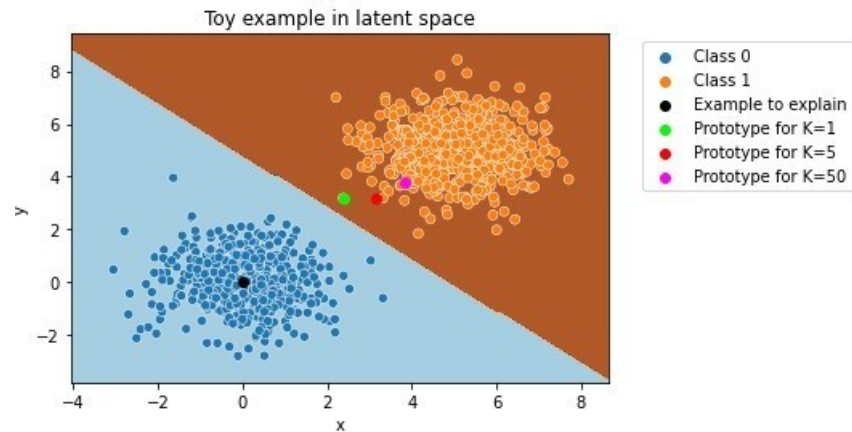


# The cost function

$$\min_{\delta} (c \cdot f_{\kappa}(x_0, \delta) + f_{\text{dist}}(\delta) + L_{AE} + L_{\text{proto}})$$

$$\text{proto}_{y_j} = \frac{1}{K} \sum_{k=1}^K \text{ENC}_D(x_k^i)$$

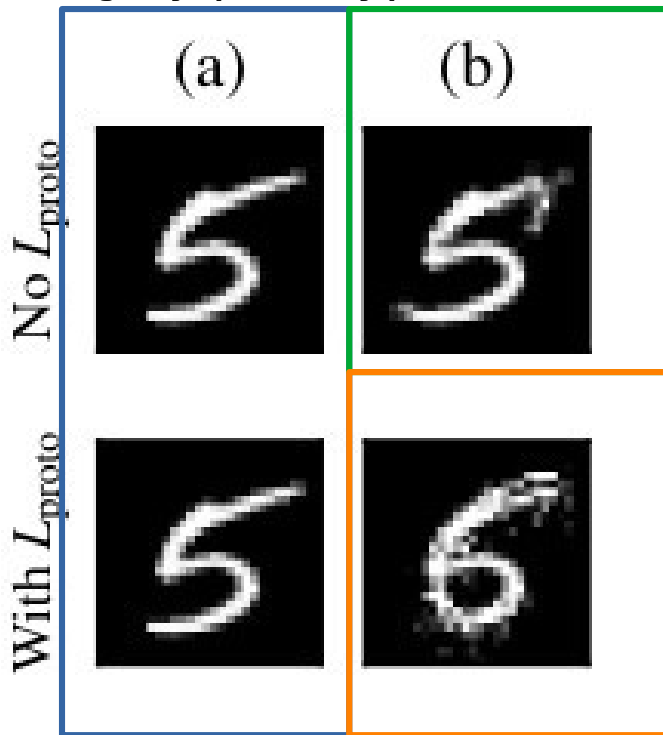
$$L_{\text{proto}} = \theta \cdot \|\text{ENC}_D(x_0 + \delta) - \text{proto}_{y_j}\|_2^2,$$






***Counterfactual examples belong distribution of counterfactual class***

# The cost function

Why guiding by prototype in a latent space?



-  Example predicted as a 5
-  Counterfactual without guiding by prototype, predicted as a 6
-  Counterfactual with guiding by prototype, predicted as a 6

# Illustration of limits



Example predicted as 3

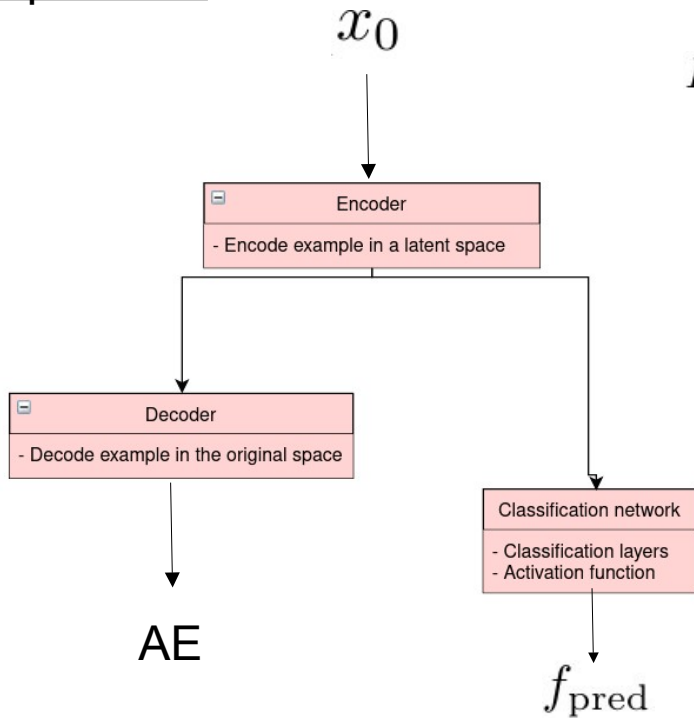


Counterfactual example predicted as a 6  
→ **Not looks like a "6"**

# Our contribution

2 steps process:

1)

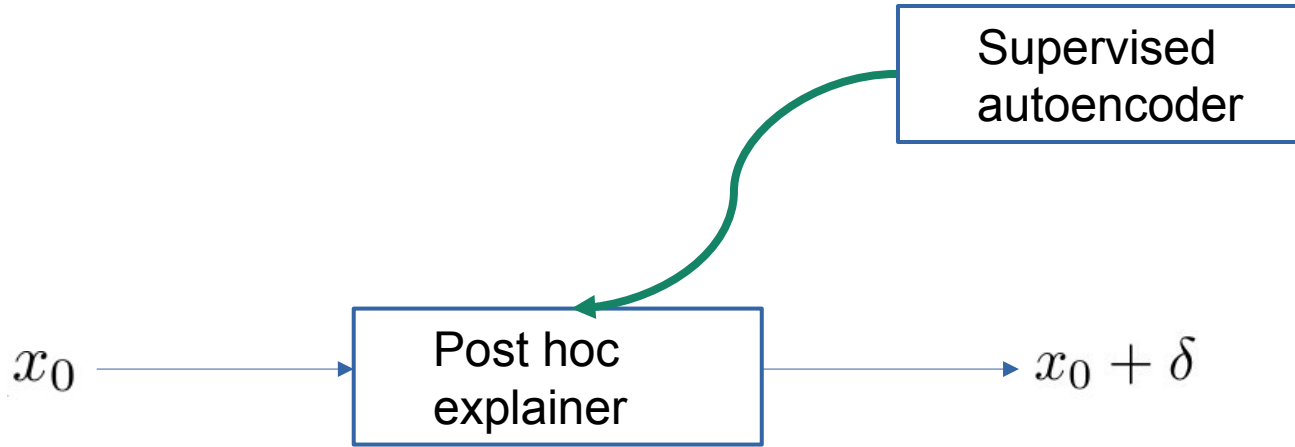


$$L((f_{\text{pred}}, \text{AE}), D) = \underbrace{E(f_{\text{pred}}, D)}_{\text{Classification loss}} + \lambda \underbrace{R(\text{AE}, D)}_{\text{Reconstruction loss}}$$

- Train a supervised autoencoder
- We then obtain:
  - A classifier
  - An autoencoder

# Our contribution

2)



*Find a counterfactual ( $x_0 + \delta$ ) by optimizing a cost function*

$$\min_{\delta} (c \cdot f_{\kappa}(x_0, \delta) + f_{\text{dist}}(\delta) + L_{AE} + L_{\text{proto}})$$

*Limit: No model agnostic (only neuronal networks models)*

*First benefit: Only one model to train*



# Our contribution

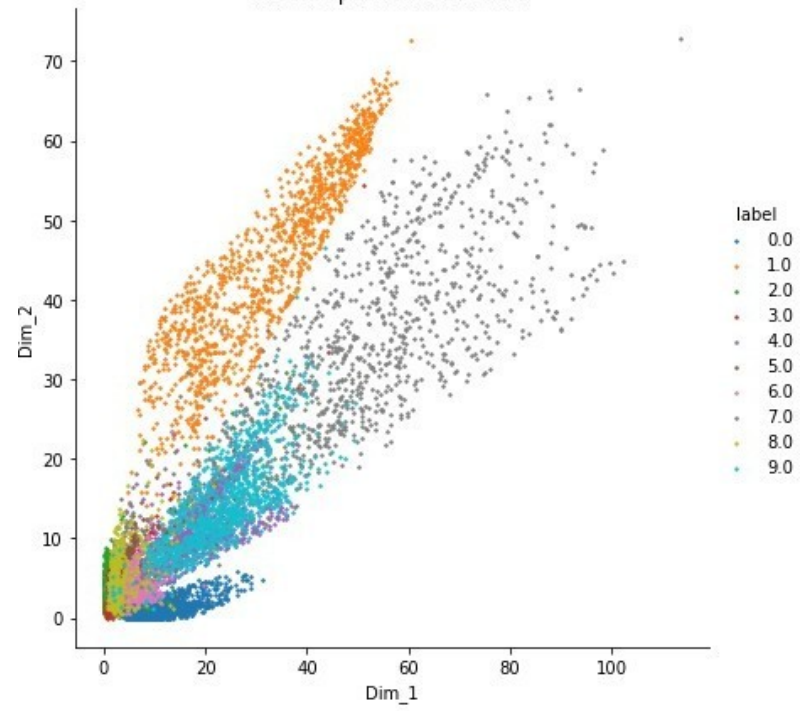
Intuition behind the use of a supervised autoencoder:

Design an **organized latent** space according to **classes**.

**Prototypes** will be **more representative of a given class** /  
Hence more representative counterfactuals

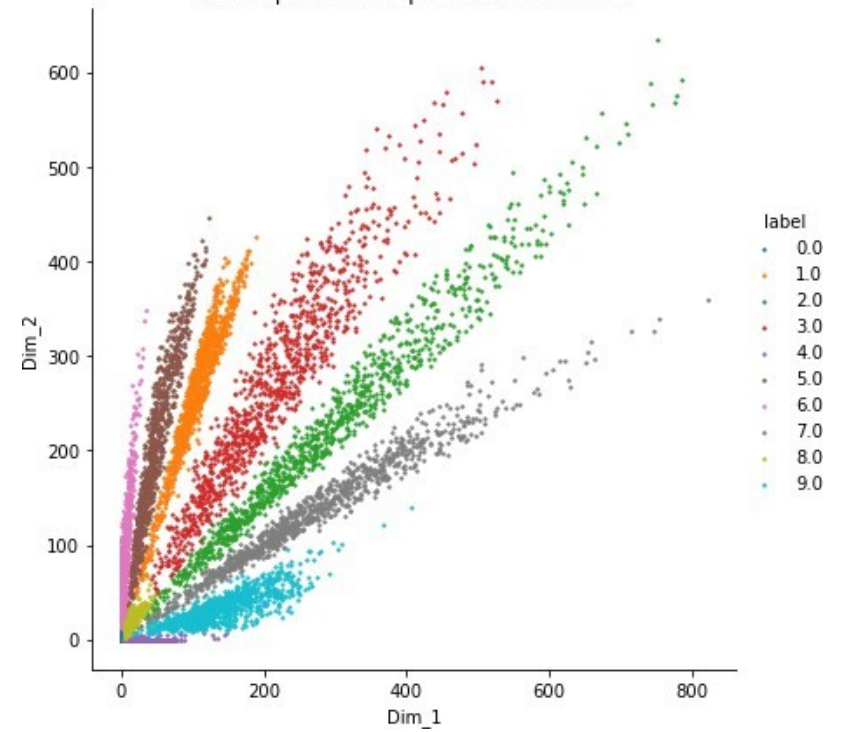
# Visualization of a 2 dimensional latent space on MNIST

Latent space with baseline



Examples of the same predicted class are «mixed» in the latent space

Latent space with supervised autoencoder



Examples of the same predicted class are clustered in the latent space

# Experimental setting

- MNIST Dataset
- Random sample of 5000 examples.
- Same hyperparameters as *Van Looveren et al.* for counterfactual generation.

# Evaluation Metrics

Predicted probability for counterfactual  
(according to counterfactual class)

$$\text{Gain} = [f_{\text{pred}}(x_{cf})]_{y_i} - [f_{\text{pred}}(x_0)]_{y_i}$$

Predicted probability for example  
(according to counterfactual class)

$$\text{Realism} = \|\mathbb{A}E_{\text{evaluate}}(x_{cf}) - x_{cf}\|_2^2$$

$$\text{Actionability} = \|x_{cf} - x_0\|_1 = \|\delta\|_1$$

$y_i$  : Counterfactual predicted class       $\delta$  : Perturbation

$x_{cf}$  : Counterfactual example

*Daniel Nemirovsky et al, CounteRGAN: Generating Realistic Counterfactuals with Residual Generative Adversarial Nets, 2020, arXiv.*

# Results

**Table 1.** Counterfactual metrics comparison. The arrows indicate whether larger  $\uparrow$  or lower  $\downarrow$  values are better, and the best results are in bold.

Metrics	Baseline	Supervised autoencoder
$\uparrow$ Prediction gain	0.552 $\pm$ 0.106	<b>0.839<math>\pm</math>0.160</b>
$\downarrow$ Realism	0.253 $\pm$ 0.010	<b>0.249<math>\pm</math>0.012</b>
$\downarrow$ Actionability	<b>26.174<math>\pm</math>13.762</b>	38.360 $\pm$ 18.465

Higher gain = **more confidence** in the class change of the counterfactual example.

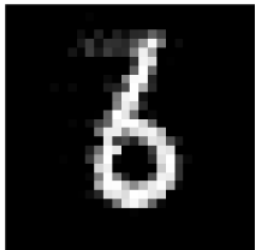
Higher actionability / Equivalent realism

# Results Illustration

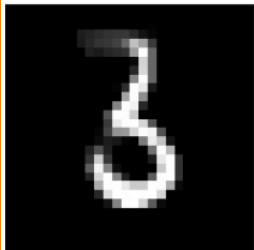
Example,3



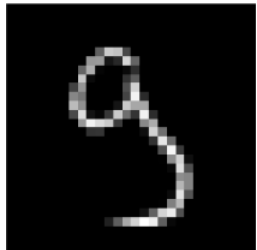
Supervised-autoencoder,6



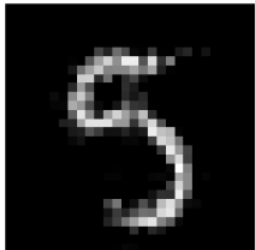
Baseline,6



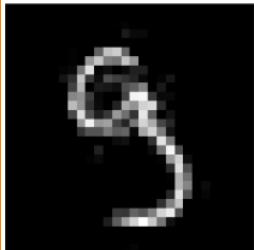
Example,9



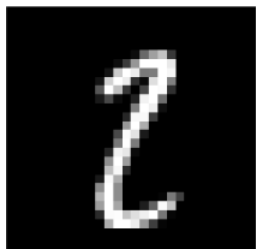
Supervised-autoencoder,5



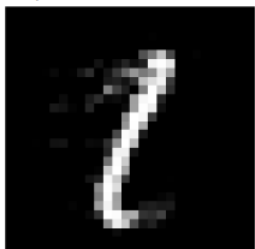
Baseline,5



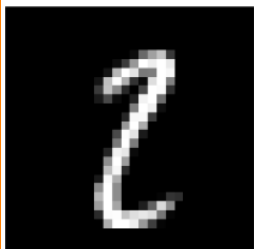
Example,2



Supervised-autoencoder,1



Baseline,8



Examples



Counterfactuals with supervised autoencoder



Counterfactuals with baseline

# Conclusion and future work

## Conclusion:

- 2 steps process (train only one model by using a supervised autoencoder) instead of 3 steps process
- Organize the latent space according to classes (more meaningful prototypes hence counterfactuals)
- Evaluation on MNIST dataset
- Higher prediction gain with less actionability and equivalent realism

## Future work:

- Adapt this method to tabular data

***Scientific issues:*** *Using a latent space still relevant? / How to treat categorical variables? / Take into account loss of visual interpretability?*

**Thank you !**