

FIG. 3

FIG.4a

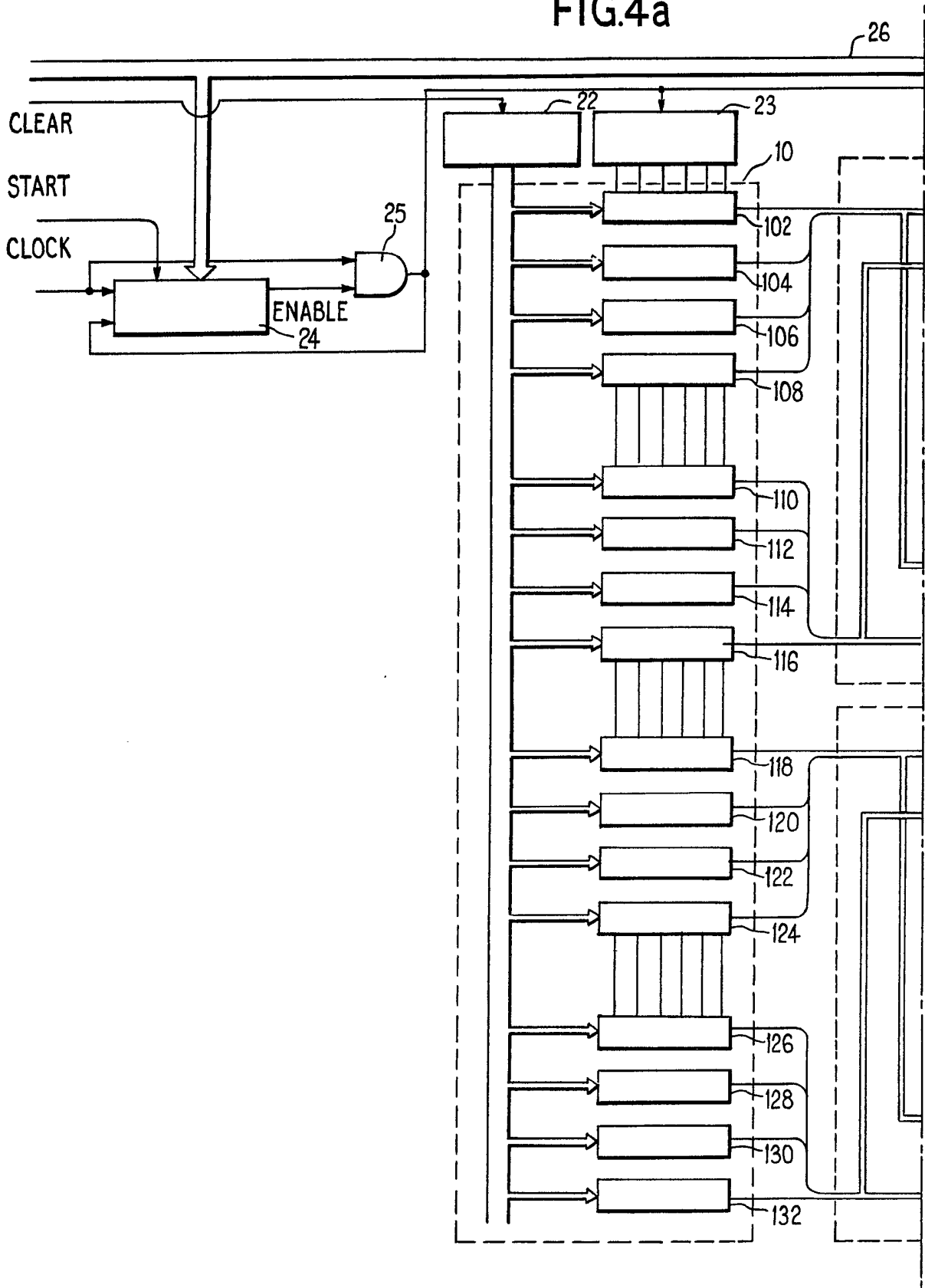
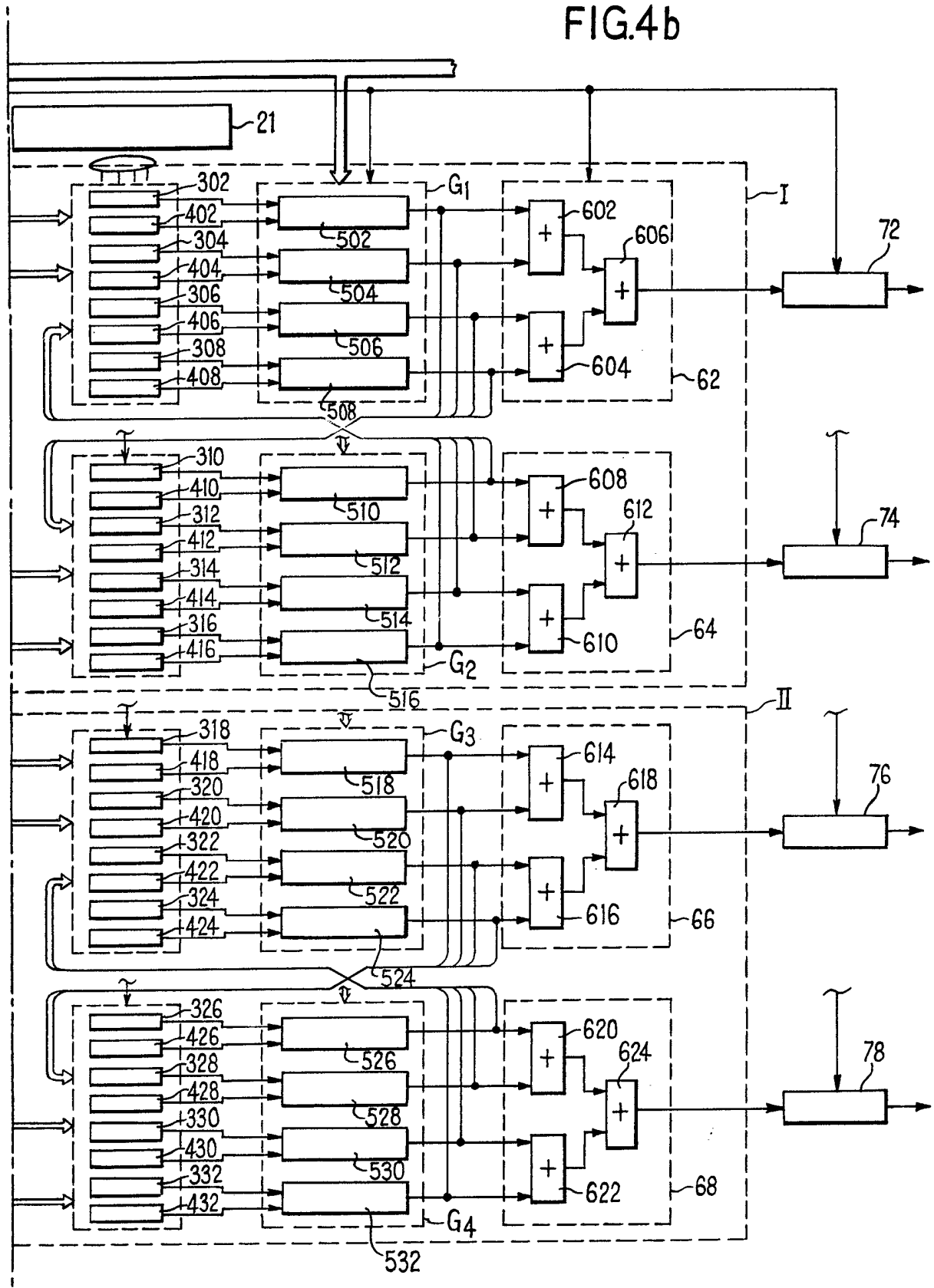


FIG.4b



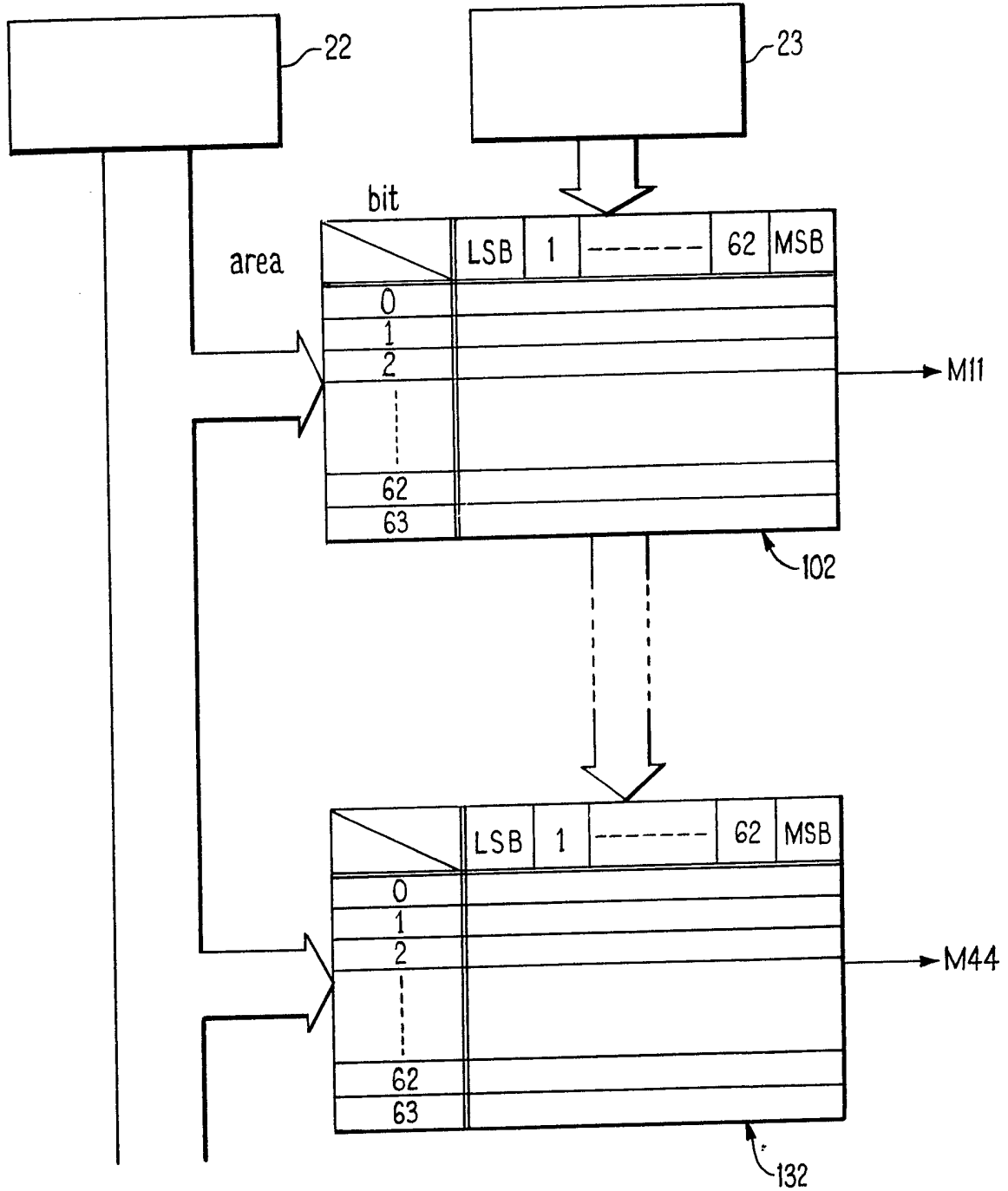


FIG. 5

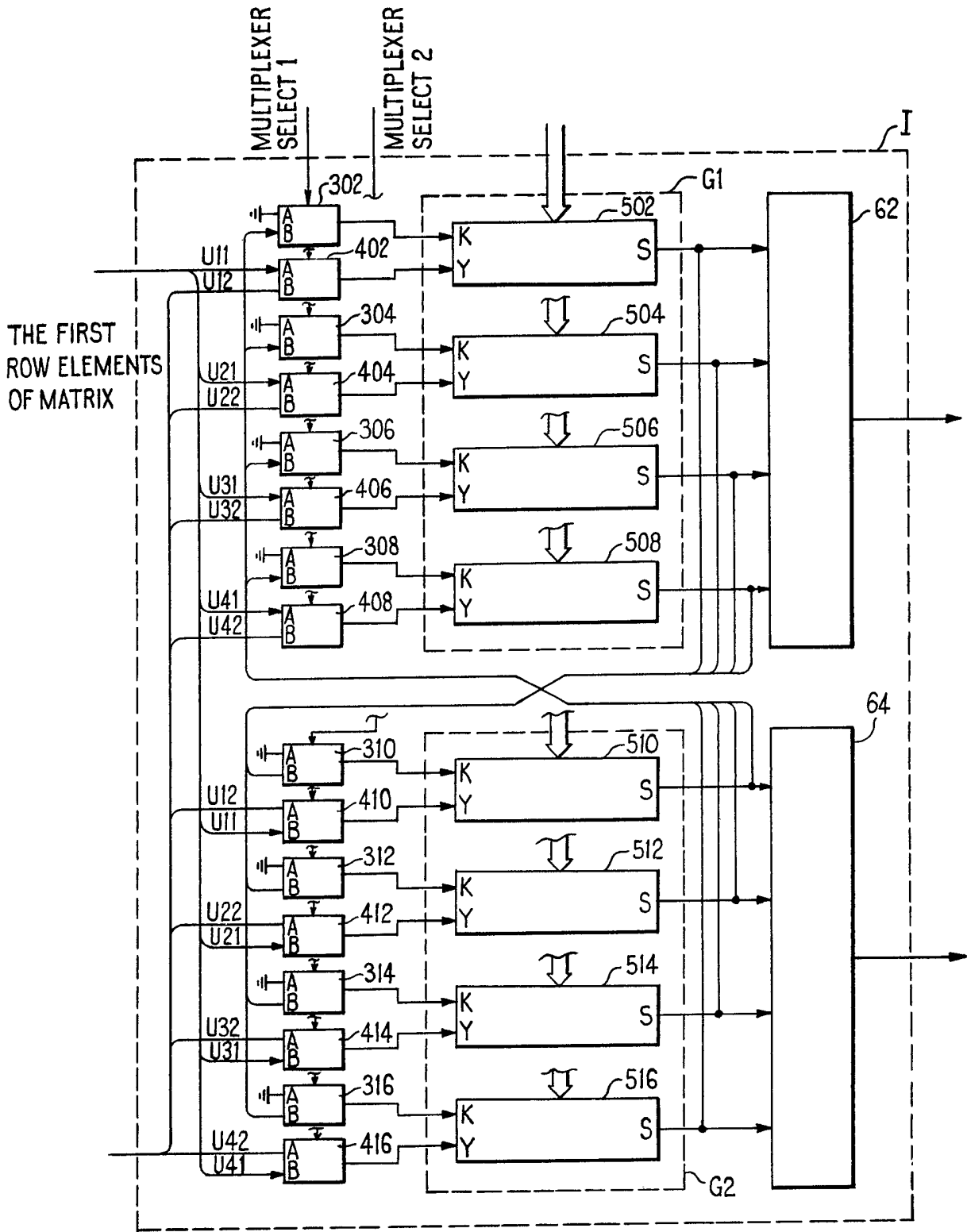


FIG. 6

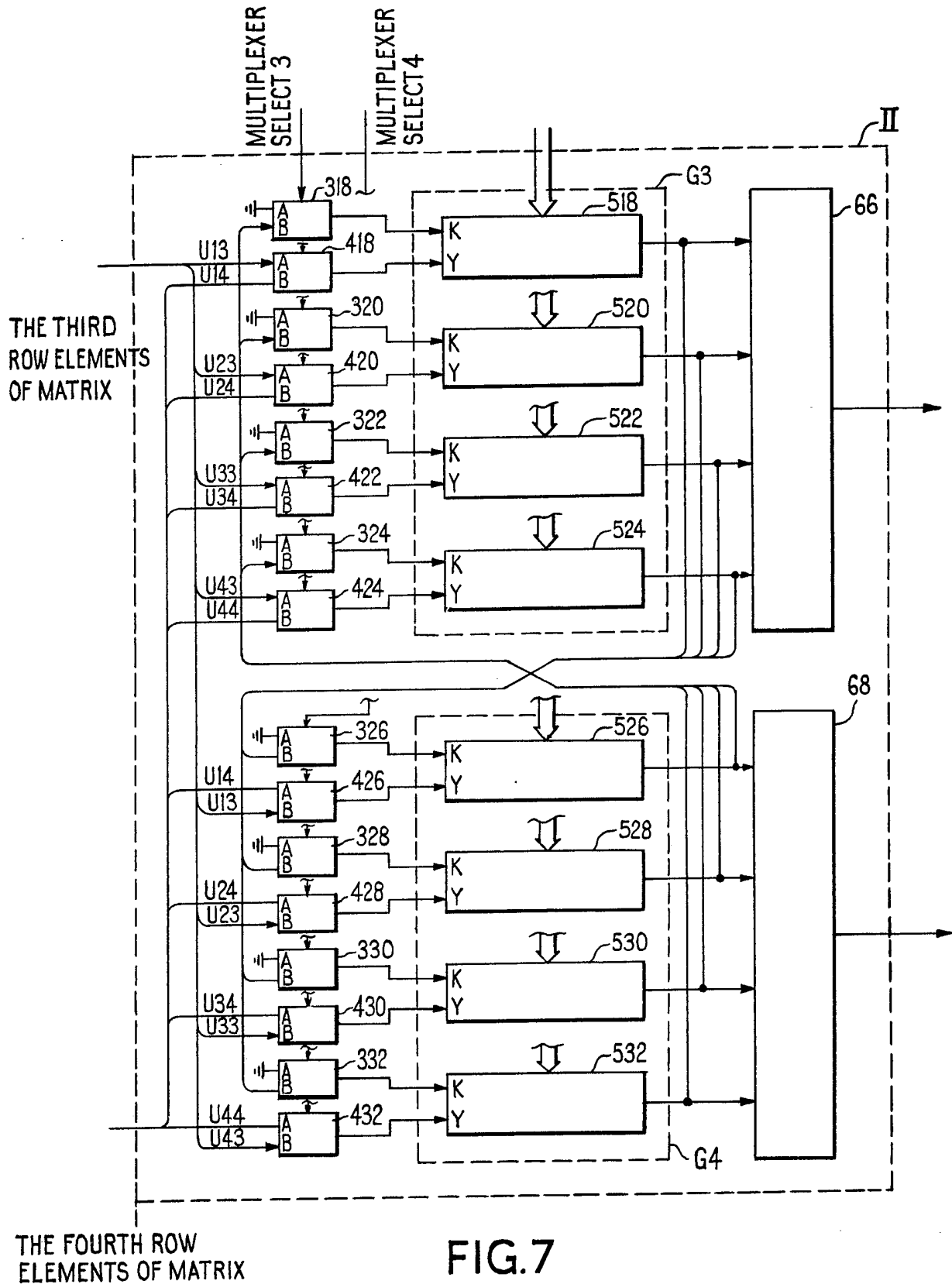


FIG. 7

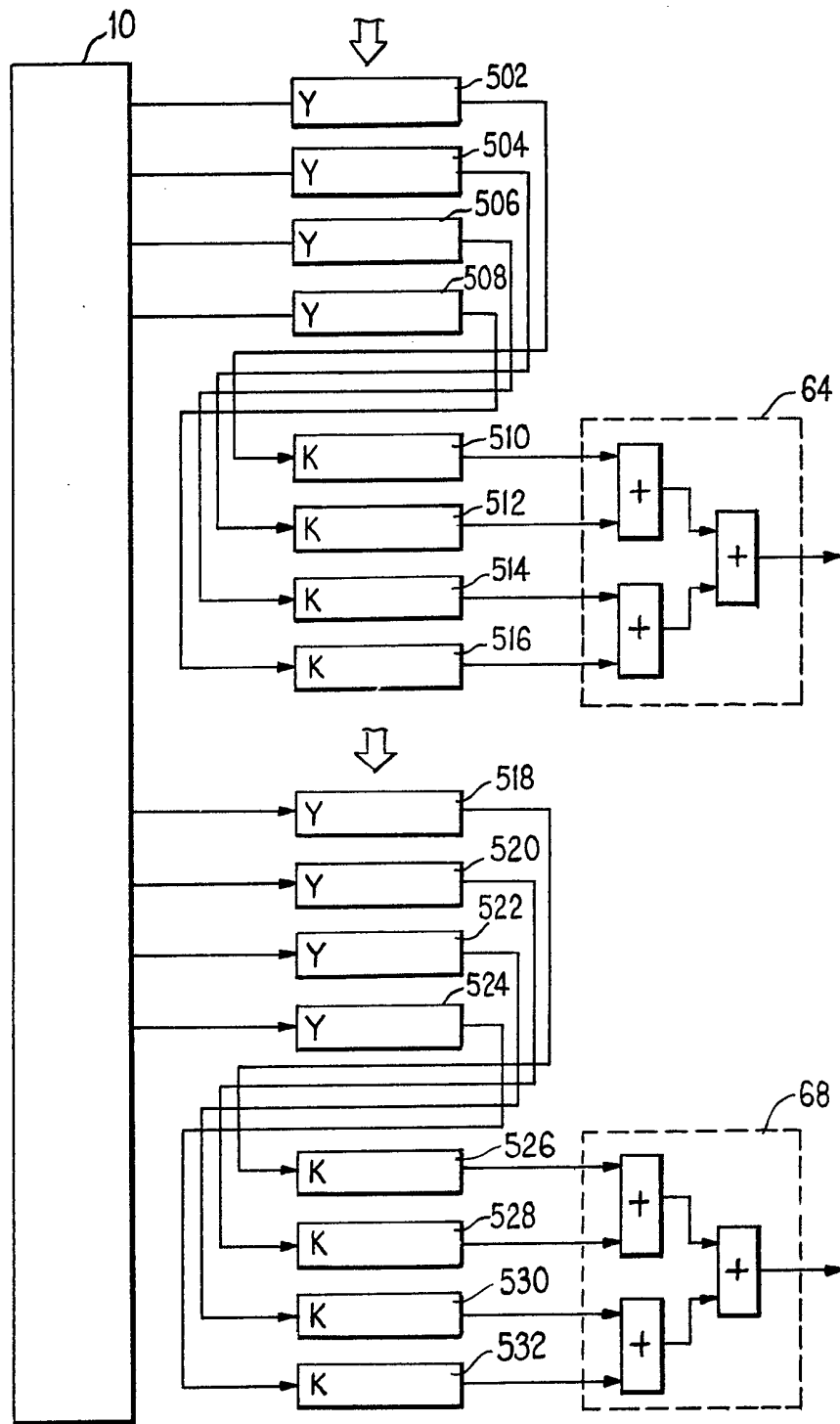


FIG.8

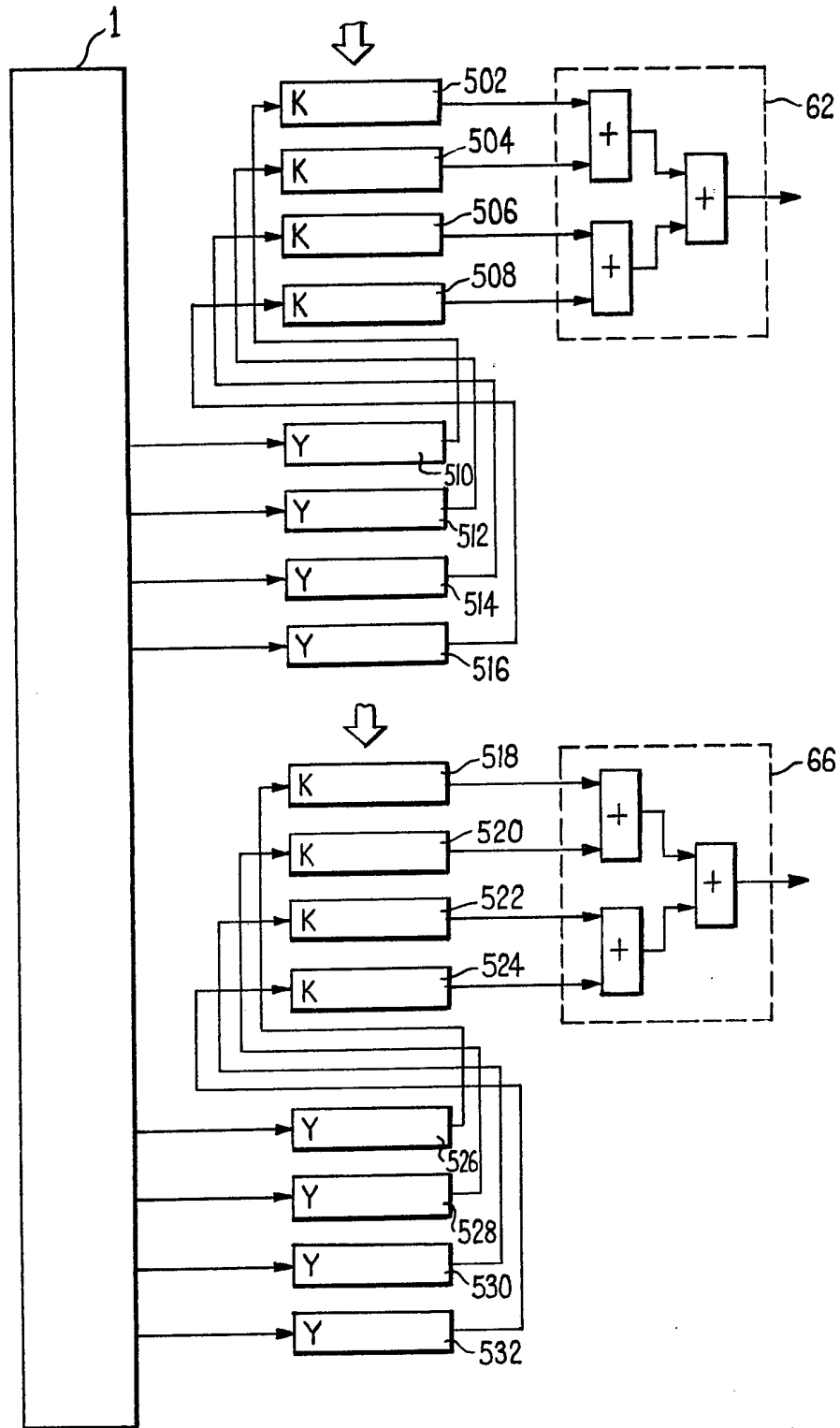


FIG. 9

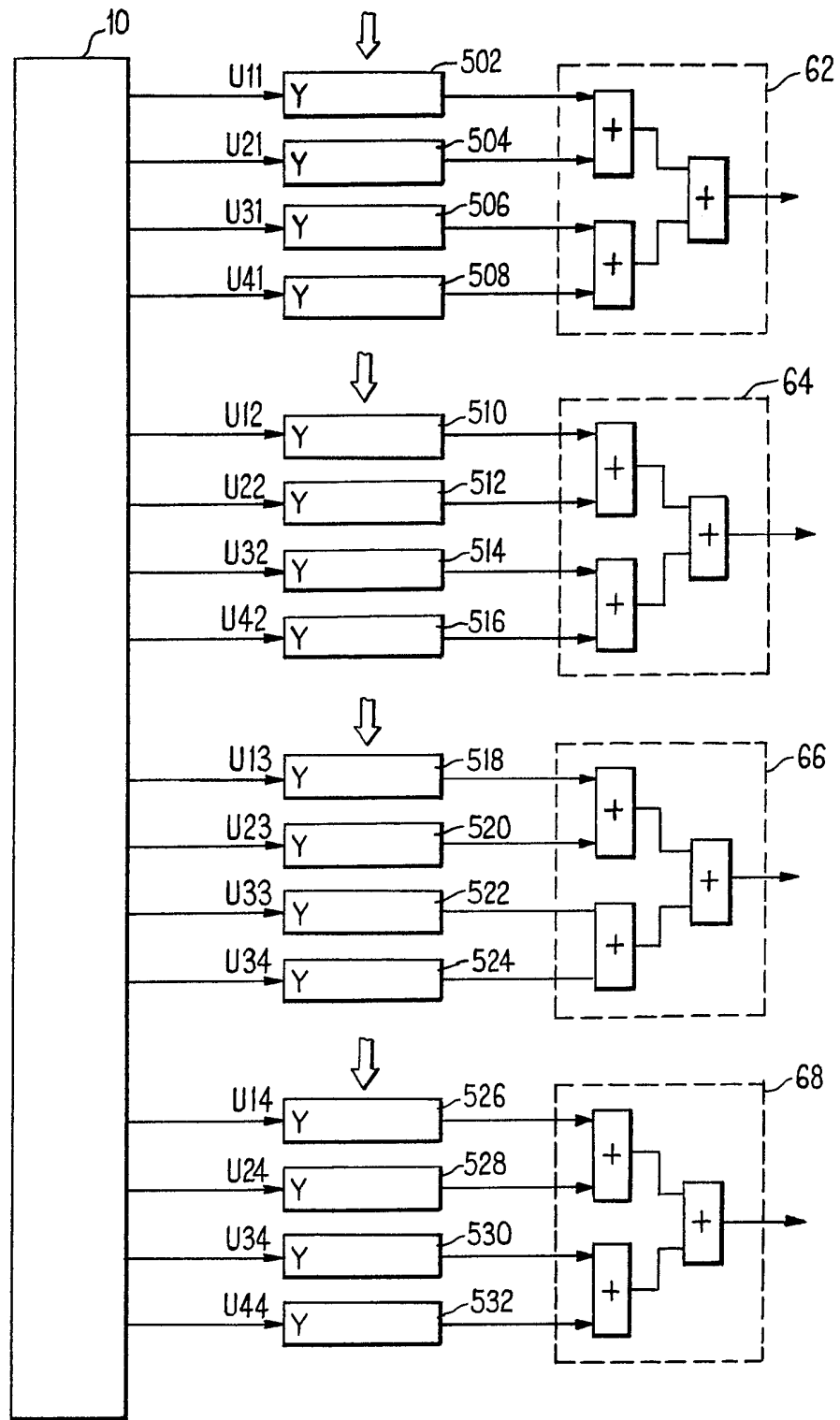


FIG. 10

FIG. 11

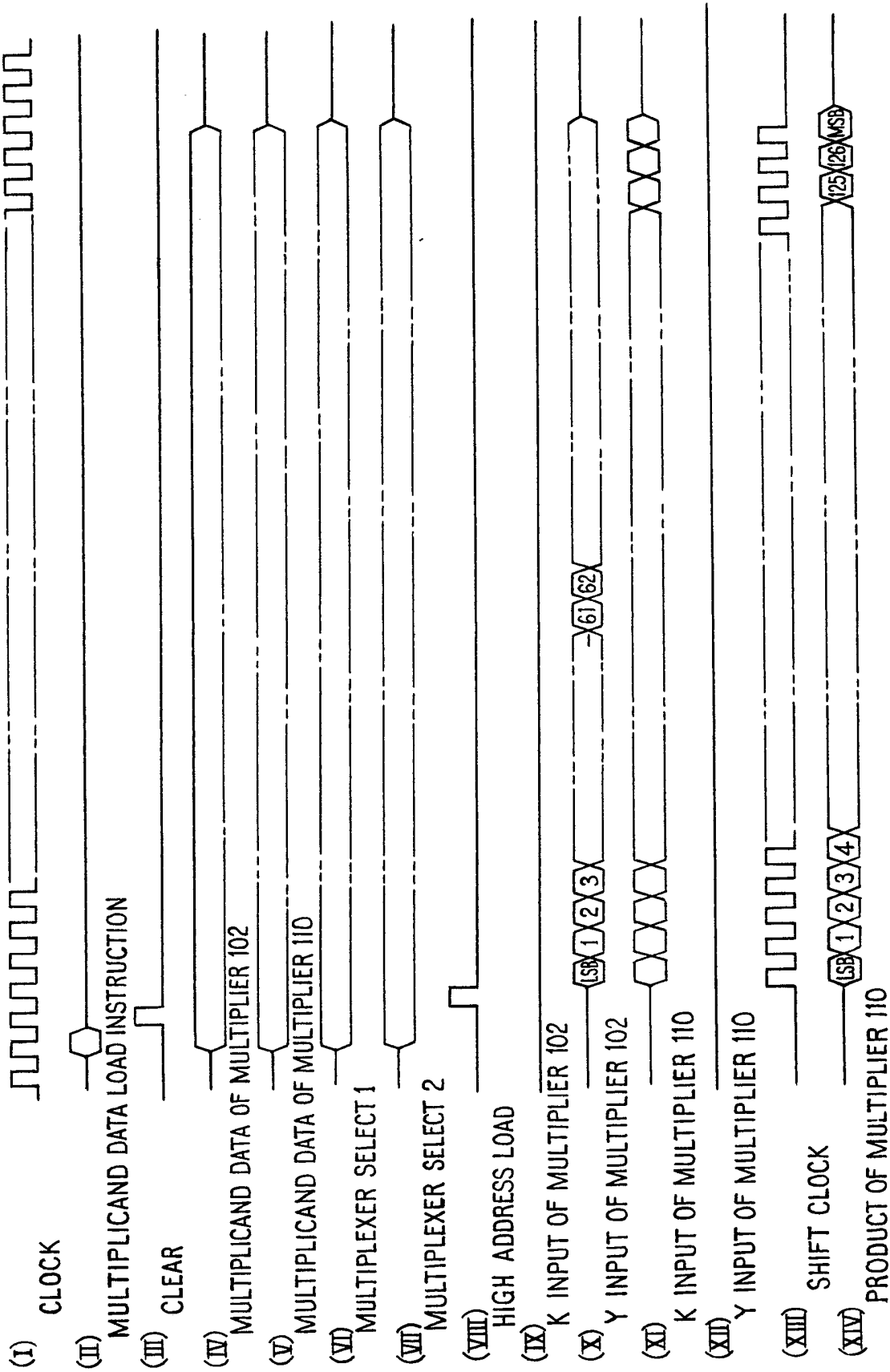
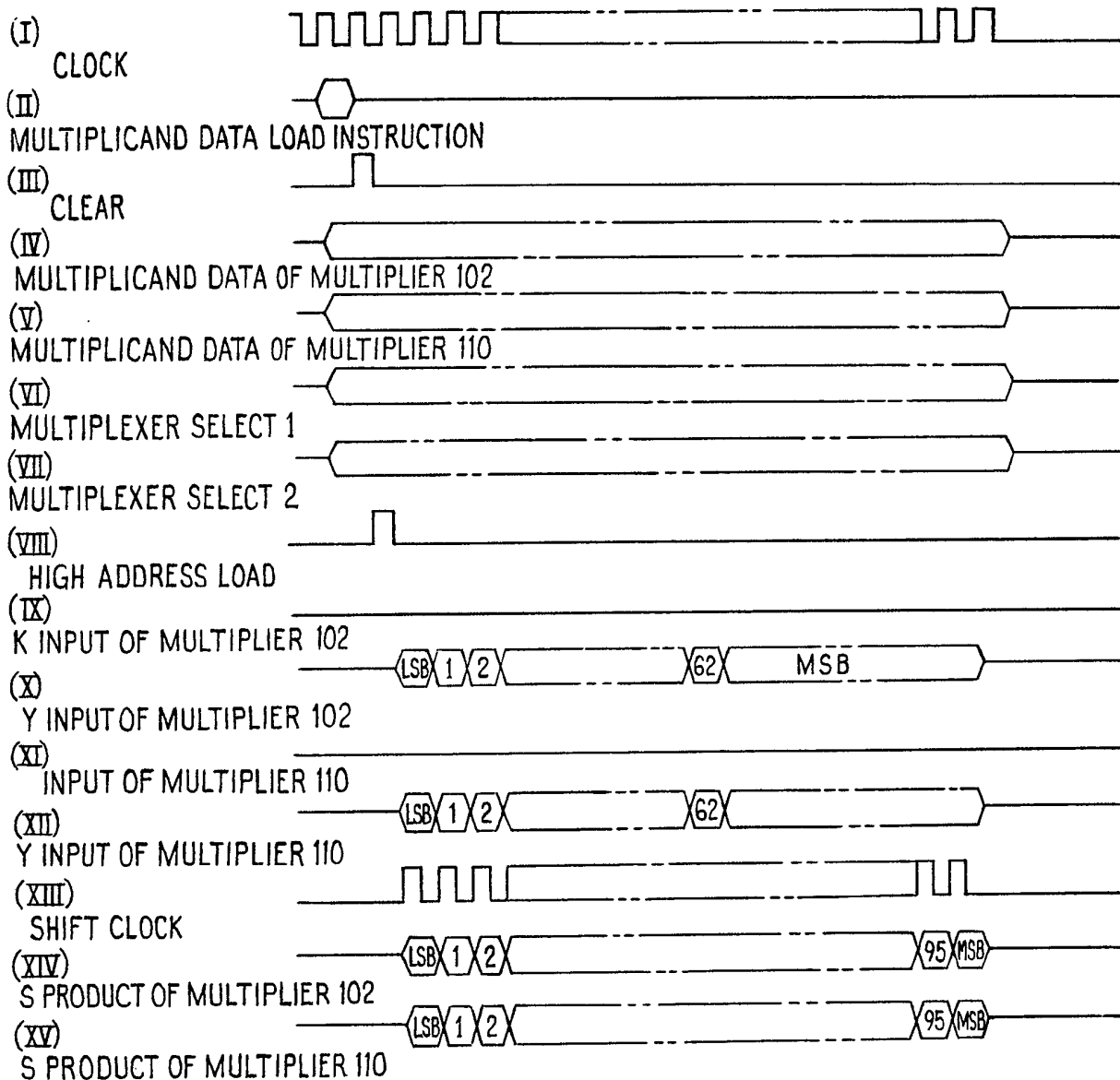


FIG. 12



SPECIFICATION

Matrix multiplication apparatus for graphic display

- 5 This invention relates to matrix multiplication apparatus for graphic displays. 5
- The present invention seeks to provide a matrix multiplication apparatus which can reduce the time taken to read data from a matrices elements memory, can form a serial multiplier in accordance with the data length of a multiplicand, and can multiply a transformation matrix by coordinate data at high speed.
- Although the present invention is primarily directed to any novel integer or step, or combination of 10 integers or steps, herein disclosed and/or as shown in the accompanying drawings, nevertheless, according to one aspect of the present invention to which, however, the invention is in no way restricted, there is provided a matrix multiplication apparatus for graphic display which transforms line segment into a dot pattern and displays the corresponding picture, the apparatus comprising: matrix storing means capable of reading out directly and serially elements of matrices acting as multipliers; and multiplication means 15 capable of changing the number of bits input thereto, in accordance with the data length of a multiplicand, and of multiplying said multiplier from said matrix storing means.
- Preferably said matrix storing means comprises random access memories provided with a number of blocks corresponding to the number of elements of a matrix, in which each block is divided into at least one area, and which has a memory capacity such that one area can store the elements of a matrix, and which has 20 high address terminals for designating said areas and low address terminals for reading out said matrix elements stored in said area in bit units starting from the least significant bit, high address setting means connected to said high address terminals, and low address setting means connected to said low address terminals.
- Preferably said multiplication means comprises one set of multipliers consisting of two groups, each 25 group in turn consisting of a plurality of serial multipliers each of a number of bits greater than the shortest data length of said multiplicand, and each being equipped with a direct-connection terminal and a cascade terminal, first change-over means for connecting two serial multipliers of different groups in a cascade connection to form a pair, or for enabling said serial multipliers of said pair to operate independently of each other, second change-over means for changing over multipliers input from matrix 30 terminals to the direct-connection terminal of each multiplier, and addition means for adding the results of multiplications within said groups and output one matrix element.
- Said first change-over means may have two input terminals and one output terminal, one of said input terminals being grounded with the other connected to the other of said serial multipliers forming said pair, and said output terminal is connected to the cascade terminal of each multiplier.
- 35 Said second change-over means may have two input terminals and one output terminal, one of said input terminals being connected to an odd-numbered row element output terminal of said matrix storing means with the other being connected to an even-numbered row element output terminal thereof, and said output terminal is connected to the direct-connection terminal of each multiplier.
- The invention is illustrated, merely by way of example, in the accompanying drawings, in which:-
- 40 *Figure 1* is a block diagram of a graphic display; 40
Figure 2 is a schematic view explaining the transformation of a figure in a graphic display;
Figure 3 is a timing chart illustrating the operation of a conventional matrix multiplication apparatus using a stack memory as a matrices elements memory;
Figure 4 is a block diagram of one embodiment of a matrix multiplication apparatus according to the 45 present invention for a graphic display; 45
Figure 5 is a diagram of the construction of a memory of the matrix multiplication apparatus of *Figure 4*;
Figures 6 and *7* are block circuit diagrams of details of the matrix multiplication apparatus of *Figure 4*;
Figures 8 and *9* are schematic illustrations of how multiplication circuit groups are connected when conversion matrices are being multiplied together in the matrix multiplication apparatus of *Figure 4*;
- 50 *Figure 10* is a schematic illustration of how the multiplication circuit groups are connected when 50 coordinate data and a transformation matrix are being multiplied together in the matrix multiplication apparatus of *Figure 4*;
Figure 11 is a timing chart illustrating the operation of the matrix multiplication apparatus of *Figure 4* when transformation matrices are being multiplied together; and
- 55 *Figure 12* is a timing chart illustrating the operation of the matrix multiplication apparatus of *Figure 4* when 55 a conversion matrix is being multiplied by coordinate data.
- A graphic display is shown in *Figure 1* and has a matrix multiplication circuit 3 which calculates line segments transferred thereto from a host computer 1 in accordance with the instructions from an input device 2 such as a keyboard, so as to execute enlargement, reduction, rotation, perspective viewing or 60 translating of a figure. A clipping circuit 4 then determines whether or not the figure after the transformation then remains within a window, the line segment is transformed into coordinate values on display screen coordinates by a window viewport transformation, a line generation circuit 5 generates pixels interpolating between line segments, an image memory 6 temporarily stores dot data, and a display is thereafter 65 produced on a cathode ray tube (CRT) 7.
- 65 In order to transform a figure K1 to a figure K2, as shown in *Figure 2*, a rotational movement and a 65

translation movement must be carried out. For this reason, the matrix multiplication circuit 3 executes a multiplication of a rotational transformation matrix R for rotational movement, a translation transformation matrix P for translation, and a coordinate data L, that is, an affine transformation according to the following formula, for each of the line segments V_0, V_1, V_2 of the figure K1:

$$\begin{array}{rcccl}
 5 & & & & 5 \\
 & \text{L.P.R.} = (X_i, Y_i, Z_i, 1) \cdot & P_{11} & P_{12} & P_{13} & P_{14} & R_{11} & R_{12} & R_{13} & R_{14} \\
 & & P_{21} & P_{22} & P_{23} & P_{24} & R_{21} & R_{22} & R_{23} & R_{24} \\
 10 & & P_{31} & P_{32} & P_{33} & P_{34} & R_{31} & R_{32} & R_{33} & R_{34} \\
 & & P_{41} & P_{42} & P_{43} & P_{44} & R_{41} & R_{42} & R_{43} & R_{44} \\
 & & & & & & & & & 10
 \end{array}$$

This calculation is done in the following way. First, a multiplication of the translation transformation matrix P as the multiplicand by the rotational transformation matrix R is performed to obtain a transformation matrix W, and then all the line segments of the figure are multiplied by the transformation matrix W, using the coordinate matrix $(x_i, y_i, z_i, 1)$ as the multiplicand. 15

This matrix multiplication is done conventionally as follows. A transformation matrix U necessary for the calculation is temporarily called in a parallel system to a shift register from a stack memory in which are stored element matrices, by a load instruction (III), Figure 3, and while the data is converted into serial data by shift clocks, it is applied to a multiplier as a multiplier (V) and is then multiplied serially by the multiplicand that is input previously. 20

Although a stack memory is an extremely convenient memory for calculation processing in which the data stored therein must be frequently updated, it has the problem for serial multiplication that the multipliers are first called by a load instruction before the start of the calculation and are applied bit-by-bit to the multiplier by the shift clocks, so that an excessive period of time is needed for the execution of the load instruction, and the calculation time for one multiplication is very long. 25

The coordinate data L usually consists of 32 bits, but the transformation matrices, such as the rotational transformation matrix R or the translation transformation matrix P, have a long data length of 64 bits in order to provide an improved calculation accuracy. 30

Conventionally, the multiplication of transformation matrices with each other and the multiplication of a transformation matrix by coordinate data are carried out using a serial multiplier of a 64-bit construction. When the transformation matrix W is multiplied by the coordinate data, therefore, 32 zeros are added to the high-order bits of the coordinate data so as to make it match the data length of the transformation matrix acting as the multiplier, and the multiplication is effected between data each of 64 bits. 35

Accordingly, $64 + 64 = 128$ shift clocks are required for a single calculation, although the multiplication is actually done between data of an effective length of 32 bits and data of an effective length of 64 bits and the total length of data actually handled is only 96 bits. In other words, as many as 32 bits of excess clocks are necessary, and time is wasted during the period of the calculation with the transformation matrix W and the coordinate data that occupies the major proportion of the calculation time in a graphic display. 40

Referring now to Figure 4 there is shown one embodiment of a matrix multiplication apparatus according to the present invention having a matrices elements memory 10 which is constructed of random access memories (hereinafter referred to "RAMs") 102 - 132 forming 16 blocks and storing matrix elements U11 - U44. Each RAM is divided into 64 areas each consisting of 64 bits, as shown in Figure 5, and the n th area of each RAM stores a corresponding matrix element (U_{ij}) of one transformation matrix, so that 64 different matrices can be read therefrom. 45

The output terminals of the RAMs 102 - 132 of the matrices elements memory 10 are connected to multiplier input terminals of serial multipliers 502 - 532 by second multiplexers 402 - 432 that are controlled by a multiplexer control circuit 21. The address terminals of each RAM are divided into high address terminals A11 ... A6 for selecting the n th area and low address terminals A5 ... A0 for reading out the element data $(U_{ij})_n$ stored in that area. The high address terminals A11 ... A6 of each RAM are connected in common to the output terminal of a high address counter 22, while the low address terminals A5 ... A0 are connected in common to a low address counter 23, so that the n th area can be specified by a high address and thereafter the low addresses are sequentially designated from the least significant address so that the matrix can be read out in bit units. 50

A shift counter 24 is connected to a clock signal source, and AND gate 25 and a data bus 26, and is constituted so that when shift number signals are input thereto from the data bus after the reception of a start signal, it outputs an enable signal until a predetermined number of clock signals have been inputted to the low address counter 23. The AND gate 25 continues to output the shift clocks to the low address counter 23, the serial multipliers 502 - 532 and addition circuits 62 - 68 only during the period in which the shift counter 24 outputs the enable signal. 55

Multiplication is effected by two multiplication circuit groups I and II, each multiplication circuit group being further divided into two groups G1 and G2, G3 and G4 respectively. The multiplication circuit groups also contain first multiplexers 302 - 332 that are controlled by signals from the multiplexer control circuit 21, the serial multipliers 502 - 532 that can be connected in cascade connections by corresponding first 60

65

multiplexers or can be used independently of one another, the addition circuits 62 - 68 that add outputs from these multipliers, and the second multiplexers 402 - 432.

As shown in Figures 6 and 7, the multiplication circuit groups I and II have serial multipliers 502 - 516, 518 - 532, respectively, that can multiply 32-bit data in a serial form. Each multiplier has a cascade terminal K, a direct-connection terminal Y, and a serial output terminal S. The cascade terminals K are connected to the corresponding first multiplexers 302 - 332 which each have two input terminals A and B, a selection signal input terminal and an output terminal. The direct-connection terminals Y are connected to the corresponding second multiplexers 402 - 432 which each have two input terminals, a selection signal input terminal and an output terminal.

One of the input terminals A of each of the first multiplexers 302 - 332 is grounded and the other input terminal B is connected to the output terminal of a multiplier of the other group so as to form pairs of multipliers 502 and 510, 504 and 512, 506 and 514, 508 and 516, 518 and 526, 520 and 528, 522 and 530, and 524 and 532. Thus, the multipliers can be selectively connected so that when they are placed in this cascade connection, they can handle 64-bit multiplicands. In the first multiplication circuit group I, the input terminal A of each of the second multiplexers 402 - 432 is connected to an output terminal of the first row of the matrices elements memory 10, and its input terminal B is connected to an output terminal of the second row thereof, so that each element U11 ... U41 and U12 ... U42 of the first and second rows of the matrices elements memory 10 can be input thereto. In the second multiplication circuit group II, the input terminals A are connected to an output terminal of the third row of the matrices elements memory 10, and the input terminals B are connected to an output terminal of the fourth row, so that each element of the third and fourth rows U13 ... U43 and U14 ... U44 can be input thereto. According to this arrangement, matrix elements of either row can be selected for each multiplication circuit for the multiplication of transformation matrices (Figures 8 and 9), and the transformation matrix elements corresponding to each multiplier can be selectively output for the multiplication of coordinate data by a transformation matrix (Figure 10).

The addition circuits 62 - 68 each consist of two adders 602 and 604, 608 and 610, 614 and 616, 620 and 622, respectively, that are connected to two of these multipliers to obtain a sum of the outputs thereof, and third adders 606, 612, 618, 624 which obtain a sum of the outputs of these pairs of adders. The addition circuit 62 - 68 each output one of the elements of the matrix obtained by the calculation to corresponding buffer registers 72 - 78 connected thereto.

The operation of the matrix multiplication apparatus of Figure 4 will now be described with reference to the timing charts of Figures 11 and 12.

This example of the operation concerns the case in which line segments input from a host computer, such as the triangular figure K1 of Figure 2, is transformed and moved to figure K2 by instructions from the keyboard.

In this example, a multiplication of the translation transformation matrix P by the rotational transformation matrix R must be done first, as described above, to obtain the transformation matrix W.

First of all, the multiplexer control circuit 21 selects terminals A of the first multiplexers 302 - 308 of the first group G1 of the multiplication circuit group I, and terminals B of the first and second multiplexers 310 - 316 and 410 - 416 of the second group G2 thereof. Similarly, it selects terminals A of the first and second multiplexers 318 - 324 and 418 - 424 of the first group G3 of the second multiplication circuit group II and terminals B of the first and second multiplexers 326 - 332 and 426 - 432 of the second group G4 thereof. As a result, the multipliers of each group are connected to the corresponding multipliers of the other group in a cascade arrangement, that is, the multiplier 502 is connected to the multiplier 510, the multiplier 504 is connected to the multiplier 512, the multiplier 506 is connected to the multiplier 514 and the multiplier 508 is connected to the multiplier 516 in the multiplication circuit group I and the multiplier 518 is connected to the multiplier 526, the multiplier 520 is connected to the multiplier 528, the multiplier 522 is connected to the multiplier 530 and the multiplier 524 is connected to the multiplier 532 in the multiplication circuit group II, thereby forming multipliers of a 64-bit construction. Thus, 64-bit data can be input as a multiplicand.

After this preparation is completed, the translation transformation matrix acting as the multiplicand is input to the multiplication circuit groups I and II from the data bus 26. Accordingly, as shown in Figure 8, the pairs of multipliers in the multiplication group I receive the elements of the first column of the translation transformation matrix P, that is, the multipliers 502 and 510 receive element P_{11} of column 1, row 1, the multipliers 504 and 512 receive element P_{12} of the column 1, row 2, the multipliers 506 and 514 receive element P_{13} of column 1, row 3, and the multipliers 508 and 516 receive element P_{14} of column 1, row 4. The pairs of multipliers in the multiplication circuit group II similarly receive the elements of the first column of the translation transformation matrix P, that is, the multipliers 518 and 526 receive element P_{11} of column 1, row 1, the multipliers 520 and 528 receive element P_{12} of column 1, row 2, the multipliers 522 and 530 receive element P_{13} of column 1, row 3 and the multipliers 524 and 532 receive element P_{14} of column 1, row 4. After the input of the multiplicand is thus completed, the area n of the matrices elements memory 10 which holds therein the rotational transformation matrix R necessary for moving figure K1 to figure K2 is selected. The high address corresponding to this area is set in the high address counter 22, and at the same time the shift counter 24 outputs shift clocks to the low address counter 25 to read out sequentially the data $(U_{ij})_n$ in the area n designated by the high address counter 22, at the timing of the shift clocks, starting from the least significant bit LSB.

Accordingly, the multipliers in the first group G1 of the multiplication circuit group I receive the elements of the first column in synchronism with the shift clocks and start the multiplication, that is, the multiplier 502 receives and starts a multiplication with element R_{11} of column 1, row 1, the multiplier 504 does the same with element R_{21} of the column 2, row 1, the multiplier 506 does the same with element R_{31} of column 3, row 1 and the multiplier 508 does the same with element R_{41} of column 4, row 1. The multiplier 510 outputs $R_{11} \times P_{11}$, the multiplier 512 outputs $R_{12} \times P_{21}$, the multiplier 514 outputs $R_{13} \times P_{31}$ and the multiplier 516 outputs $R_{14} \times P_{41}$. The results of these calculations are added by the addition circuit 64 to provide the element $R_{11} \cdot P_{11} + R_{12} \cdot P_{21} + R_{13} \cdot P_{31} + R_{14} \cdot P_{41}$. At the same time, the multiplication circuit group II receives the elements of the third column, that is, the multiplier 518 receives R_{13} , the multiplier 520 receives R_{23} , the multiplier 522 receives R_{33} , and the multiplier 524 receives R_{43} , starting from the least significant bit, and the results of the calculations therewith are output from the multipliers 526 - 532. These results are added by the addition circuit 68 to provide the element of column 1, row 3, i.e. $R_{11} \cdot P_{13} + R_{12} \cdot P_{23} + R_{13} \cdot P_{33} + R_{14} \cdot P_{43}$. The elements W_{11} and W_{13} thus calculated are input to shift registers 74,78 connected to the corresponding addition circuits 64,68 and after they are digitally processed, they are ordered in a predetermined bit length, e.g. 64 bits, and are stored in an empty area of the matrices elements memory 10. In the same way, similar calculations are carried out four times with different column elements of the translating transformation matrix acting as the multiplicands, to obtain the transformation matrix elements W_{21} , W_{23} , W_{31} , W_{33} , W_{41} , and W_{43} .

When the calculation of this transformation matrix is completed, the multiplexer control circuit 21 changes over the second multiplexers 402 - 432 and the multiplication circuit group I repeats this calculation process four times using the second row of the rotational transformation matrix R as the multiplier and replacing the column elements of the translation transformation matrix. Similarly, the multiplication circuit group II repeats the calculation process four times using the elements of the fourth line of the rotational transformation matrix as the multiplier. Thus, the elements W_{12} , W_{14} , W_{22} , W_{24} , W_{32} , W_{34} , W_{42} , and W_{44} of the transformation matrix W are calculated.

When all the transformation matrix W is stored in the matrices elements memory 10, the multiplexer control circuit 21 selects all the terminals A of the first and second multiplexers 302 - 332 and 402 - 432 and grounds the cascade terminals K of the multipliers to form independent 32-bit multipliers, as shown in Figure 10. The serial input terminal Y of each multiplier is connected to the output terminal of the matrices elements memory 10 so that the multipliers 502 - 508 of the first group of the multiplication circuit group I can be connected to elements $W_{11} - W_{14}$ of the first column of the transformation matrix W, the multipliers of the second group to elements $W_{21} - W_{24}$ of the second column, and the multipliers of groups G3 and G4 of the multiplication circuit group II to elements $W_{31} - W_{34}$ and $W_{41} - W_{44}$ of the third and fourth columns, respectively, as shown in Figure 10.

After this preparation is completed, the x-coordinate data is input to first multipliers 502, 510, 518, 526 in each group, the y-coordinate data to second multipliers 504, 512, 520, 528, the z-coordinate data to third multipliers 506, 514, 522, 530, and 1 to fourth multipliers 508, 516, 524, 532. Under this state, the high address of the area holding the transformation matrix W determined in the procedure described above is set in the high address counter 22, and the shift clocks are input to the low address counter 23, so that the multipliers 502 - 532 receive the elements of the transformation matrix W, that is, the multiplier 502 receives the element of column 1, row 1 of the transformation matrix, the multiplier 504 receives the element of column 2, row 1, ..., and the multiplier 532 receives the element of column 4, row 4, starting from the least significant bit, and they execute the multiplication in a serial system. After 96 clocks corresponding to the bit length have thus been applied to the multipliers the addition circuit 62 outputs the coordinate data x, the addition circuit 64 outputs the coordinate data y, the addition circuit 66 outputs the coordinate data z, and the addition circuit 68 outputs 1, thereby completing the calculation of the data $(x_m', y_m', z_m', 1)$ for one coordinates point V_m . In this manner, the coordinate data for each point V_0, V_1, \dots are sequentially input as multiplicands to the multipliers 502 - 532 in order to execute the multiplication by the transformation matrix W. When a number of shift clocks corresponding to the data length have been input, the result of the multiplication is output, making it possible to perform an affine transformation without wasting any time in the calculation process.

CLAIMS

1. A matrix multiplication apparatus for graphic display which transforms line segment into a dot pattern and displays the corresponding picture, the apparatus comprising: matrix storing means capable of reading out directly and serially elements of matrices acting as multipliers; and multiplication means capable of changing the number of bits input thereto, in accordance with the data length of a multiplicand, and of multiplying said multiplicand by said multiplier from said matrix storing means.
2. A matrix multiplication apparatus as claimed in claim 1 in which said matrix storing means comprises random access memories provided with a number of blocks corresponding to the number of elements of a matrix, in which each block is divided into at least one area, and which has a memory capacity such that one area can store the elements of a matrix, and which has high address terminals for designating said areas and low address terminals for reading out said matrix elements stored in said area in bit units starting from the least significant bit, high address setting means connected to said high address terminals, and low address

setting means connected to said low address terminals.

3. A matrix multiplication apparatus as claimed in claim 1 or 2 in which said multiplication means comprises one set of multipliers consisting of two groups, each group in turn consisting of a plurality of serial multipliers each of a number of bits greater than the shortest data length of said multiplicand, and each being equipped with a direct-connection terminal and a cascade terminal, first change-over means for connecting two serial multipliers of different groups in a cascade connection to form a pair, or for enabling said serial multipliers of said pair to operate independently of each other, second change-over means for changing over multipliers input from matrix terminals to the direct-connection terminal of each multiplier, and addition means for adding the results of multiplications within said groups and output one matrix element.

4. A matrix multiplication apparatus as claimed in claim 3 in which said first change-over means has two input terminals and one output terminal, one of said input terminals being grounded with the other connected to the other of said serial multipliers forming said pair, and said output terminal is connected to the cascade terminal of each multiplier.

5. A matrix multiplication apparatus as claimed in claim 3 or 4 in which said second change-over means has two input terminals and one output terminal, one of said input terminals being connected to an odd-numbered row element output terminal of said matrix storing means with the other being connected to an even-numbered row element output terminal thereof, and said output terminal is connected to the direct-connection terminal of each multiplier.

6. A matrix multiplication apparatus substantially as herein described with reference to and as shown in Figures 4 to 12 of the accompanying drawings.

7. Any novel integer or step, or combination of integers or steps, hereinbefore described, irrespective of whether the present claim is within the scope of, or relates to the same or a different invention from that of, the preceding claims.