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(71) Applicant(s):
**Rolls-Royce plc**
**(Incorporated in the United Kingdom)**
**65 Buckingham Gate, LONDON, SW1E 6AT,**
**United Kingdom**

(72) Inventor(s):
**John Michael Harrison**

(74) Agent and/or Address for Service:
**Rolls-Royce plc**
**PO Box 3, Filton, BRISTOL, BS34 7QE,**
**United Kingdom**

(54) Title of the Invention: **A method for predicting initial unbalance in a component**
Abstract Title: **A method for predicting initial unbalance in a component such as a blisk**

(57) A method for predicting initial unbalance in a component comprising one or more elements, the method comprising: defining a statistical distribution of a mass moment weight of each of the one or more elements; restricting the statistical distribution to a selected range; and calculating an initial unbalance of the component for the restricted distribution of the one or more elements. Where the component is a bladed element, e.g. a blisk, and the elements are blades the predicted initial unbalance is calculated by selecting a plurality of sets of aerofoil elements from the statistical distribution and allocating a location for each aerofoil element on the bladed disk or ring, wherein each set of aerofoil elements forms a sample distribution; and calculating a vector sum of the mass moment weights for each sample distribution to determine the initial unbalance of the blisk. The method is repeated for every permutation of the mass moment weight and/or location of each aerofoil component. A maximum probable unbalance is predicted in order that the size of sacrificial balancing lands of a blisk can be reduced to save weight. The statistical distribution may include a tool wear characteristic.
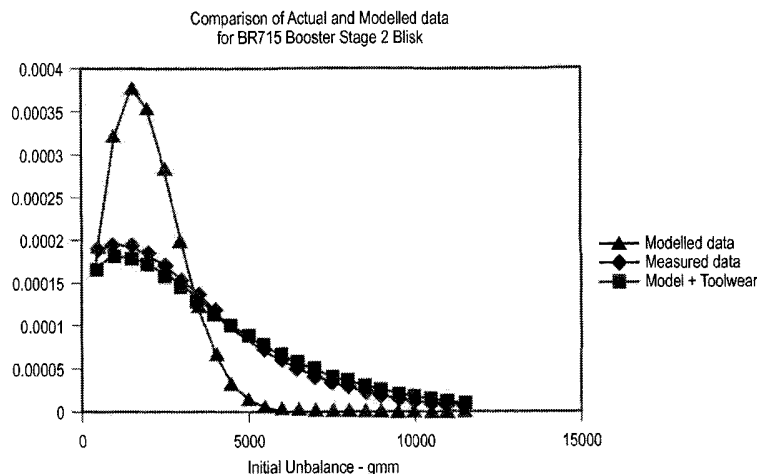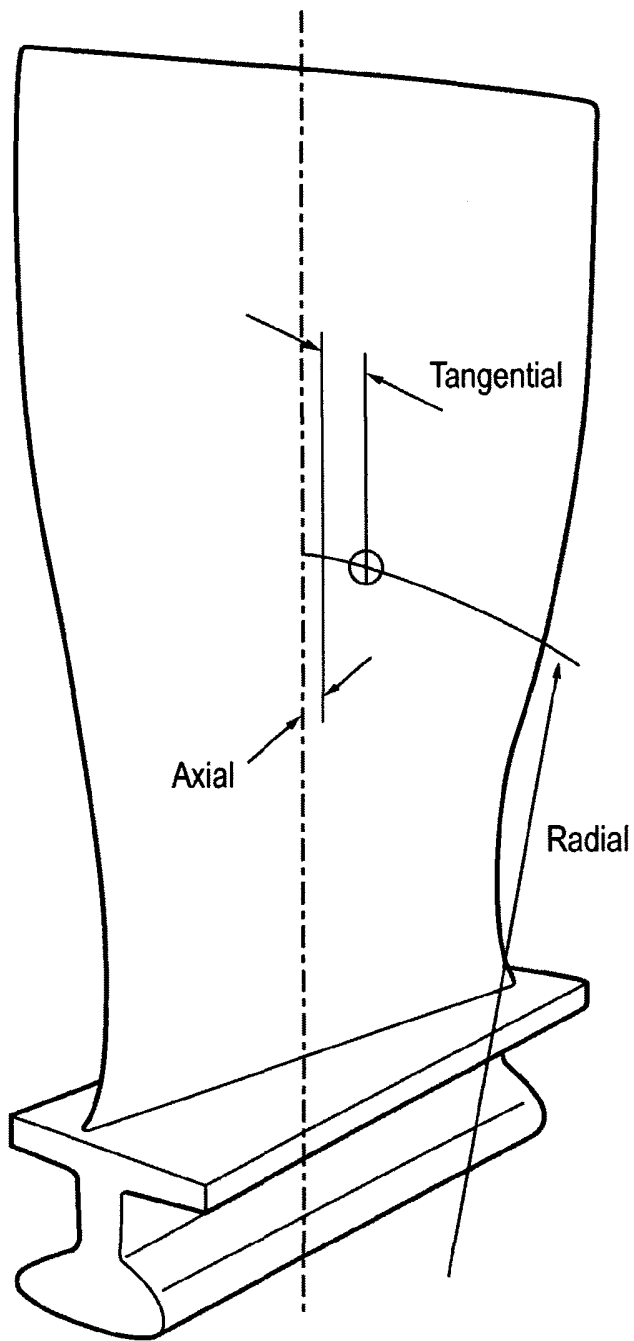
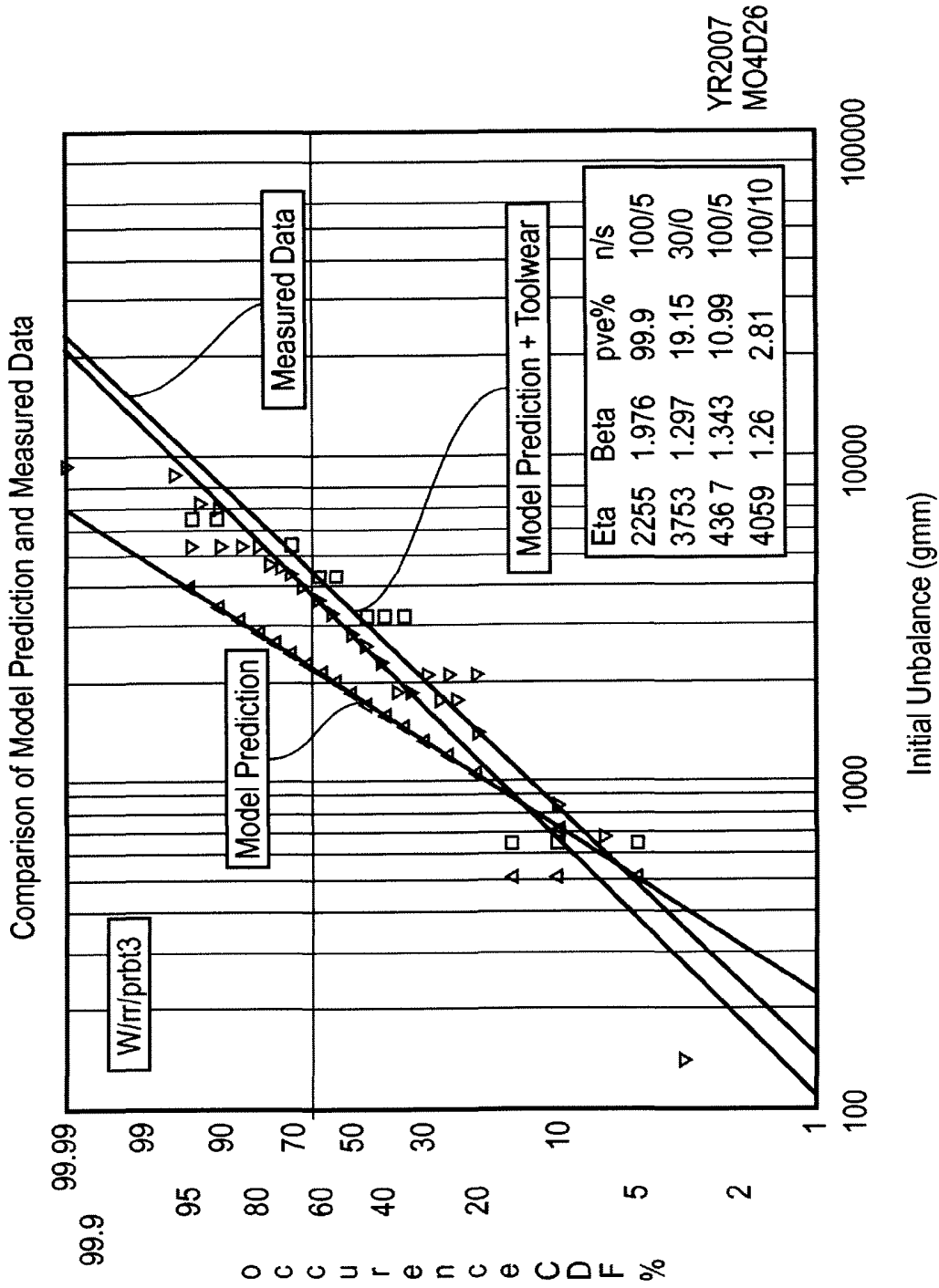Comparison of Actual and Modelled data
for BR715 Booster Stage 2 Blisk

FIG. 3

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15 06 11



FIG. 1

FIG. 2

Comparison of Model Prediction and Measured Data

W/rr/prbt3

Measured Data

Model Prediction + Toolwear

Model Prediction

| Eta | Beta | pve% | n/s |
|---|---|---|---|
| 2255 | 1.976 | 99.9 | 100/5 |
| 3753 | 1.297 | 19.15 | 30/0 |
| 436 7 | 1.343 | 10.99 | 100/5 |
| 4059 | 1.26 | 2.81 | 100/10 |

YR2007
MO4D26

Initial Unbalance (gmm)

Occurrence CDF %

100    1000    10000    100000

99.99
99.9
99
95
90
80
70
60
50
40
30
20
10
5
2
1

15 06 11

Comparison of Actual and Modelled data
for BR715 Booster Stage 2 Blisk

Modelled data
Measured data
Model + Toolwear
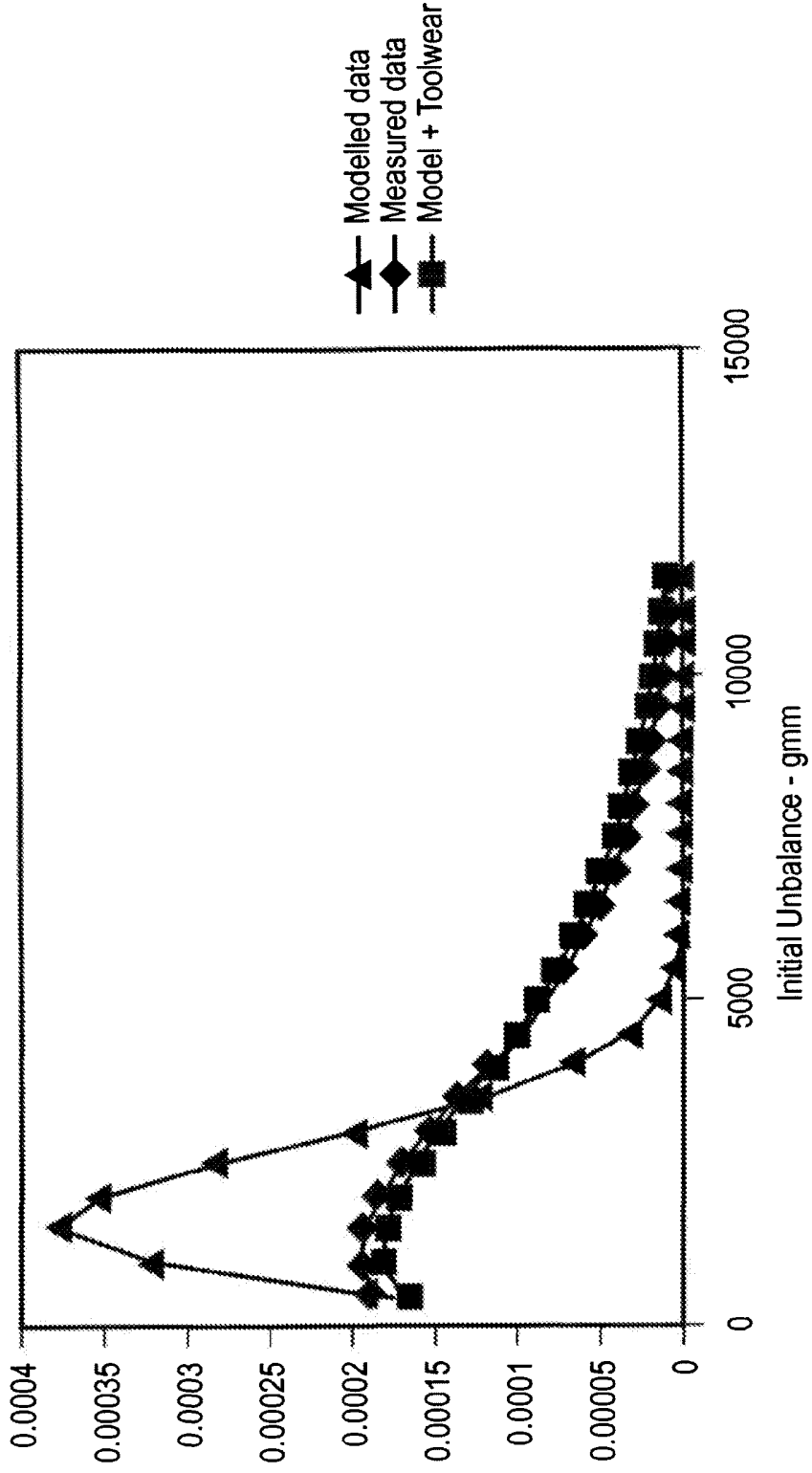
Initial Unbalance - gmm

FIG. 3

# A METHOD FOR PREDICTING INITIAL UNBALANCE IN A COMPONENT

The present invention relates to a method for predicting initial unbalance in a
component and particularly, but not exclusively, to a method which allows the weight of
the component to be reduced.

## Background

Mass unbalance in rotating components such as wheels, crankshafts, gas turbine
engine rotors, etc. can cause undesirable vibration. Such vibration may cause damage
to the component and the surrounding structure. Mass unbalance may be corrected by
redistributing the mass of the component so as to position the centre of mass at the
axis of rotation.

The effects of unbalance become more pronounced at higher rotational speeds.
Consequently, unbalance is a particular issue in the aerospace industry where
components rotate at extremely high speeds. Furthermore, vibration levels in an
aerospace gas turbine engine are not only important from an engine reliability viewpoint
but also from a passenger comfort viewpoint.

An unbalanced component exerts a force on its bearings which is given by:

$$F = Mr\omega^2$$

where M is the mass of the rotating component; r is the radial offset of the mass from its
centre of mass; and $\omega$ is the angular velocity.

For a gas turbine engine, the mass of the rotor is relatively high and the angular velocity is extremely high. Therefore, it can be seen that any radial offset of the mass from its centre of mass (i.e. unbalance) results in a large force being exerted on the bearings. Consequently, it is necessary to minimise the radial offset.

5

Typically a Balance Grade of G2 (ISO 1940-1) may be imposed on gas turbine engines. For a rotor rotating at 10000rpm, this equates to a permissible mass offset of 2μm. This tolerance is some 200 times more stringent than those applied to everyday applications, such as car wheel balancing (Balance Grade G40).

10

Gas turbine engine rotors are conventionally balanced using the weight variation present in a set of aerofoil blades. The blades are detachably mounted to a disc of the rotor via slots provided around the circumference of the disc. The location of the blades around the rotor's disc can be varied to correct not only the disc unbalance but also that

15    of the set of blades, thus producing a balanced rotor. With this method, the blades are weighed, or moment weighed and then distributed around the disc in a pattern to either minimise the unbalance in the blade set, or to compensate for the unbalance in the assembly.

20    In contrast, a blisk comprises a disc with integrally formed blades. This provides a considerable weight saving over the above described rotor by removing the fixtures required to detachably mount the blades to the disc. A reduction in mass of between 20% and 60% can be achieved by using a blisk. The reduction in weight provides an increase in the thrust to weight ratio, which leads to increased fuel economy and

25    associated reduction in running costs, or to an increased payload for the aircraft. As a result, blisks are becoming more prevalent. However, blisks are very complex and time consuming to produce, and consequently, the cost per component is very high. Owing to the complexity of the manufacturing process, there is significant potential for non-conformance in the finished component, and the cost of rejection will again be very

30    high. Furthermore, it is not possible to balance a blisk by interchanging blades and therefore it is necessary to correct the balance of the blisk using alternative methods.

One method of balancing a blisk is to bolt balancing weights onto the blisk to adjust its balance. However, adding weights to balance a blisk is counterproductive since the purpose of a blisk is to save weight. Furthermore, the weights increase the centrifugal loading on the blisk and can only be located in low stress areas. In addition, the

5    connection between the weight and the blisk provides an interface where vibration may occur. This can lead to fretting and erosion. Also, the weights present a potential cause of Domestic Object Damage (DOD) to the engine, if the connection between a weight and the blisk fails.

10   An alternative method uses sacrificial balancing lands which are specifically provided on the component. These balancing lands may be machined to remove some or all of their mass and thus adjust the balance of the component. Such balancing methods require the provision of balancing lands or other features which can be later removed, if required. This results in the component being heavier than would otherwise be

15   necessary.

Conventionally, the required size of the sacrificial balancing lands is calculated based on a worst case scenario for the distribution of the blades. This is where a 180 degree arc of maximum mass blades is located opposite a 180 degree arc of minimum mass

20   blades. Although this ensures that all of the blisks produced can be balanced, the size of the balancing lands is excessive and counteracts the weight saving associated with a blisk.

The present invention seeks to provide a method for predicting initial unbalance in a

25   blisk which provides a value of maximum probable unbalance rather than maximum possible unbalance, as is the case with the prior art method.

## Statements of Invention

In accordance with an aspect of the invention there is provided a method for predicting initial unbalance in a component comprising one or more elements, the method
5 comprising: defining a statistical distribution of a mass moment weight of each of the one or more elements; restricting the statistical distribution to a selected range; and calculating an initial unbalance of the component for the restricted distribution of the one or more elements.

10 The method may further comprise providing the component with a balance correction feature of suitable size to correct a maximum unbalance of the restricted distribution.

The selected range may indicate the probability of obtaining a component which cannot be balanced using the balance correction feature.
15
The component may be a bladed disk or ring and the elements may be a set of aerofoil components. The method may further comprise selecting a plurality of sets of aerofoil components from the statistical distribution and allocating a location for each aerofoil component on the bladed disk or ring, wherein each set of aerofoil components forms a
20 sample distribution; calculating a vector sum of the mass moment weights for each sample distribution to determine the initial unbalance of the blisk.
The method may be repeated for every permutation of the mass moment weight and/or location of each aerofoil component.

25 The statistical distribution may include a tool wear characteristic.

The tool wear characteristic may be based on the manufacturing process of the component.

30 The tool wear characteristic may define an increase in the mass of the aerofoil components around the circumference of the bladed disk or ring.

The statistical distribution may be a normal distribution.

The normal distribution may have a maximum variation of ±8% from an expected value of the mass moment weight.

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The selected range may be ±3 standard deviations from an expected value of the mass moment weight.

The mass moment weight may include one or more of a radial, axial or tangential

10     component.

The initial unbalance may be calculated using a Monte Carlo simulation.

**Brief Description of the Drawings**

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For a better understanding of the present invention, and to show more clearly how it may be carried into effect, reference will now be made, by way of example, to the accompanying drawings, in which:

20     Figure 1 is a perspective view of a blade showing the components of its mass moment;

Figure 2 is a Weibull plot showing the correlation between unbalance values predicted using the invention and measured data; and

25

Figure 3 is a Weibull probability density function plot of the predicted unbalance using the invention and measured data.

## Detailed Description

In an embodiment of the present invention, a prediction of the initial unbalance in a blisk is made using a statistical approach to provide a more realistic reflection of probable

5    unbalance.

Firstly, it is assumed that each blade used to form the blisk has a mass moment weight which is selected from a normal distribution centred on the expected mass of the blades. However, to remove the most extreme situations, i.e. the maximum possible

10    unbalance described previously, the blades are assumed to have a maximum variation of ±8% from the expected mass. The selected distribution equates to ±3 standard deviations ($\sigma$) and thus includes 99.7% of blades.

The normal distribution of the mass moment weights may be a radial, tangential or axial

15    component of the mass moment, as shown in Figure 1.

A simulated blisk is formed by selecting a plurality of blades from the distribution and locating the blades at the blade positions around the blisk. The unbalance effect of each blade is calculated by multiplying the mass of the blade by the radius to the centre

20    of mass of the blade. From this, a vector sum of the unbalances of each blade is calculated so as to determine the resulting unbalance for the blisk.

This process is repeated for every positional permutation of the selected blades and is again repeated for many sets of blades selected from the distribution, or vice-versa,

25    such that a distribution of the blisk unbalance is created.

The distribution of the blisk unbalance can be calculated using a Monte Carlo simulation, where the blades are modelled as individual normal distributions positioned around the blisk. However, other statistical methods may be used to calculate the

30    distribution of the blisk unbalance.

The distribution of the blisk unbalance shows the maximum unbalance for the selected distribution. From this value, one or more balance correction features, such as sacrificial balancing lands, can be provided on the blisk which allows the maximum unbalance to be corrected. This ensures that all blisks within the selected distribution

5    can be successfully balanced.

The selected distribution also shows how many blisks are expected to fall outside the defined maximum unbalance and thus can not be balanced using the sacrificial balancing land. These blisks will be rejected and thus the selected distribution provides

10   a measure of the risk in reducing the size of the sacrificial balancing land. For example, where the selected distribution is ±3 standard deviations ($\sigma$), it can be expected that 1 in every 370 blisks manufactured will fall outside of the range.

Having excluded the most extreme situations, the size of the balancing lands required

15   to balance the blisk are dramatically reduced with only a slight increase in the rejection rate of components.

The invention has been used on blisks of varying geometry and it has been observed that the ratio of the maximum possible unbalance to the maximum acquired with the

20   present invention varies depending on the relative sizes of the blades and disc. For example, a larger number of smaller sized blades on a large diameter disc generates a higher ratio than a small number of large blades on a smaller disc.

The present invention has been shown to provide a reduction in the size of the balance

25   correction feature of between 65% and 83% compared to the prior art method. This saves significant weight and thus improves the thrust to weight ratio, which leads to increased fuel economy and associated reduction in running costs, or to an increased payload for the aircraft.

In an alternative embodiment, the selection of the range of blade masses may be applied to the distribution of the blisk unbalance. Furthermore, the range of values included may be any selected range, with the selected range being chosen with regard to the associated rejection rate.

5

Figure 2 shows a Weibull plot of the predicted unbalance ("Model Prediction") and measured unbalance ("Measured Data") from a sample of manufactured blisks.

The Weibull plot shows the distributions (i.e. the initial unbalance and cumulative

10 density function of the occurrence of the initial unbalances) on a log-log scale, and expresses each distribution with a positional parameter ($\eta$) and a measure of spread of the data ($\beta$). The spread of the data ($\beta$) corresponds to the slope of the line in Figure 4 and thus is can be seen that the value of $\beta$ for the predicted unbalance does not correspond to that of the measured unbalance.

15

This can also be seen in Figure 3, which shows the Weibull probability density function plot of the predicted unbalance ("Modelled data") and the measured unbalance from the sample of manufactured blisks ("Measured data").

20 In another embodiment of the invention, a tool wear characteristic is included in the distribution of the mass moment weights of the blades.

The tool wear characteristic is based on the manufacturing process used to make the blisk. In the present case, the blisk is machined from solid using the same cutter for all

25 of the blades. Therefore, as the cutter becomes worn during the manufacturing process, the blades become slightly larger and thus heavier. Furthermore, the cutting forces become larger as the cutter becomes worn, causing the blade to push-off during machining and thus resulting in a heavier blade. Consequently, the tool wear generates a circumferential variation in the mass moment of the aerofoils and hence an

30 associated unbalance.

In order to incorporate a tool wear characteristic, an estimate is made of the effect of the worn tool on the blade mass. Here, the mass is assumed to increase linearly around the circumference of the blisk in the sequence of blade manufacture. However, other corrections may be applied depending on the manufacturing process.

5

Figures 2 and 3 also shows the predicted unbalance including this tool wear characteristic ("Model Prediction + Toolwear"). As shown, the predicted unbalance including the tool wear characteristic provides a very close correlation with the measured distribution data.

10

Accordingly, the predicted unbalance ("Model Prediction") is considered suitable where the manufacturing process does not bias the unbalance within the blisk.

Although the invention has been described with reference to a blisk, it could also be

15      applied to a bladed ring (bling) or other rotating component.

To avoid unnecessary duplication of effort and repetition of text in the specification, certain features are described in relation to only one or several aspects or embodiments of the invention. However, it is to be understood that, where it is

20      technically possible, features described in relation to any aspect or embodiment of the invention may also be used with any other aspect or embodiment of the invention.

## CLAIMS

1    A method for predicting initial unbalance in a component comprising one or more
     elements, the method comprising:

     defining a statistical distribution of a mass moment weight of each of the one or
     more elements;

     restricting the statistical distribution to a selected range; and

     calculating an initial unbalance of the component for the restricted distribution of
     the one or more elements.

2    A method as claimed in claim 1, further comprising providing the component with
     a balance correction feature of suitable size to correct a maximum unbalance of
     the restricted distribution.

3    A method as claimed in claim 2, wherein the selected range indicates the
     probability of obtaining a component which cannot be balanced using the
     balance correction feature.

4    A method as claimed in any one of the preceding claims, wherein the component
     is a bladed disk or ring and the elements are a set of aerofoil components, the
     method further comprising:

     selecting a plurality of sets of aerofoil components from the statistical distribution
     and allocating a location for each aerofoil component on the bladed disk or ring,
     wherein each set of aerofoil components forms a sample distribution;

     calculating a vector sum of the mass moment weights for each sample
     distribution to determine the initial unbalance of the blisk.

5      A method as claimed in claim 4, wherein the method is repeated for every permutation of the mass moment weight and/or location of each aerofoil component.

6      A method as claimed in claim 4 or 5, wherein the statistical distribution includes a tool wear characteristic.

7      A method as claimed in claim 6, wherein the tool wear characteristic is based on the manufacturing process of the component.

8      A method as claimed in claim 6 or 7, wherein the tool wear characteristic defines an increase in the mass of the aerofoil components around the circumference of the bladed disk or ring.

9      A method as claimed in any one of the preceding claims, wherein the statistical distribution is a normal distribution.

10      A method as claimed in any one of the preceding claims, wherein the normal distribution has a maximum variation of ±8% from an expected value of the mass moment weight.

11      A method as claimed in any one of the preceding claims, wherein the selected range is ±3 standard deviations from an expected value of the mass moment weight.

12      A method as claimed in any one of the preceding claims, wherein the mass moment weight includes one or more of a radial, axial or tangential component.

13      A method as claimed in any one of the preceding claims, wherein the initial unbalance is calculated using a Monte Carlo simulation.

14      A method as claimed in any one of the preceding claims,

15      A method for predicting initial unbalance in a bladed disk or ring substantially as described herein.

5

## CLAIMS

1    A method for predicting initial unbalance in a component comprising one or more elements, the method comprising:

defining a statistical distribution of a mass moment weight of each of the one or more elements;

restricting the statistical distribution to a selected range of mass moment weight for each of the one or more elements; and

calculating an initial unbalance of the component for the selected range of mass moment weight of the one or more elements, and

providing the component with a balance correction feature of suitable size to correct a maximum unbalance of the restricted distribution.

2    A method as claimed in claim 1, wherein the selected range indicates the probability of obtaining a component which cannot be balanced using the balance correction feature.

3    A method as claimed in any one of the preceding claims, wherein the component is a bladed disk or ring and the elements are a set of aerofoil components, the method further comprising:

selecting a plurality of sets of aerofoil components from the statistical distribution and allocating a location for each aerofoil component on the bladed disk or ring, wherein each set of aerofoil components forms a sample distribution;

calculating a vector sum of the mass moment weights for each sample distribution to determine the initial unbalance of the blisk.

4  A method as claimed in claim 3, wherein the method is repeated for every permutation of the mass moment weight and/or location of each aerofoil component.

5  A method as claimed in claim 3 or 4, wherein the statistical distribution includes a tool wear characteristic.

6  A method as claimed in claim 5, wherein the tool wear characteristic is based on the manufacturing process of the component.

7  A method as claimed in claim 5 or 6, wherein the tool wear characteristic defines an increase in the mass of the aerofoil components around the circumference of the bladed disk or ring.

8  A method as claimed in any one of the preceding claims, wherein the statistical distribution is a normal distribution.

9  A method as claimed in any one of the preceding claims, wherein the normal distribution has a maximum variation of ±8% from an expected value of the mass moment weight.

10  A method as claimed in any one of the preceding claims, wherein the selected range is ±3 standard deviations from an expected value of the mass moment weight.

11  A method as claimed in any one of the preceding claims, wherein the mass moment weight includes one or more of a radial, axial or tangential component.

12  A method as claimed in any one of the preceding claims, wherein the initial unbalance is calculated using a Monte Carlo simulation.

13    A method for predicting initial unbalance in a bladed disk or ring substantially as
described herein.

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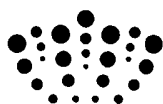
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|---|---|---|
| **Application No:** GB1010757.1 | **Examiner:** | Mr Daniel Jones |
| **Claims searched:** 1-15 | **Date of search:** | 30 July 2010 |

## Patents Act 1977: Search Report under Section 17

**Documents considered to be relevant:**

| Category | Relevant to claims | Identity of document and passage or figure of particular relevance |
|---|---|---|
| X | 1 at least. | JP2003323468 A (TSURUMI MFG) Whole doc. is relevant. |
| X | 1 at least. | JP2003323469 A (TSURUMI MFG) Whole doc. is relevant. |
| A | - | JP10281913 A (AKASHI CORP) |
| A | - | US2005/273302 A1 (SMITH INTERNATIONAL) |

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**Field of Search:**

Search of GB, EP, WO & US patent documents classified in the following areas of the UKC$^X$ :

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Worldwide search of patent documents classified in the following areas of the IPC

| F01D; F04D; G01M; G06F |
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The following online and other databases have been used in the preparation of this search report

| WPI, EPODOC |
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**International Classification:**

| Subclass | Subgroup | Valid From |
|---|---|---|
| G01M | 0001/14 | 01/01/2006 |
| G01M | 0001/38 | 01/01/2006 |
| G06F | 0017/50 | 01/01/2006 |