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(54) **Title: ROBOTIC SYSTEMS, METHODS AND** SOFTWARE PROGRAMS FOR **MODIFYING** TOOL OPERATION **BASED ON TISSUE** PARAMETERS

(57) Abstract: **A** computer-implemented surgical planning method is provided. The method includes obtaining anatomical data of an anatomical volume and path data including a tool path along which a tool will move. The method also includes obtaining tool data; merging the path data and the anatomical data; and for a point of the tool path, identifying a location of the point, loading a geometry of the tool at the location, identifying an intersection between the tool and the anatomical volume at the location, determining density values of the anatomical data within the intersection, computing a tool contact factor related to the intersection, setting a planned feed rate factor for the tool based on the density values and the tool contact factor, associating the planned feed rate factor with the point; and outputting cut plan data including the planned feed rate factor associated with the point of the tool path.

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ROBOTIC SYSTEMS, METHODS AND SOFTWARE PROGRAMS FOR MODIFYING TOOL OPERATION BASED ON TISSUE PARAMETERS

CROSS-REFERENCE **TO RELATED APPLICATIONS**

[0001] The subject application claims priority to and all the benefits of United States Provisional Patent Application No. **63/291,566,** filed December 20, 2021, the entire contents of which are hereby incorporated **by** reference.

TECHNICAL FIELD

[0002] The present disclosure relates generally to robotic systems, methods, and software programs for modifying tool operation based on tissue parameters, such as bone density.

BACKGROUND

[0003] Robotic systems that perform surgical procedures at surgical sites often include a manipulator with a base, a plurality of links and joints, and an end effector coupled to the manipulator. Many times, the end effector comprises or supports a surgical tool with an energy applicator designed to remove tissue at the surgical site.

[0004] The energy applicator is typically moved along a tool path to remove tissue at the surgical site. The velocity or speed at which the energy applicator moves along the tool path is commonly known to those skilled in the art as a "feed rate" of the tool or energy applicator.

[0005] Prior systems have contemplated to adjust or determine the feed rate to account for conditions or inputs, such as manual user selection of the feed rate, characteristics of the tissue such as bone mineral density, sensed forces applied to the energy applicator, curvature of the path, and the like.

[0006] However, prior feed rate techniques fall short in providing in-depth pre planning of the tool path feed rates based on, at least, detailed analysis of the patient imaging data and density of the anatomy relative to the planned tool path. For example, in determining the feed rate, the prior techniques fail to account for, among other things, a ratio of intersection of the tool geometry relative to the anatomy as evaluated at point(s) along the tool path or whether certain portions of the anatomy would have been already removed **by** the tool at another point along the tool path. In turn, the prior feed rate techniques may lead to outcomes that are less than optimal, such as implant fit issues due to resection under-sizing or tool skiving, formation of pits in the resection surface, sub-optimal cutting forces applied **by** the tool, and the like. There remains a need to address at least some of these deficiencies.

SUMMARY

[0007] This Summary introduces a selection of concepts in a simplified form that are further described below in the Detailed Description below. This Summary is not intended to limit the scope of the claimed subject matter nor identify key features or essential features of the claimed subject matter.

[0008] In a first aspect, a computer-implemented surgical planning method is provided. The method comprises: obtaining anatomical data comprising a geometry and density values of an anatomical volume; obtaining path data comprising a tool path along which a robotic manipulator will move a tool to interact with the anatomical volume, the tool path defined **by** points between which the tool will successively pass; obtaining tool data including a geometry of the tool that will interact with the tool path; merging the path data and the anatomical data; and for at least one point of the tool path: identifying a location of the point relative to the anatomical data, loading, from the tool data, the geometry of the tool at the identified location, at the identified location, identifying an intersection between the geometry of the tool and the anatomical volume, determining density values of the anatomical data within the intersection, computing a tool contact factor related to an interaction between the geometry of the tool and the anatomical volume, setting a planned feed rate factor for the tool based on the determined density values and the computed tool contact factor, and associating the planned feed rate factor with the at least one point; and outputting cut plan data comprising the tool path including the planned feed rate factor associated with the at least one point of the tool path.

[0009] In a second aspect, a non-transitory computer readable medium is provided. The non-transitory computer readable medium has stored thereon instructions which, when executed **by** one or more processors, implements a computer-implemented surgical planning software configured to: obtain anatomical data comprising a geometry and density values of an anatomical volume; obtain path data comprising a tool path along which a robotic manipulator will move a tool to interact with the anatomical volume, the tool path defined **by** points between which the tool will successively pass; obtain tool data including a geometry of the tool that will interact with the tool path; merge the path data and the anatomical data; and for at least one point of the tool path: identify a location of the point relative to the anatomical data, load, from the tool data, the geometry of the tool at the identified location, at the identified location, identify an intersection between the geometry of the tool and the anatomical volume, determine density values of the anatomical data within the intersection, compute a tool contact factor related to an interaction between the geometry of the tool and the anatomical volume, set a planned feed rate factor for the tool based on the determined density values and the computed

tool contact factor, and associate the planned feed rate factor with the at least one point; and output cut plan data comprising the tool path including the planned feed rate factor associated with the at least one point of the tool path.

[0010] In a third aspect, a surgical system is provided. The surgical system comprising: a robotic manipulator configured to support and move a tool; and a control system coupled to the robotic manipulator, and comprising: one or more processors; and a non transitory computer readable medium, having stored thereon instructions which, when executed **by** the one or more processors, implement a computer-implemented surgical planning software configured to: obtain anatomical data comprising a geometry and density values of the anatomical volume; obtain path data comprising a tool path along which a robotic manipulator will move a tool to interact with an anatomical volume, the tool path defined **by** points between which the tool will successively pass; obtain tool data including a geometry of the tool that will interact with the tool path; merge the path data and the anatomical data; and for at least one point of the tool path: identify a location of the point relative to the anatomical data, load, from the tool data, the geometry of the tool at the identified location, at the identified location, identify an intersection between the geometry of the tool and the anatomical volume, determine density values of the anatomical data within the intersection, compute a tool contact factor related to an interaction between the geometry of the tool and the anatomical volume, set a planned feed rate factor for the tool based on the determined density values and the computed tool contact factor, and associate the planned feed rate factor with the at least one point; and output cut plan data comprising the tool path including the planned feed rate factor associated with the at least one point of the tool path; and wherein the control system utilizes the outputted cut plan data to control the robotic manipulator to move the tool along the tool path according to the planned feed rate factor associated with the at least one point of the tool path for enabling the tool to interact with the anatomical volume. **A** method of operating the surgical system of the third aspect is also provided.

[0011] In a fourth aspect, a computer-implemented surgical planning method is provided. The computer-implemented surgical planning method comprises: obtaining anatomical data comprising a geometry of an anatomy; obtaining path data comprising a tool path along which a robotic manipulator will move a tool to interact with the anatomy, the tool path defined **by** points between which the tool will pass; obtaining tool data including a geometry of the tool; merging the path data and the anatomical data; for at least one point of the tool path: identifying a location of the point relative to the anatomical data, loading, from the tool data, the geometry of the tool at the identified location, computing a tool contact factor

related to an interaction between the geometry of the tool and the anatomical volume, setting a planned feed rate factor for the tool based on the computed tool contact factor, and associating the planned feed rate factor with the at least one point; and outputting cut plan data comprising the tool path including the planned feed rate factor associated with the at least one point of the tool path. **A** non-transitory computer readable medium, or computer program product, comprising instructions to execute the computer-implemented method of the fourth aspect is also provided.

[0012] In a fifth aspect, a computer-implemented method is provided. The computer-implemented method comprises: obtaining anatomical data comprising a geometry and density values of an anatomical volume; obtaining virtual object data comprising geometry of a virtual object having a mesh of polygonal elements; merging the anatomical data and the virtual object data; determining a parameter for one or more polygonal elements of the mesh based on the density values; and modifying operation of a tool according to the parameter in response to the tool interacting with the one or more polygonal elements. **A** non-transitory computer readable medium, or computer program product, comprising instructions to execute the computer-implemented method of the fifth aspect is also provided.

[0013] In a sixth aspect, a computer-implemented method is provided. The computer-implemented method comprises: obtaining anatomical data comprising a geometry and density values of an anatomical volume; obtaining virtual object data comprising geometry of a virtual object having a mesh of polygonal elements; and merging the anatomical data and the virtual object data to determine a parameter for one or more polygonal elements of the mesh based on the density values. **A** non-transitory computer readable medium, or computer program product, comprising instructions to execute the computer-implemented method of the sixth aspect is also provided.

[0014] In a seventh aspect, a non-transitory computer readable medium is provided. The non-transitory computer readable medium has stored thereon instructions which, when executed **by** one or more processors, implements a computer-implemented surgical planning software configured to: obtain anatomical data comprising a geometry and a tissue parameter of an anatomical volume; obtain path data comprising a tool path along which a robotic manipulator will move a tool to interact with the anatomical volume, the tool path defined **by** points between which the tool will successively pass; obtain tool data including a geometry of the tool that will interact with the tool path; merge the path data and the anatomical data; and for at least one point of the tool path: identify a location of the point relative to the anatomical data, load, from the tool data, the geometry of the tool at the identified location, at the identified

location, identify an intersection between the geometry of the tool and the anatomical volume, determine the tissue parameter of the anatomical data within the intersection, compute a tool contact factor related to an interaction between the geometry of the tool and the anatomical volume, set a planned feed rate factor for the tool based on the determined tissue parameter and the computed tool contact factor, and associate the planned feed rate factor with the at least one point; and output cut plan data comprising the tool path including the planned feed rate factor associated with the at least one point of the tool path. **A** computer-implemented method of executing the steps of the seventh aspect is also provided.

[0015] In an eighth aspect, a non-transitory computer readable medium is provided. The non-transitory computer readable medium has stored thereon instructions which, when executed **by** one or more processors, implements a computer-implemented surgical planning software configured to: obtain anatomical data comprising a geometry and a tissue parameter of an anatomical volume; obtain path data comprising a tool path along which a robotic manipulator will move a tool to interact with the anatomical volume, the tool path defined **by** points between which the tool will successively pass; obtain tool data including a geometry of the tool that will interact with the tool path; merge the path data and the anatomical data; and for at least one point of the tool path: identify a location of the point relative to the anatomical data, load, from the tool data, the geometry of the tool at the identified location, at the identified location, identify an intersection between the geometry of the tool and the anatomical volume, determine the tissue parameter of the anatomical data within the intersection, compute a tool contact factor related to an interaction between the geometry of the tool and the anatomical volume, set a output pose for the tool based on the determined tissue parameter and the computed tool contact factor, and associate the output pose with the at least one point; and output cut plan data comprising the tool path including the output pose associated with the at least one point of the tool path. **A** computer-implemented method of executing the steps of the eighth aspect is also provided.

[0016] In a ninth aspect, a non-transitory computer readable medium is provided. The non-transitory computer readable medium has stored thereon instructions which, when executed **by** one or more processors, implements a computer-implemented surgical planning software configured to: obtain anatomical data comprising a geometry and a tissue parameter of an anatomical volume; obtain path data comprising a tool path along which a robotic manipulator will move a tool to interact with the anatomical volume, the tool path defined **by** points between which the tool will successively pass; obtain tool data including a geometry of the tool that will interact with the tool path; merge the path data and the anatomical data; and

for at least one point of the tool path: identify a location of the point relative to the anatomical data, load, from the tool data, the geometry of the tool at the identified location, at the identified location, identify an intersection between the geometry of the tool and the anatomical volume, determine the tissue parameter of the anatomical data within the intersection, compute a tool contact factor related to an interaction between the geometry of the tool and the anatomical volume, set a planned feed rate factor for the tool based on the determined tissue parameter, the computed tool contact factor, and achieving a predetermined motor current on a motor of the tool, and associate the planned feed rate factor with the at least one point; and output cut plan data comprising the tool path including the planned feed rate factor associated with the at least one point of the tool path. **A** computer-implemented method of executing the steps of the ninth aspect is also provided.

[0017] In a tenth aspect, a non-transitory computer readable medium, having stored thereon instructions which, when executed **by** one or more processors, implement a computer implemented surgical planning software configured to: obtain anatomical data comprising a geometry and a tissue parameter of an anatomical volume; obtain path data comprising a tool path along which a robotic manipulator will move a tool to interact with the anatomical volume, the tool path defined **by** points between which the tool will successively pass; obtain tool data including a geometry of the tool that will interact with the tool path; merge the path data and the anatomical data; and for at least one point of the tool path: identify a location of the point relative to the anatomical data, load, from the tool data, the geometry of the tool at the identified location, at the identified location, identify an intersection between the geometry of the tool and the anatomical volume, determine the tissue parameter of the anatomical data within the intersection, compute a tool contact factor related to an interaction between the geometry of the tool and the anatomical volume, set a tool operation parameter based on the determined tissue parameter and the computed tool contact factor, and associate the tool operation parameter with the at least one point; and output plan data comprising the tool path including the tool operation parameter associated with the at least one point of the tool path. **A** computer implemented method of executing the steps of the tenth aspect is also provided.

[0018] In an eleventh aspect, a computer-implemented method is provided comprising: identifying an intersection between a geometry of a tool and an anatomical volume, determining a tissue parameter of the anatomical data within the intersection, computing a tool contact factor related to an interaction between the geometry of the tool and the anatomical volume, and setting a tool operation parameter based on the determined tissue parameter and

the computed tool contact factor. **A** computer program product or robotic system implementing the steps of the eleventh aspect is also provided.

[0019] Any of the above aspects can be combined in part or in whole.

[0020] Any of the above aspects can be implemented as a computer-implemented method, a robotic surgical system, and/or a non-transitory computer readable medium having stored thereon instructions which, when executed **by** one or more processors, implement a computer-implemented surgical planning software or computer program product.

[0021] Any of the above aspects can be utilized with any of the following implementations, whether used in part or in whole.

[0022] In one implementation, obtaining anatomical data includes obtaining a bone model associated with the anatomical volume. In one implementation, obtaining path data further includes obtaining the tool path being predetermined based on a planned resection volume of the bone model of the anatomical volume. In one implementation, obtaining path data further includes obtaining the tool path being predetermined based on a geometry of an implant model selected for the bone model. In some implementations, the bone model may be patient-specific or a statistical bone model. In some implementations, obtaining path data includes obtaining a predefined pose of the tool with respect to at least one point of the tool path. The bone model can be of an acetabulum, a glenoid, or any type of joint socket. The bone model can be of a femur, tibia, humerus, or portion of the spine (vertebra). In one implementation, the anatomical data is obtained without preoperative images (e.g., imageless) or without forming a bone model. The bone model may be patient-specific or may be based on a statistical dataset from a similar population.

[0023] In one implementation, obtaining anatomical data includes obtaining imaging data including slices of the anatomical volume. In one implementation, obtaining imaging data includes obtaining **DICOM** data including intercept and slope values, slice thickness, and patient position at a time of imaging. In one implementation, obtaining anatomical data includes obtaining **CT** slices of the anatomical volume. In such an implementation, the geometry of the tool comprises a **3-D** geometry of the tool and, for the at least one point of the tool path, loading the **3-D** geometry of the tool at the identified location, and at the identified location, identifying **CT** slices for which there is a cross-sectional intersection between the **3-D** geometry of the tool and the anatomical volume; for each identified **CT** slice, determining a Hounsfield unit for each pixel within the cross-sectional intersection; and collecting the Hounsfield units from the pixels within the cross-sectional intersections of each of the identified **CT** slices.

[0024] In one implementation, identifying the intersection, at the identified location, between the geometry of the tool and the anatomical volume includes identifying one or more slices of the imaging data exhibiting the intersection between the geometry of the tool and the anatomical volume. One implementation includes, for the at least one point of the tool path, and after identifying slices of the imaging data exhibiting the intersection between the geometry of the tool and the anatomical volume, for each identified slice, computing the intersection ratio related to the geometry of the tool within the intersection relative to the geometry of the tool outside of the intersection. One implementation includes, for each identified slice, determining a quantity of pixels within the geometry of the tool having Hounsfield units exceeding a predetermined threshold.

[0025] In one implementation, determining density values of the anatomical data within the intersection includes, for each identified slice, determining radiodensity values of the imaging data located within the intersection. In one implementation, determining density values of the anatomical data within the intersection includes collecting radiodensity values located within the intersections of each of the one or more identified slices. In one implementation collecting the radiodensity values located within the intersection of each of the one or more identified slices includes identifying one or more of: an average, a median, and a maximum radiodensity value from the collected radiodensity values.

[0026] In one implementation, setting the planned feed rate factor for the tool based on the determined density values includes calculating a bone mineral density (BMD) factor of the anatomical volume relative to the identified location based on the collected radiodensity values. In one implementation, setting the planned feed rate factor for the tool based on the determined density values includes setting the planned feed rate factor for the tool based on the calculated BMD factor. In one implementation, calculating the BMD factor includes converting an average, a median, and/or a maximum radiodensity value into the BMD factor. In one implementation, converting the one or more of: the average, the median, and the maximum radiodensity value into the BMD factor includes multiplying the one or more of: the average, the median, and the maximum radiodensity value with the intersection ratio. In one implementation, setting the planned feed rate factor for the tool based on the determined density values includes setting the planned feed rate factor based on the calculated BMD factor. One implementation includes accessing a look-up table defining associations between predefined bone mineral density (BMD) factors and predefined feed rate factors. In such an implementation, for at least one point of the tool path, setting the planned feed rate factor based on the calculated BMD factor includes identifying, in the look-up table, the predefined BMD

factor that is closest to the calculated BMD factor; and setting the planned feed rate factor based on the predefined feed rate factor associated with the closest identified predefined BMD factor in the look-up table. In one implementation, for the at least one point of the tool path, setting the planned feed rate factor based on the calculated BMD factor includes setting the planned feed rate factor to be a maximum feed rate factor in response to determining that the calculated BMD factor is below a minimum threshold; and/or setting the planned feed rate factor to be a minimum feed rate factor in response to determining that the calculated BMD factor is above a maximum threshold. In one implementation, setting the planned feed rate factor includes setting the planned feed rate factor based on achieving a predetermined motor current on a motor of the tool.

[0027] One implementation includes, for one point of the tool path, storing interaction coordinates obtained from the intersection between the geometry of the tool and the anatomical volume at the location of the one point, the interaction coordinates indicative of locations of simulated interaction between the geometry of the tool and the anatomical volume at the location of the one point; and for a second point of the tool path successive to the one point; identifying a location of the second point relative to the anatomical data, loading, from the tool data, the geometry of the tool at the identified location of the second point, at the identified location of the second point, identifying an intersection between the geometry of the tool and the anatomical volume, determining density values of the anatomical data within the intersection at the location of the second point, comparing coordinates of the determined density values to the interaction coordinates; and disregarding any density values having coordinates that are identical to the interaction coordinates.

[0028] One implementation includes, for the at least one point of the tool path, disregarding any density values located beyond the intersection between the geometry of the tool and the anatomical volume.

[0029] In one implementation, merging the path data and the anatomical data includes merging the path data and anatomical data into a common coordinate system.

[0030] In one implementation, the cut plan data comprises the tool path along which a robotic manipulator will move a tool in an autonomous mode to interact with the anatomical volume.

[0031] One implementation includes, for each point of the tool path: identifying the location of the point relative to the anatomical data, loading, from the tool data, the geometry of the tool at the identified location, at the identified location, identifying the intersection between the geometry of the tool and the anatomical volume, determining density values of the

anatomical data within the intersection, setting the planned feed rate factor for the tool based on the determined density values, and associating the planned feed rate factor with the point; and wherein outputting the cut plan data further comprises the tool path including the planned feed rate factor associated with each point of the tool path.

[0032] In one implementation, the robotic manipulator is commanded to move the tool according to a first feed rate; while the tool moves according to the first feed rate, an interaction between the virtual model and the one or more polygonal elements of the virtual object is detected. **A** second feed rate is computed based on the parameter associated with the one or more polygonal elements. Operation of the tool is modified such that the robotic manipulator is commanded to move the tool at the second feed rate.

[0033] In one implementation, the robotic manipulator is commanded to move the tool. The virtual model of the tool penetrates the one or more polygonal elements of the virtual object; **A** reactive force is computed based on the parameter associated with the one or more polygonal elements; a reactive force is applied to the virtual model in the virtual simulation to reduce penetration of the one or more polygonal elements **by** the virtual model; and operation of the tool is modified such that the robotic manipulator is commanded to move the tool in accordance with application of the reactive force to the virtual model in the virtual simulation to constrain movement of the tool relative to the virtual object.

DESCRIPTION OF THE DRAWINGS

[0034] Advantages of the present disclosure will be readily appreciated as the same becomes better understood **by** reference to the following detailed description when considered in connection with the accompanying drawings.

[0035] Figure 1 is a perspective view of one implementation of a robotic surgical system.

[0036] Figure 2 is a block diagram of a control system, including components and controllers, for controlling the robotic surgical system, according to one implementation.

[0037] Figure **3** is a functional block diagram of a software program utilized **by** the robotic surgical system, according to one implementation.

[0038] Figure 4 is a flow chart of a method determining cut plan data.

[0039] Figure **5** is a diagram illustrating a step of the method of Figure 4 of merging path data and anatomical data.

[0040] Figure **6** is a diagrammatic view of cut plan data.

[0041] Figure **7** includes multiple cross-sectional views of an intersection of a tool of the robotic surgical system of Figure 1 and an anatomical volume.

[0042] Figure **8** is a cross-sectional view of an intersection of the tool of the robotic surgical system of Figure 1 and the anatomical volume.

[0043] Figure **9** is a table illustrating stored quantities used for determining the cut plan data.

[0044] Figure **10** is a look-up table defining associations between predefined bone mineral density factors and predefined feed rate factors.

[0045] Figure 11 is a cross-sectional view of an intersection of the tool of the robotic surgical system of Figure 1 and the anatomical volume when the tool is located at a first point and an intersection of the tool of the robotic surgical system of Figure 1 and the anatomical volume when the tool is located at a second point.

[0046] Figure 12 is a diagram illustrating a step of a virtual object and anatomical data.

[0047] Figures **13A** and 13B are various view of the tool of the robotic surgical system of Figure 1 interacting with the virtual object of Figure 12.

DETAILED DESCRIPTION

[0048] I. System Overview

[0049] Referring to **FIG. 1,** a robotic surgical system **10** is illustrated. The system **10** is useful for treating a surgical site or anatomical volume (AV) of a patient 12, such as treating bone or soft tissue. In **FIG. 1,** the patient 12 is undergoing a surgical procedure. The anatomy in **FIG.** 1 includes a femur F and a tibia T of the patient 12. The surgical procedure may involve tissue removal or other forms of treatment. Treatment may include cutting, coagulating, lesioning the tissue, other *in-situ* tissue treatments, or the like. In some examples, the surgical procedure involves partial or total knee or hip joint replacement surgery, shoulder joint replacement surgery, spine surgery, or ankle surgery. In some examples, the system **10** is designed to cut away material to be replaced **by** surgical implants, such as hip and knee implants, including unicompartmental, bicompartmental, multicompartmental, or total knee implants. Some of these types of implants are shown in **U.S.** Patent Application Publication No. 2012/0330429, entitled "Prosthetic Implant and Method of Implantation," the disclosure of which is hereby incorporated **by** reference. The system **10** and techniques disclosed herein may be used to perform other procedures, surgical or non-surgical, or may be used in industrial applications or other applications where robotic systems are utilized.

[0050] As shown in **FIG.** 1, the system **10** includes a manipulator 14. **A** manipulator cart **17** (as shown in **FIG. 1)** can support the manipulator 14 such that the manipulator 14 is fixed to the manipulator cart **17.** The manipulator 14 has a base **16** and plurality of links **18.**

In one example, pairs of adjacent links **18** are connected **by** one of the joints **J.** The links **18** collectively form one or more arm(s) **23** of the manipulator 14. The manipulator 14 may have a serial arm configuration (as shown in **FIG. 1),** a parallel arm configuration, or any other suitable manipulator configuration. In other examples, more than one manipulator 14 may be utilized in a multiple arm configuration. The manipulator 14 according to one example has six joints **J1-J6** implementing at least six-degrees of freedom (DOF) for the manipulator 14. The manipulator 14 may have any number of degrees of freedom and may have any suitable number of joints **J** and may have redundant joints. The manipulator 14 can also be mounted to a surgical table or partially supported **by** the patient.

[0051] At each joint **J,** there may be an actuator, such as a joint motor **27** disposed between adjacent links **18.** The joint motors **27** are configured to rotate the links **18.** As such, positions of the links **18** are set **by** joint motors **27.** Each joint motor **27** may be attached to a structural frame internal to the manipulator 14. In one example, the joint motor **27** is a servo motor, such as a permanent magnet brushless motor. The joint motor **27** may have other configurations, such as synchronous motors, brush-type **DC** motors, stepper motors, induction motors, and the like.

[0052] The joint motors **27** are positioned at one of a plurality of angular positions, hereinafter referred to as joint angles. The joint angle is the angle of the joint **J** between adjacent links **18.** Each joint **J** may be configured to undergo a joint torque. The joint torque is a turning or twisting "force" of the joint **J** and is a function of the force applied at a length from a pivot point of the joint **J. A** torque sensor may be connected to one or more joint motors **27** for measuring the joint torque of the joint **J.** Alternatively, signals representative of currents applied to the joint motors **27** may be used to measure the joint torques.

[0053] One or more joint motors **27** may be equipped with a position sensor or encoder **19.** For simplicity, one joint encoder **19** is illustrated in **FIG. 1,** although other joint encoders **19** may be similarly illustrated. Alternatively, one or more links **18** being driven **by** that joint motor **27** may be equipped with the position sensor or encoder **19.** The encoder **19** may measure the joint angle of the respective joint **J.** In some embodiments, two encoders, one for the joint motor **27** and one for the link **18** being moved can be used to determine the joint angle, such as **by** averaging the joint angle, and the displacement between joint motor **27** and joint through the compliant transmission. The manipulator 14 need not require joint encoders **19** but may alternatively, or additionally, utilize motor encoders present on joint motors **27** at one or more joints **J.** Also, the manipulator 14 need not require rotary joints, but may alternatively, or additionally, utilize one or more prismatic joints. Certain joints **J** may be

passively moveable and lockable while other joints **J** may be actively driven. Any suitable combination of joint types is contemplated.

[0054] Referring to **FIG. 1,** the base **16** of the manipulator 14 is generally a portion of the manipulator 14 that provides a fixed reference coordinate system for other components of the manipulator 14 or the system **10** in general. Generally, the origin of a manipulator coordinate system **MNPL** is defined at the fixed reference of the base **16.** The base **16** may be defined with respect to any suitable portion of the manipulator 14, such as one or more of the links **18.** Alternatively, or additionally, the base **16** may be defined with respect to the manipulator cart **17,** such as where the manipulator 14 is physically attached to the manipulator cart **17.** In one example, the base **16** is defined at an intersection of the axes of joints **JI** and **J2.** Thus, although joints J1 and **J2** are moving components in reality, the intersection of the axes of joints **JI** and **J2** is nevertheless a virtual fixed reference pose, which provides both a fixed position and orientation reference and which does not move relative to the manipulator 14 and/or manipulator cart **17.** In other examples, the manipulator 14 can be a hand-held manipulator where the base **16** is a base portion of a tool (e.g., a portion held free hand **by** the user or coupled to a set-up linkage) and the tool tip is movable (e.g., semi-autonomously) relative to the base portion. The base portion has a reference coordinate system that is tracked, and the tool tip has a tool tip coordinate system that is computed relative to the reference coordinate system (e.g., via motor and/or joint encoders and forward kinematic calculations). Movement of the tool tip can be controlled to follow the path since its pose relative to the path can be determined. Such a hand-held configuration can be like that described in **U.S.** Patent No. **9,707,043,** entitled "Surgical Instrument Including Housing, a Cutting Accessory that Extends from the Housing and Actuators that Establish the Position of the Cutting Accessory Relative to the Housing," the entire content of which is hereby incorporated **by** reference.

[0055] A tool 20 couples to the manipulator 14 and is movable relative to the base **16** to interact with the anatomy in certain modes. The tool 20 is a physical and surgical tool and is, or forms part of, an end effector 22 supported **by** the manipulator 14 in certain embodiments. The tool 20 may be grasped **by** the user. One possible arrangement of the manipulator 14 and the tool 20 is described in **U.S.** Patent No. **9,119,655,** entitled "Surgical Manipulator Capable of Controlling a Surgical Instrument in Multiple Modes," the disclosure of which is hereby incorporated **by** reference. The manipulator 14 and the tool 20 may be arranged in alternative configurations. The tool 20 can be like that shown in **U.S.** Patent Application Publication No. 2014/0276949, filed on March *15,* 2014, entitled "End Effector of a Surgical Robotic Manipulator," hereby incorporated **by** reference.

[0056] The tool 20 includes an energy applicator 24 designed to contact and remove the tissue of the patient 12 at the surgical site. In one example, the energy applicator 24 is a bur **25** or surgical cutter. The tool 20 may comprise a tool shaft **33** having a proximal end coupled to the manipulator 14 and a distal end where the energy applicator 24 is located. The tool shaft **33** rotates about a cutting axis such that the energy applicator 24 can manipulate the tissue. The bur **25** may be substantially spherical and comprise a spherical center, radius (r) and diameter. Alternatively, the energy applicator 24 may be a drill bit, a saw blade, an ultrasonic vibrating tip, or the like. The tool 20 and/or energy applicator 24 may comprise any geometric feature, e.g., perimeter, circumference, radius, diameter, width, length, volume, area, surface/plane, range of motion envelope (along any one or more axes), etc. The geometric feature may be considered to determine how to locate the tool 20 relative to the tissue at the surgical site to perform the desired treatment. In some of the embodiments described herein, a spherical bur having a tool center point (TCP) will be described for convenience and ease of illustration but is not intended to limit the tool 20 to any particular form.

[0057] A sensor **S,** such as a force-torque sensor, may be mounted proximal the end effector 22. The force-torque sensor **S** is configured to output variable signals as a function of a force and/or a torque to which the end effector 22 and/or tool 20 are exposed. **By** doing so, the force-torque sensor **S** allows sensing of an input force applied to the end effector 22 and/or tool 20 **by** the user. The input force can be utilized to control movement of the manipulator 14 to emulate the user's applied force/torque. The force-torque sensor **S** may also sense external forces applied to the energy applicator 24. In one implementation, the force-torque sensor **S** is a **6DOF** sensor such that the force-torque sensor **S** is configured to output signals representative of three mutually orthogonal forces and three torques about the axes of the orthogonal forces that are applied to the tool 20. Additionally, or alternatively, the input force applied to the end effector 22 and/or tool 20 may be determined using joint torques or electrical current sensors on the joint motors **27.**

[0058] Referring to **FIG. 1,** the manipulator 14 and/or manipulator cart **17** may house a manipulator controller **26,** or other type of control unit. The manipulator controller **26** may comprise one or more computers, or any other suitable form of controller that directs the motion of the manipulator 14. The manipulator controller **26** may have a central processing unit **(CPU)** and/or other processors, memory (not shown), and storage (not shown). The manipulator controller **26** is loaded with software as described below. The processors could include one or more processors to control operation of the manipulator 14. The processors can be any type of microprocessor, multi-processor, and/or multi-core processing system. The manipulator

controller **26** may additionally, or alternatively, comprise one or more microcontrollers, field programmable gate arrays, systems on a chip, discrete circuitry, and/or other suitable hardware, software, or firmware that can carry out the functions described herein. The term processor is not intended to limit any implementation to a single processor. The manipulator 14 may also comprise a user interface **UI** with one or more displays and/or input devices (e.g., push buttons, keyboard, mouse, microphone (voice-activation), gesture control devices, touchscreens, etc.).

[0059] The tool 20 may comprise a tool controller 21 to control operation of the tool 20, such as to control power to the tool (e.g., to a rotary motor of the tool 20), control movement of the tool **20,** control irrigation/aspiration of the tool 20, and/or the like. The tool controller 21 may be in communication with the manipulator controller **26** or other components. The tool 20 may also comprise a user interface **UI** with one or more displays and/or input devices (e.g., push buttons, keyboard, mouse, microphone (voice-activation), gesture control devices, touchscreens, etc.). The manipulator controller **26** controls a state (position and/or orientation) of the tool 20 (e.g., the tool center point (TCP)) with respect to a coordinate system, such as the manipulator coordinate system **MNPL.** The manipulator controller **26** can control (linear or angular) velocity, acceleration, or other derivatives of motion of the tool 20.

[0060] The TCP, in one example, is a predetermined reference point defined at the energy applicator 24. The geometry of the energy applicator 24 is known in or defined relative to a TCP coordinate system. The TCP may be located at the spherical center of the bur **25** of the tool 20 such that one point is tracked. The TCP may be defined in various ways depending on the configuration of the energy applicator 24. The control of the tool 20 is not limited to a center point. For example, any suitable primitives, meshes, etc., can be used to represent the tool 20.

[0061] The shaft **33** of the tool 20 has a known, or able to be calculated (i.e., not necessarily static), pose relative to other coordinate systems. The manipulator 14 could employ the joint/motor encoders, or any other non-encoder position sensing method, to enable a pose of the shaft **33** to be determined. The manipulator 14 may use joint measurements to determine pose of the shaft **33** and/or could employ techniques to measure pose of the shaft **33** directly.

[0062] As shown in **FIG. 1,** the system **10** may further include a navigation system **32.** One example of the navigation system **32** is described in **U.S.** Patent No. *9,008,757,* filed on September 24, **2013,** entitled "Navigation System Including Optical and Non-Optical Sensors," hereby incorporated **by** reference. The navigation system **32** tracks movement of various objects. Such objects include, for example, the manipulator 14, the tool 20 and the anatomy, e.g., femur F and tibia T. The navigation system **32** tracks these objects to gather

state information of the objects with respect to a (navigation) localizer coordinate system LCLZ. Coordinates in the localizer coordinate system LCLZ may be transformed to the manipulator coordinate system **MNPL,** and/or vice-versa, using transformations.

[0063] The navigation system **32** includes a cart assembly 34 that houses a navigation controller **36,** and/or other types of control units. **A** navigation user interface UI is in operative communication with the navigation controller **36.** The navigation user interface UI includes one or more displays **38.** The navigation system **32** can display a graphical representation of the relative states of the tracked objects to the user using the one or more displays **38.** The navigation user interface UI further comprises one or more input devices to input information into the navigation controller **36** or otherwise to select/control certain aspects of the navigation controller **36.** Such input devices include interactive touchscreen displays. The input devices may include any one or more of push buttons, a keyboard, a mouse, a microphone (voice-activation), gesture control devices, and the like.

[0064] The navigation system **32** also includes a navigation localizer *44* coupled to the navigation controller **36.** In one example, the localizer *44* is an optical localizer and includes a camera unit 46. The camera unit 46 has an outer casing 48 that houses one or more optical sensors **50.** The localizer *44* may comprise its own localizer controller 49 and may further comprise a video camera **VC,** such as a machine vision camera.

[0065] The navigation system **32** includes one or more trackers. In one example, the trackers include a pointer tracker PT, one or more manipulator trackers *52A,* 52B, a first patient tracker *54,* and a second patient tracker *56.* In the illustrated example of **FIG. 1,** the manipulator tracker is firmly attached to the tool 20 (i.e., tracker *52A),* the first patient tracker 54 is firmly affixed to the femur F of the patient 12, and the second patient tracker **56** is firmly affixed to the tibia T of the patient 12. In this example, the patient trackers *54,* **56** are firmly affixed to sections of bone. The pointer tracker PT is firmly affixed to a pointer P used for registering the anatomy to the localizer coordinate system LCLZ. The manipulator trackers *52A,* 52B may be affixed to any suitable component of the manipulator 14, in addition to, or other than, the tool 20, such as the base **16** (i.e., tracker 52B), or any one or more links **18** of the manipulator 14. The trackers **52A,** 52B, *54, 56,* PT may be fixed to their respective components in any suitable manner. For example, the trackers may be rigidly fixed, flexibly connected (optical fiber), or not physically connected at all (ultrasound), as long as there is a suitable (supplemental) way to determine the relationship (measurement) of that respective tracker to the object that it is associated with.

[0066] Any one or more of the trackers may include active markers *58.* The active markers *58* may include light emitting diodes (LEDs). Alternatively, the trackers *52A,* 52B, *54, 56,* PT may have passive markers, such as reflectors, which reflect light emitted from the camera unit 46. Other suitable markers not specifically described herein may be utilized.

[0067] The localizer *44* tracks the trackers **52A,** 52B, *54, 56,* PT to determine a state of the trackers **52A,** 52B, *54, 56,* PT, which corresponds respectively to the state of the object respectively attached thereto. The localizer *44* may perform known triangulation techniques to determine the states of the trackers **52A,** 52B, *54, 56,* PT, and associated objects. The localizer *44* provides the state of the trackers **52A,** 52B, *54, 56,* PT to the navigation controller **36.** In one example, the navigation controller **36** determines and communicates the state of the trackers **52A,** 52B, *54, 56,* PT to the manipulator controller **26.** As used herein, the state of an object includes, but is not limited to, data that defines the position and/or orientation of the tracked object or equivalents/derivatives of the position and/or orientation. For example, the state may be a pose of the object, and may include linear velocity data, and/or angular velocity data, and the like.

[0068] The navigation controller **36** may comprise one or more computers, or any other suitable form of controller. The navigation controller **36** has a central processing unit **(CPU)** and/or other processors, memory (not shown), and storage (not shown). The processors can be any type of processor, microprocessor, or multi-processor system. The navigation controller **36** is loaded with software. The software, for example, converts the signals received from the localizer 44 into data representative of the position and orientation of the objects being tracked. The navigation controller **36** may additionally, or alternatively, comprise one or more microcontrollers, field programmable gate arrays, systems on a chip, discrete circuitry, and/or other suitable hardware, software, or firmware that can carry out the functions described herein. The term processor is not intended to limit to a single processor.

[0069] Although one example of the navigation system **32** is shown that employs triangulation techniques to determine object states, the navigation system **32** may have any other suitable configuration for tracking the manipulator 14, tool 20, and/or the patient 12. In another example, the navigation system **32** and/or localizer 44 are ultrasound-based. For example, the navigation system **32** may comprise an ultrasound imaging device coupled to the navigation controller **36.** The ultrasound imaging device images any of the aforementioned objects, e.g., the manipulator 14, the tool 20, and/or the patient 12, and generates state signals to the navigation controller **36** based on the ultrasound images. The ultrasound images may be **2-D, 3-D,** or a combination of both. The navigation controller **36** may process the images in

near real-time to determine states of the objects. The ultrasound imaging device may have any suitable configuration and may be different than the camera unit 46 as shown in **FIG. 1.**

[0070] In another example, the navigation system **32** and/or localizer 44 are radio frequency (RF)-based. For example, the navigation system **32** may comprise an RF transceiver coupled to the navigation controller **36.** The manipulator 14, the tool 20, and/or the patient 12 may comprise RF emitters or transponders attached thereto. The RF emitters or transponders may be passive or actively energized. The RF transceiver transmits an RF tracking signal and generates state signals to the navigation controller **36** based on RF signals received from the RF emitters. The navigation controller **36** may analyze the received RF signals to associate relative states thereto. The RF signals may be of any suitable frequency. The RF transceiver may be positioned at any suitable location to track the objects using RF signals effectively. Furthermore, the RF emitters or transponders may have any suitable structural configuration that may be much different than the trackers **52A,** 52B, *54, 56,* PT shown in **FIG. 1.**

[0071] In yet another example, the navigation system **32** and/or localizer 44 are electromagnetically based. For example, the navigation system **32** may comprise an EM transceiver coupled to the navigation controller **36.** The manipulator 14, the tool 20, and/or the patient 12 may comprise EM components attached thereto, such as any suitable magnetic tracker, electro-magnetic tracker, inductive tracker, or the like. The trackers may be passive or actively energized. The EM transceiver generates an EM field and generates states. Such navigation system **32** examples may have structural configurations that are different than the navigation system **32** configuration shown in **FIG. 1.**

[0072] The navigation system **32** may have any other suitable components or structure not specifically recited herein. Furthermore, any of the techniques, methods, and/or components described above with respect to the navigation system **32** shown may be implemented or provided for any of the other examples of the navigation system **32** described herein. For example, the navigation system **32** may utilize solely inertial tracking or any combination of tracking techniques, and may additionally, or alternatively, comprise fiber optic-based tracking, machine-vision tracking, and the like.

[0073] Referring to **FIG.** 2, the system **10** includes a control system **60** that comprises, among other components, the manipulator controller **26,** the navigation controller **36,** and the tool controller 21. The control system **60** further includes one or more software programs and software modules shown in **FIG. 3.** The software modules may be part of the program or programs that operate on the manipulator controller **26,** navigation controller **36,** tool controller 21, or any combination thereof, to process data to assist with control of the

system **10.** The software programs and/or modules include computer readable instructions stored in non-transitory memory *64* on the manipulator controller **26,** navigation controller **36,** tool controller 21, or a combination thereof, to be executed **by** one or more processors **70** of the controllers 21, **26, 36.** The memory 64 may be any suitable configuration of memory, such as RAM, non-volatile memory, etc., and may be implemented locally or from a remote database. Additionally, software modules for prompting and/or communicating with the user may form part of the program or programs and may include instructions stored in memory 64 on the manipulator controller **26,** navigation controller **36,** tool controller 21, or any combination thereof. The user may interact with any of the input devices of the navigation user interface UI or other user interface UI to communicate with the software modules. The user interface software may run on a separate device from the manipulator controller **26,** navigation controller **36,** and/or tool controller **21.**

[0074] The control system **60** may comprise any suitable configuration of input, output, and processing devices suitable for carrying out the functions and methods described herein. The control system **60** may comprise the manipulator controller **26,** the navigation controller **36,** or the tool controller 21, or any combination thereof, or may comprise one of these controllers. These controllers may communicate via a wired bus or communication network as shown in **FIG.** 2, via wireless communication, or otherwise. The control system **60** may also be referred to as a controller. The control system **60** may comprise one or more microcontrollers, field programmable gate arrays, systems on a chip, discrete circuitry, sensors, displays, user interfaces, indicators, and/or other suitable hardware, software, or firmware that is capable of carrying out the functions described herein.

[0075] Referring to **FIG. 3,** the software employed **by** the control system **60** may utilize anatomical data *65.* The anatomical data **65** may include imaging data of an anatomical volume AV of the patient 12. The imaging data may be obtained via any suitable imaging modality, such as MRI, X-Ray/Fluoroscopy, **CT,** and/or Ultrasound. The imaging data may include or be used to derive a geometry of the anatomical volume AV. For example, the imaging data may include imaged slices, such as **CT** slices which, in combination, form the geometry of the anatomical volume AV. The anatomical data **65** may also include Digital Imaging and Communications in Medicine **(DICOM)** data of the anatomical volume AV, which may include intercept and slope values of each slice, slice thickness, and a position of the patient 12 at a time of imaging.

[0076] The geometry of the anatomical volume AV may be a **2-D** or a **3-D** geometry. Referring to **FIG. 5,** the **3-D** geometry is represented using an anatomical model AM. **In FIG.**

6, the anatomical model AM is a **3-D** bone model of an acetabulum AM of the patient 12. As described, the bone model could be of any other type of bone, such as a femur, tibia, scapula (glenoid), humerus, vertebra, or the like. The anatomical model AM may be formed of imaged slices, such as **CT** slices, of the anatomical volume AV. Additionally, the **3-D** bone model may be a patient-specific bone model (e.g., based on a bone of the patient 12) or a statistical bone model (e.g., based on a bone of a representative patient). The bone model can be formed of any suitable method, such as manual or automated segmentation of imaging data, morphing of the statistical bone model, or the like.

[0077] The anatomical data **65** may also include density values DV of an anatomical volume AV. For instance, referring to **FIG.** *5,* the anatomical data **65** may include radiodensity values DV that are associated with the anatomical model AM. The radiodensity values DV may be mapped to coordinates, pixels, and/or voxels of the anatomical model AM. In this way, the anatomical data *65,* in addition to providing the anatomical model AM, also provides density values DV that correspond to the anatomical model AM. The density values DV may be any suitable density value. For instance, the density values DV may be measured in Hounsfield units **(HU),** as shown in **FIG. 5.** The density values DV can be determined or derived using any suitable technique. For example, the density values DV could be detected from electrical conductivity measurements of the anatomical volume AV. As another example, the density values DV may be determined using a density phantom that is imaged simultaneously with the anatomy. The density phantom may be imaged using bone densitometry, absorptiometry, quantitative computerized tomography, ultrasonography, dual energy X-ray absorptiometry **(DEXA),** scanning electron microscopy **(SEM),** or any other type of image analysis, or the like. The density values DV can be included in the **DICOM** data. Density values could also be obtained intra-operatively using, e.g., a **CT** scanning device in the operating room.

[0078] The control system **60** may be configured to normalize the density values DV. In some instances, the density values DV may vary depending on, among other things, the imaging modality and/or the system used to image the anatomical volume AV. For example, the density values DV may vary if the anatomical volume AV is scanned using an MRI or a **CT.** As another example, the density values DV may vary based on a type or brand of scanner used to image the anatomical volume AV. In such instances the control system **60** may normalize the density values DV to provide consistent interpretation or evaluation of the density values DV for the techniques described herein. In one example, the control system **60** may normalize or calibrate the density values DV based on parameters of a density phantom

that is imaged with the anatomical volume AV. In some instances, the control system **60** may normalize the density values DV **by** controlling the tool 20 to interact with the anatomical volume AV and measuring forces and torques related the interaction. For example, the control system **60** may control the tool 20 to cut a tissue of the anatomical volume AV and measure forces placed on the tool 20 (e.g., a motor **27** of the tool 20). The density values DV can be normalized **by** the control system **60** comparing the measured forces on the tool 20 to the raw density values.

[0079] Referring to **FIG. 3,** the software employed **by** the control system **60** can include a boundary generator **66.** As shown in **FIG. 6,** the boundary generator **66** is a software program or module that generates a virtual object **71** for constraining movement and/or operation of the tool 20. The virtual object **71** may be a virtual boundary and can be one dimensional, two-dimensional, or three-dimensional, and may comprise a point, line, axis, trajectory, plane, or other shapes, including complex geometric shapes. In some embodiments, the virtual object **71** is a surface defined **by** a polygonal or triangular mesh. The virtual objects **71** may be defined with respect to the anatomical model AM and can define a region of the anatomical model AM for which material is allowed to be removed **by** the tool 20 from a region of the anatomical model AM for which material is prohibited from being removed **by** the tool 20. In the example of **FIG. 5,** the virtual objects **71** are **3-D** boundaries that delineate an area for an acetabular component of a hip replacement surgery and are associated with the **3-D** anatomical model AM of the acetabulum. The anatomical model AM is registered to the one or more patient trackers 54, **56** such that the virtual objects **71** become associated with the anatomical model AM. The virtual objects **71** may be implant-specific, e.g., defined based on a size, shape, volume, etc. of an implant and/or patient-specific, e.g., defined based on the patient's anatomy. The virtual objects **71** may be created pre-operatively, intra-operatively, or combinations thereof. In other words, the virtual objects **71** may be defined before the surgical procedure begins, during the surgical procedure (including during tissue removal), or combinations thereof. In any case, the control system **60** obtains the virtual objects **71 by** storing/retrieving the virtual objects **71** in/from memory, obtaining the virtual objects **71** from memory, creating the virtual objects **71** pre-operatively, creating the virtual objects **71** intra operatively, or the like.

[0080] The manipulator controller **26** and/or the navigation controller **36** track the state of the tool 20 relative to the virtual objects **71.** In one example, the state of the TCP is measured relative to the virtual objects **71** for purposes of determining forces to be applied to a virtual rigid body model via a virtual simulation. This determination can be made, in one

example, so that the tool 20 remains in a desired positional relationship to the virtual objects **71** (e.g., not moved beyond them). The results of the virtual simulation are commanded to the manipulator 14. The control system **60** controls/positions the manipulator 14 in a manner that emulates the way a physical handpiece would respond in the presence of physical boundaries/barriers. The boundary generator **66** may be implemented on the manipulator controller **26.** Alternatively, the boundary generator **66** may be implemented on other components, such as the navigation controller **36.**

[0081] Referring to **FIG. 3,** a path generator **68** can be another software program or module run **by** the control system **60.** In one example, the path generator **68** is run **by** the manipulator controller **26** and generates path data **73.** The path data **73** may include a tool path TP along which the manipulator 14 moves a tool 20 to interact with the anatomical volume AV. For example, the tool 20 may traverse the tool path TP to remove sections of the anatomical volume AV to prepare the anatomical volume AV for receiving an implant. The tool path TP may comprise a plurality of path segments **PS,** or may comprise a single path segment **PS.** The path segments **PS** may be straight segments, curved segments, combinations thereof, or the like. The tool path TP may also be defined with respect to the anatomical model AM. The tool path TP may be predetermined based on a geometry of an implant model selected for the anatomical model AM and/or a planned resection volume of the anatomical model AM. In other words, the tool path TP may be implant-specific, e.g., defined based on a size, shape, volume, etc. of an implant, and/or patient-specific, e.g., defined based on the patient's anatomy. In some instances, the path data **73** may include a set of potential tool paths TP, which are evaluated to determine which tool path TP optimizes cutting performance.

[0082] In some instances, the path data **73** may also include a predefined pose of the shaft **33** of the tool 20. For example, the predefined pose of the shaft **33** may include a state (e.g., a position and/or orientation) of the shaft **33** with respect to the manipulator coordinate system **MNPL.** As previously stated, the manipulator 14 could employ the joint/motor encoders, or any other non-encoder position sensing method, to enable a pose of the shaft **33** to be determined. As such, the predefined pose may also be provided in terms of a sensed reading of the joint/motor encoders, or any other non-encoder position sensing method. Therefore, the path data **73** may include not only the tool path TP, but may also include predefined poses of the shaft **33** along the tool path TP. For instance, the path data **73** may include a predefined pose of the shaft **33** corresponding to a path segment **PS** of the tool path TP.

[0083] In one version described herein, the tool path TP is defined as a tissue removal path, but, in other versions, the tool path TP may be used for treatment other than tissue removal. One example of the tissue removal path described herein comprises a milling path **72.** It should be understood that the term "milling path" generally refers to the path of the tool 20 in the vicinity of the target site for milling the anatomy and is not intended to require that the tool 20 be operably milling the anatomy throughout the entire duration of the path. For instance, the milling path **72** may comprise sections or segments where the tool 20 transitions from one location to another without milling. Additionally, other forms of tissue removal along the milling path **72** may be employed, such as tissue ablation, and the like. The milling path **72** may be a predefined path that is created pre-operatively, intra-operatively, or combinations thereof. In other words, the milling path **72** may be defined before the surgical procedure begins, during the surgical procedure (including during tissue removal), or combinations thereof. In any case, the control system **60** obtains the milling path **72 by** storing/retrieving the milling path **72** in/from memory, obtaining the milling path **72** from memory, creating the milling path **72** pre-operatively, creating the milling path **72** intra-operatively, or the like. The milling path **72** may have any suitable shape, or combinations of shapes, such as circular, helical/corkscrew, linear, curvilinear, combinations thereof, and the like.

[0084] One example of a system and method for generating the virtual objects **71** and/or the milling path **72** is described in **U.S.** Patent No. *9,119,655,* entitled "Surgical Manipulator Capable of Controlling a Surgical Instrument in Multiple Modes," the disclosure of which is hereby incorporated **by** reference. In some examples, the virtual objects **71** and/or milling paths **72** may be generated offline rather than on the manipulator controller **26** or navigation controller **36.** Thereafter, the virtual objects **71** and/or milling paths **72** may be utilized at runtime **by** the manipulator controller **26.**

[0085] A path interpolator **86,** as shown in **FIG. 3,** can be a sub-module of the path generator **68.** Path interpolator **86** determines target positions for a coordinate system of the energy applicator 24 along the tool path TP. The pose of the shaft **33** is fixed relative to the coordinate system of the energy applicator 24. Referring to **FIG.** *5,* these target positions are points P along the tool path TP which the energy applicator 24 will successively pass to perform the task. In one implementation, the path segments **PS** of the tool path TP are defined between subsequent points P. Inputs into the path interpolator **86** can include but are not limited to: the data defining the origin and terminus of a path segment **PS;** the data indicating if the path segment **PS** is straight or curved and, if curved, the characteristics of the curve. Another input into the path interpolator **86** is a feed rate, which will be described in greater detail in the

subsequent section. This is a predetermined rate (speed or velocity) at which the energy applicator 24 is set to travel along the path segment **PS.** Based on the above input variables, the path interpolator **86,** in one implementation, can determine the target positions of the energy applicator 24 according to the following steps: **1)** The origin of the coordinate system of energy applicator 24 is assumed to be at an initial position. The initial position is a position along the path segment **PS** over which the energy applicator 24 should travel. **If** the energy applicator 24 is at the beginning point P of the path segment **PS,** this point P is the initial position of the coordinate system of energy applicator 24. Both the initial position and the target position are points P in the bone coordinate system. 2) Based on the feed rate, the distance along which the energy applicator 24 would travel along the path segment **PS** in a single time frame is calculated. In some versions, the period of a time frame is **0.1** to 2 milliseconds. **3)** Based on the initial position, the length of the calculated distance and the location of the segment terminus, the path interpolator **86** generates data defining the target position. **A** further variable that can be used to determine target positions are data from the tool path generator describing the characteristics of the path segment **PS:** straight or curved; and, if curved, the radius of curvature. 4) Steps 1 through **3** are repeated until it is determined that the coordinate system has reached the terminus of the path segment. After the calculation of the first target position spaced from the segment origin, the target position calculated in each frame is employed as the initial position upon which the calculation of the next frame's target position is based. **5)** Once the target position equals the terminus position for a path segment **PS,** the path interpolator **86** repeats steps 1 through 4 to generate a set of target positions that are located along the new segment. During the time period of a single frame, the distance the energy applicator 24 can travel may be greater than the distance to the terminus position for the current segment. **If** the path interpolator **86** determines that the energy applicator 24 would be in this state, the path interpolator **86,** for a time point starting when it is determined that the energy applicator 24 would be at the terminus of the current path segment **PS,** generates data indicating where the energy applicator 24 should be located at along the next path segment **PS** at the end of that frame. The techniques described herein are not exclusively limited to this method for determining target positions.

[0086] Referring to **FIG. 3,** the software employed **by** the control system **60** may further utilize tool data **69.** The tool data **69** includes geometry of the tool 20 that will interact with the tool path TP. For example, the tool data **69** may include a **3-D** geometry, such as a **3 D** model of the energy applicator 24 of the tool 20, to specify a shape of a cutting surface of the tool 20. For instance, the **3-D** geometry may specify that the cutting surface of the energy

applicator 24 of the tool 20 includes a circular cross-sectional area, a triangular cross-sectional area, a flat cross-sectional area, or a tapered cross-sectional area. The **3-D** geometry may include slices of the energy applicator 24 extracted from the **3-D** model or any other source. In some instances, the tool data **69** may include a shape of the cutting surface, size, surface area, volume, and/or dimensions of the energy applicator 24. The tool data **69** may also include a preferred use of the tool 20. For example, in some instances, the cutting surface of the energy applicator 24 may be positioned at a side of the energy applicator 24 to promote cutting using sides of the energy applicator 24, instead of a tip of the energy applicator 24. The tool data **69** may also include a preferred cutting depth corresponding to a particular tool 20. For example, a particular tool 20 may be used to perform a very shallower cut, whereas another tool 20 may be used to perform a deeper cut. The tool data **69** may also include a shaft **33** of the tool 20. The tool data **69** can be obtained from tool parameters, specifications, or calibration data and/or pre-operatively measured.

[0087] Referring to **FIG. 3,** another software program or module run **by** the control system **60** may be a behavior controller 74. Behavior control is the process of computing data that indicates the next commanded position **CP** of the energy applicator 24 and/or orientation (e.g., pose) for the shaft **33** of the tool 20. In some cases, the position of the TCP is output from the behavior controller 74, while in other cases, the position and orientation of the tool 20 is output. Output from the boundary generator **66,** the path generator **68,** and a force/torque sensor **S** may feed as inputs into the behavior controller 74 to determine the next commanded position **CP** for the energy applicator 24 and/or orientation for the tool 20. The behavior controller 74 may process these inputs, along with one or more virtual constraints, to determine the commanded pose.

[0088] Referring to **FIG. 3,** yet another software program or module run **by** the control system **60** may be a motion controller **76.** One aspect of motion control is the control of the manipulator 14. The motion controller **76** receives data defining the next commanded pose from the behavior controller 74. Based on these data, the motion controller **76** can determine the next position of the joint angles of the joints **J** of the manipulator 14 (e.g., via inverse kinematics and Jacobian calculators) so that the manipulator 14 is able to position the tool 20 as commanded **by** the behavior controller 74, e.g., at the commanded pose. In other words, the motion controller **76** processes the commanded pose, which may be defined in Cartesian space, into joint angles of the manipulator 14, so that the manipulator controller **26** can command the joint motors **27** accordingly, to move the joints **J** of the manipulator 14 to commanded joint angles corresponding to the commanded pose of the tool 20. In one version,

the motion controller **76** regulates the joint angle of the joints **J** and adjusts the torque that joint motors **27** output to, as closely as possible, ensure that the joint motor **27** drives the associated joint **J** to the commanded joint angle.

[0089] Any of the boundary generator **66,** path generator **68,** behavior controller 74, motion controller **76,** and feed rate generator **67** (to be described later) may be sub-sets of a software program **78** or software programs that operate separately and/or independently in any combination thereof. The term "software program" is used herein to describe the computer executable instructions that are configured to carry out the various capabilities of the technical solutions described. For simplicity, the term "software program" is intended to encompass, at least, any one or more of the boundary generator **66,** path generator **68,** behavior controller 74, motion controller **76,** and/or feed rate generator **82.** The software program **78** can be implemented on the manipulator controller **26,** navigation controller **36,** or any combination thereof, or may be implemented in any suitable manner **by** the control system **60.**

[0090] A clinical application **80** may be provided to handle user interaction. The clinical application **80** can handle many aspects of user interaction and coordinates the surgical workflow, including pre-operative planning, implant placement, registration, bone preparation visualization, feed-rate parameter adjustment or confirmation, and post-operative evaluation of implant fit, etc. The clinical application **80** is configured to output to one or more of the displays **38.** The clinical application **80** may run on its own separate processor or may run alongside the navigation controller **36.** In one example, the clinical application **80** interfaces with the boundary generator **66** and/or path generator **68** after implant placement is set **by** the user, and then sends the virtual object **71** and/or tool path TP returned **by** the boundary generator **66** and/or path generator **68** to the manipulator controller **26** for execution.

[0091] The system **10** may operate in a force-input or manual mode, such as described in **U.S.** Patent No. *9,119,655,* incorporated herein **by** reference. Here, the user applies a force to the manipulator 14, and in response, the manipulator 14 executes movement of the tool 20 and its energy applicator 24 at the surgical site. In one example, the user physically contacts the tool 20 to cause movement of the tool 20 in the manual mode. In one version, the manipulator 14 monitors forces and torques placed on the tool 20 **by** the user in order to position the tool 20. For example, the manipulator 14 may comprise the force/torque sensor **S** that detects the forces and torques applied **by** the user and generates corresponding input used **by** the control system **60** (e.g., one or more corresponding input/output signals).

[0092] The manipulator controller **26** and/or the navigation controller **36** receives the input (e.g., signals) from the force/torque sensor **S.** In response to the user-applied forces

and torques, the manipulator 14 moves the tool 20 in a manner that emulates the movement that would have occurred based on the forces and torques applied **by** the user. Movement of the tool 20 in the manual mode may also be constrained in relation to the virtual objects **71** generated **by** the boundary generator **66.** In some versions, measurements taken **by** the force/torque sensor **S** are transformed from a force/torque coordinate system FT of the force/torque sensor **S** to another coordinate system, such as a virtual mass coordinate system in which a virtual simulation is carried out on the virtual rigid body model of the tool 20 so that the forces and torques can be virtually applied to the virtual rigid body in the virtual simulation to ultimately determine how those forces and torques (among other inputs) would affect movement of the virtual rigid body.

[0093] The system **10** may also operate in a semi-autonomous mode in which the manipulator 14 moves the tool 20 along the tool path TP in an automated manner. An example of operation in the semi-autonomous mode is also described in **U.S.** Patent No. *9,119,655,* incorporated herein **by** reference. In some embodiments, when the manipulator 14 operates in the semi-autonomous mode, the manipulator 14 can move the tool 20 free of user applied force such that a user does not physically contact the tool 20 to move the tool 20. Instead, the user may use some form of remote control or switch to control starting and stopping of automated movement. For example, the user may hold down a button of the remote control to start movement of the tool 20 and release the button to stop movement of the tool 20, as also described in **U.S.** Patent No. *9,119,655.*

[0094] II. Determining the Feed Rate

[0095] The speed or velocity at which the energy applicator 24 advances is referred to as the feed rate. In one implementation, the energy applicator 24 may advance along the tool path TP at one or more feed rates. More specifically, such advancement can occur during operation of the manipulator 14 in the semi-autonomous mode. In one implementation, this section describes techniques in which the feed rate is determined based on an interaction between the tool path TP and the anatomical model AM in order to generate cut plan data **79** (shown in **FIG. 6** and explained herein). The feed rate computation techniques described herein can be augmented **by** the feed rate techniques described in incorporated **U.S.** Patent No. *9,119,655.*

[0096] Referring to **FIG. 3,** the software employed **by** the control system **60** can include a feed rate generator **82.** The feed rate generator **82** determines the feed rate, or feed rate factors, at which the energy applicator 24 should move as it travels along one or more individual path segments **PS** of the tool path TP (see **FIG.** *5)* to optimize cutting performance.

The feed rate factor can be a scalar value. In practice, the manipulator controller **26** may be provided with plural feed rate factors. These feed rate factors can be used to set default feed rates and/or can be scaled or modified according to variables, as described below. The feed rate factors need not always correspond to the actual feed rate **by** which the energy applicator 24 is advanced.

[0097] The feed rate generator **82** can determine the feed rate(s) or feed rate factors and associate such with the tool path TP. The feed rate generator **82** can do so pre-operatively and/or intraoperatively. In some examples, the feed rate generator **82** does so pre-operatively, and the surgeon can modify or adjust the output of the feed rate generator **82** at a later time, using, e.g., the clinical application **80.**

[0098] The generator **82** is not intended to be limited exclusively to feed rate. To the extent that tool operating parameters other than feed rate are generated, the generator **82** can be identified using any suitable terminology, such as tool parameter generator **82,** tool operating parameter generator **82,** and the like.

[0099] i. Cut Plan Data Overview

[00100] The control system **60,** using the feed rate generator **82** can generate or output cut plan data **79.** The cut plan data **79** can be understood as the planned tool path TP, path segments **PS,** and optionally, planned feed rates or feed rate factors for the tool that are associated with the tool path TP or path segments. An example illustration of the cut plan data **79** is shown in **FIG. 6.** As shown, the cut plan data **79** includes a planned feed rate factor FR1...FRN assigned to each path segment **PS1...PSN** of the tool path TP. The feed rate generator **82** is configured to determine the planned feed rate factor FRI...FRN assigned to each path segment **PSI...PSN** based on simulating an interaction between the anatomical model AM and a tool 20 at a point **P1...PN.** The cut plan data **79** can include any other parameters (such as tool operating parameters) that relate to how the tool and/or manipulator 14 can be controlled to cut the anatomy. These parameters can include, but are not limited to, virtual object **71,** stiffness/damping parameters of the tool or mesh, cutting speed, cutting depth, number of tool passes or tool segments, cutting force, tissue temperature, and the like.

[00101] One example of the cut plan data **79** and tool path TP are illustrated in **FIG. 6** with respect to an example involving an acetabulum. The cut plan data **79** and the tool path TP may vary from what is illustrated. For example, the tool path TP may include a greater or lesser number of points P and path segments **PS.** As another example, the cut plan data **79** may include a greater or lesser number of planned feed rate factors FRI...FRN. The tool path TP may also be different from what is shown depending on the region of the anatomy or implant.

[00102] Referring to **FIG. 6,** the one or more controllers, including but not limited to the manipulator controller **26,** including the path generator **68** and feed rate generator **82,** are configured to control the manipulator 14 to advance the energy applicator 24 of the tool 20 to a plurality of commanded positions **CP-CPN** according to the cut plan data **79.** The commanded positions **CP** are often, but not necessarily, defined with respect to points P along the tool path TP in the semi-autonomous mode. Alternatively, the commanded positions **CP** may be determined pursuant to user-initiated motion that is emulated **by** the system **10** in the manual mode.

[00103] ii. Method of Generating Cut Plan Data

[00104] In this subsection, a method of generating cut plan data **79** based on simulating an interaction between the tool path TP and the anatomical model AM will be described.

[00105] a. Obtaining the Anatomical Data, the Path Data, and the Tool Data

[00106] An example of the method for generating cut plan data **79** is shown in **FIG.** 4. In this implementation, the method for generating cut plan data **79** includes a step M1 of obtaining the anatomical data *65,* the path data **73,** and the tool data **69.** This information is obtained **by** the control system **60,** and more specifically, the feed rate generator **82.** Referring to **FIG. 3,** the feed rate generator **82** is shown as being in communication with the path generator **68** (for receiving the path data **73),** as well as a source (e.g., memory) that includes the anatomical data **65** and tool data **69.** The anatomical data *65,* the path data **73,** and the tool data **69** serve as inputs to the feed rate generator **82.**

[00107] b. Merging the Anatomical Data and the Path Data

[00108] Referring to **FIG.** 4, the method includes a step M2 of merging the path data **73** and the anatomical data *65.* After obtaining the anatomical data **65** and the path data **73** during step M1, the control system **60,** or feed rate generator **82,** processes the data **by** merging the data into a common coordinate system. The step M2 of merging the path data **73** and the anatomical data **65** is further shown in one illustrative example in **FIG. 5.** As shown, the path data **73** includes the tool path TP and points P along the tool path TP, the tool path TP and the points P being mapped on a path data coordinate system X_T , Y_T , Z_T . The anatomical data 65 includes the anatomical model AM and density values DV, which are mapped on an anatomical data coordinate system X_A , Y_A , Z_A . In one example, the path data 73 and the anatomical data **65** are merged such that the tool path TP and the anatomical model AM create a merged model 77, which is mapped on a merged coordinate system X_M , Y_M , Z_M .

[00109] The merged coordinate system **Xm, Ym, Zm** may be the anatomical data coordinate system X_A , Y_A , Z_A , the path data coordinate system X_T , Y_T , Z_T , or a new, different, or arbitrary coordinate system. In some instances, the anatomical data **65** may be transformed and superimposed onto the path data 73 such that the path data coordinate system X_T , Y_T , Z_T serves as the merged coordinate system X_M , Y_M , Z_M . For example, the anatomical model AM may be scaled and superimposed onto the path data **73** such that the anatomical model AM is mapped to the path data coordinate system X_T , Y_T , Z_T . Furthermore, the density values DV may be mapped from coordinates in the anatomical data coordinate system X_A , Y_A , Z_A to coordinates in the path data coordinate system X_T , Y_T , Z_T . In other instances, the path data 73 may be transformed and superimposed onto the anatomical data **65** such that the anatomical data coordinate system X_A , Y_A , Z_A serves as the merged coordinate system X_M , Y_M , Z_M . For example, the tool path TP may be scaled and superimposed onto the anatomical data **65** such that the tool path TP is mapped to the anatomical data coordinate system X_A , Y_A , Z_A . Furthermore, points P along the tool TP may be mapped from the path data coordinate system X_T , Y_T , Z_T to the anatomical data coordinate system X_A , Y_A , Z_A . In still other instances, the path data **73** and the anatomical data **65** may both be transformed and superimposed onto one another such that the merged coordinate system X_M , Y_M , Z_M is a new coordinate system. For example, the tool path TP and/or the anatomical model AM may be scaled using different factors such that the tool path TP and the anatomical model AM both may be mapped to a new, merged coordinate system X_M , Y_M , Z_M .

[00110] This merger can, but need not be, provided or performed in visual form. For instance, the merger can be purely computational and unseen to a user. Alternatively, aspects of these steps can be visualized for the user, using e.g., the clinical application **80** so that the user can experience, or interact with the path data **73** and the anatomical data **65.**

[00111] c. Generating the Cut Plan Data

[00112] Once the feed rate generator **82** merges the path data **73** and the anatomical data **65,** the feed rate generator **82** carries out a series of additional steps to generate the cut plan data **79.** These steps will be described in this section. The feed rate generator **82** does so **by** evaluating or simulating an interaction between the tool 20 and the anatomical model AM at individual point(s) P. For example, referring to **FIG. 6,** the feed rate generator **82** generates the cut plan data **79** for the tool path TP relative to path segment(s) **PS1...PSN by** simulating the interaction between the tool 20 and the anatomical model AM at a corresponding point **P1...PN.** For instance, to generate the cut plan data **79** for path segment **PSI,** the feed rate generator **82** simulates the interaction between the tool 20 and the anatomical model AM at

point P1. For simplicity, cut plan data **79** generated **by** the feed rate generator **82** for a path segment **PS** will be referred to herein as cut plan data **79** for a point P. The cut plan data **79** can be the output which includes data related to any number of, or all, path segments **PS** or points P of the tool path TP.

[00113] In one instance, the simulated interaction between the tool 20 and the anatomical model AM may include a simulated intersection **I** between the tool 20 and the anatomical model AM. The feed rate generator **82** may simulate an interaction between the tool 20 and the anatomical model AM and determine whether the tool 20 intersects the anatomical model AM during the simulated interaction. The feed rate generator **82** may then generate the cut plan data **79** based on analyzing the simulated intersection **I** between the tool 20 and the anatomical model AM. Examples of such intersections **I** are shown in **FIGS. 5-7.** Referring to the merged model **77** of **FIG. 5,** the tool 20 may intersect the anatomical model AM at various example intersections **I** as the tool 20 travels along the tool path TP. One such intersection **I** occurs at point PI. Various example intersections **I** are also shown in **FIG. 6** and shown in cross-section in **FIG. 7.** While these figures illustrate example intersections **I** they are not intended to limit the scope of the concept. In other instances, the tool path TP may intersect the anatomical model AM at different locations of the anatomical model AM and may intersect the anatomical model AM at a different number of locations of the anatomical model AM. Details related to the intersection **I** will be described in further below.

[00114] To generate the cut plan data **79** for points P along the tool path TP, the method of **FIG.** 4 can execute a loop ML. In the instance of **FIG.** 4, the loop ML iterates to generate the cut plan data **79** for **N** number of points P (and corresponding path segments **PS)** along the tool path TP in order to generate the cut plan data **79** for the tool path TP. The number of points P can be automatically determined **by** the program or selected **by** a user. The method includes a step M3 of determining whether each of the **N** points P of the tool path TP has been analyzed. At step M3, **N** can be set to any number of points. In some instances, the feed rate generator **82** may iterate through the loop ML for some, but not all, points P of the tool path TP. For example, in some instances, the feed rate generator **82** may iterate through at least one point P along the tool path TP, one or more grouping of points P along the tool path TP, every point P along the tool path TP that is a multiple of n (n being a number greater than **0),** randomly selected points P along the tool path TP, or selected/predetermined points P along the tool path TP. However, in the example shown in **FIG.** 4, this loop ML evaluates whether all points P of the tool path TP have been analyzed. **If** the feed rate generator **82** determines that each point P along the tool path TP has been evaluated, the feed rate generator **82** proceeds to step **M1**

and outputs the cut plan data **79** for the tool path TP. However, if the feed rate generator **82** determines that cut plan data **79** has not been generated for each point P along the tool path TP, the feed rate generator **82** proceeds to step M4 and iterates through the loop ML once more to generate cut plan data **79** for a successive (or remaining) point P along the tool path TP.

[00115] As shown, the loop ML includes steps M4-M1O for generating the cut plan data **79** based on the **N** number of points P along the tool path TP. The steps M4-M1O are evaluated for individual points P. However, the order of these steps M4-M1O need not be executed in the exact order shown, unless a subsequent step relies on a previous step. The loop ML includes a step M4 of identifying a location of a point P on the tool path TP relative to the anatomical data *65;* a step **M5** of loading, from the tool data **69,** the geometry of the tool 20 at the identified location; a step **M6** of identifying an intersection between the geometry of the tool 20 and the anatomical volume AV; a step **M7** of determining density values DV of the anatomical data *65* within the intersection; a step **M8** of computing an intersection ratio related to the geometry of the tool 20 within the intersection relative to the geometry of the tool 20 outside of the intersection; and a step M10 of setting a planned feed rate factor FR for the tool 20 at a path segment **PS** corresponding to the point P based on the determined density values DV and the computed intersection ratio. The step M9 of disregarding previously determined density values DV will be described herein in a separate subsection.

[00116] During step M4, the feed rate generator **82** identifies a location of the point P. Specifically, the feed rate generator **82** identifies the location of the point P relative to the anatomical data *65.* Referring to one example in **FIG. 6,** the feed rate generator **82** may determine that point P1 is located at coordinates (x_{P1}, y_{P1}, z_{P1}) in the merged coordinate system **Xm, Ym, Zm.** The feed rate generator **82** can identify a location of the point P using different methods or using coordinates from any coordinate system.

[00117] During step *M5,* the feed rate generator **82** determines a geometry of the tool 20 at the point P. Specifically, the feed rate generator **82** loads, from the tool data **69,** the geometry of the tool 20 at the point P. As previously stated, the cut plan data **79** considers an intersection **I** between the geometry of the tool 20 and the anatomical volume AV at the point P. To identify the intersection **I** between the geometry of the tool 20 and the anatomical volume AV at the point P, the feed rate generator **82** loads or provides a geometry of the tool 20 at the point P. For example, the feed rate generator **82** may load a **3-D** geometry, such as a **3-D** model, of the energy applicator 24 during step **M5.** The **3-D** geometry may include a **3-D** volume or slices of the energy applicator 24. The feed rate generator **82** may also load

dimensions of the tool 20 (e.g., a radius, diameter, volume, a shape of the cutting surface, or surface area of the energy applicator 24) to determine the geometry of the tool 20.

[00118] The feed rate generator **82** may determine the planned feed rate FR based on the tool data **69.** For example, the feed rate generator **82** may determine the planned feed rate FR based on the geometry of the tool 20. For instance, the cutting surface of the energy applicator 24 may include a tapered cross-sectional area. In such an instance, the feed rate generator **82** may determine the planned feed rate FR to move the tool 20 at a speed to optimize cutting with the tapered cross-sectional area. As another example, the feed rate generator **82** may determine the planned feed rate FR based on a preferred use of the tool 20. For instance, the cutting surface of the energy applicator 24 may be positioned at a side of the energy applicator 24 to promote cutting using sides of the energy applicator 24 with a swift brushing motion. In such an instance, the feed rate generator **82** may determine the planned feed rate FR to move the tool 20 at a speed to perform a swift brushing motion with the tool 20. As yet another example, the feed rate generator **82** may determine the planned feed rate FR based on a preferred cutting depth of the tool 20. For instance, the tool 20 may be preferably used for shallower cuts. In such an instance, the feed rate generator **82** may determine the planned feed rate FR to move the tool 20 to perform a shallower cut. These planned feed rate FR considerations related to the tool data **69** may be accounted for during step **M5** of the method or may be accounted for during any other suitable step of the method.

[00119] At step **M6** and as shown in one example in **FIG. 7,** the feed rate generator **82** identifies the intersection **I** between the geometry of the tool 20 and the anatomical volume AV at a point P1. In this example, the energy applicator 24 is a spherical cutting bur. The geometry that is compared to the anatomical volume AV is a circular cross-section of the energy applicator 24. Accordingly, the size of the circular cross section and the geometry of the anatomical volume AV will differ from slice to slice. At point P1, for any given slice, some portions of the tool geometry may be included within the intersection I, while other parts of the tool 20 may not be included within the intersection I. To identify the intersection I, the feed rate generator **82** can analyze or sweep through imaged slices of the anatomical volume AV and the tool 20 to identify intersections I.

[00120] In the instance of **FIG. 7,** the feed rate generator **82** analyzes four imaged slices **A,** B, C, **D** relative to corresponding slices of the tool 20. The slices **A,** B, C, **D** are shown for the purposes of illustration. In other instances, the feed rate generator **82** may analyze any suitable number of slices of the anatomical volume AV. Furthermore, the slices

may feature a different view of the anatomical volume AV than shown in **FIG. 7.** Additionally, the geometry of the tool 20 can be different from what is specifically shown.

[00121] In this example, the feed rate generator **82** may identify the **CT** slices for which there is a cross-sectional intersection **I** between the **3-D** geometry of the tool and the anatomical volume AV. Referring to **FIG. 7,** the cross-sectional intersection **I** is indicated using a shaded area. As follows, the feed rate generator **82** may identify that at point P1, slices B, **C,** and **D,** include the intersection I, while slice **A** does not include the intersection I.

[00122] The feed rate generator **82** may identify the intersection **I by** identifying, for each slice **A,** B, **C, D,** a quantity of pixels PX within the intersection I. Referring to **FIG. 7,** the slices **A,** B, **C, D** each include pixels PX. **FIG. 8** provides a more detailed view of slice B, where pixels PX are labeled. For slice B, the feed rate generator **82** may identify that six pixels, pixels PX1-PX6, are located within the cross-sectional intersection I. In some instances, the feed rate generator **82** may alternatively calculate an area of the cross-sectional intersection I, in terms of pixels PX (i.e. the area may be based on a size of a single pixel PX).

[00123] The pixels PX shown in **FIG. 7** (and **FIG. 8,** to be described herein) are shown for illustrative purposes. In other instances, the pixels PX may be larger or smaller in size. Furthermore, the tool 20 and the anatomical volume AV are also shown for illustrative purposes. In other instances, the tool 20 and the anatomical volume AV may include a different shape and/or size.

[00124] The feed rate generator **82** may identify the quantity of pixels PX within the intersection **I** using a variety of methods. In one example, only pixels PX that are entirely located within the intersection **I** are considered, while disregarding partial intersections. In some instances, the feed rate generator **82** may consider pixels PX that are at least partially located within the cross-sectional intersection. For example, the feed rate generator **82** may determine that a pixel PX is located within the cross-sectional intersection **I** if greater than a predetermined percentage of a pixel PX, e.g., *50%,* is located within the cross-sectional intersection I. For example, as shown in **FIG. 8,** the feed rate generator **82** may identify that pixels PX1, PX2, PX5, PX6 are partially located within the cross-sectional intersection I. In another example, a ratio of intersection can be applied to each pixel PX depending on how much of the pixel is within and outside of the intersection.

[00125] In some instances, the feed rate generator **82** may filter any intersecting pixels PX based on a density value DV of a pixel PX. For example, referring to **FIG. 7,** each pixel PX of slices **A,** B, **C, D** includes a corresponding density value DV of the anatomical data *65.* The feed rate generator **82** may evaluate whether the density value DV of the intersecting pixel
PX exceeds or falls below a predetermined threshold. **If** so, the feed rate generator **82** can include or disregard the intersecting pixel PX based on such values.

[00126] The feed rate generator **82** may store the quantity of pixels PX within the intersection **I** for each slice **A,** B, **C, D. FIG. 9** provides a visual representation of the stored quantities. As shown, the quantity of pixels PX within the intersection **I** may be stored in column **81** for each slice **A,** B, **C, D.**

[00127] Any aspect of the techniques described herein that involves using pixels **PX** can be implemented in other ways that do not involve pixels PX. For instance, voxels of the anatomical volume AV may be determined from a **3-D** model of the anatomy and compared to a **3-D** model of the tool geometry at the points P. The voxels can include density values DV. Any other type of **2-D** or **3-D** unit or measurement can be utilized when comparing the geometries described herein.

[00128] During step **M7,** the feed rate generator **82** identifies the density values DV of the anatomical data *65* within the intersection I. The density values DV illustrate a density of the anatomical volume AV at the intersection I. For example, the density values DV allow the feed rate generator **82** to determine how the tool 20 is contacting different types of tissue, such as compact bone tissue, cancellous bone tissue, subchondral bone tissue, fat, and/or cartilage. Additionally, a null or zero value may indicate a region of air. In this way, the cut plan data **79** accounts for a type of tissue contacted at a point P. More particularly, the cut plan data **79** includes a planned feed rate factor FR that accounts for the type of tissue contacted at a point P. The density values DV can be radiodensity values DV measured in Hounsfield Units. However, in other instances, the density values DV may include units other than Hounsfield units **(HU).** For instance, density values DV can be any measure of radiopacity, radiolucency, and/or transradiancy.

[00129] Continuing with the example of **FIG. 7,** the feed rate generator **82** may identify the density values DV of the anatomical data *65* within the intersection **I** for each slice **A,** B, **C, D.** The feed rate generator **82** can disregard any density values for pixels/voxels deemed to be outside of the intersection I. In **FIG. 7,** each pixel PX of anatomical slices **A,** B, **C, D** includes a corresponding radiodensity value DV. Specific, but non-limiting, examples of radiodensity values DV for slice B at point P1 are shown in **FIG. 8,** for example. As shown, the intersection **I** includes pixels PX1-PX6, and the feed rate generator **82** identifies radiodensity values DV *795* **HU, 780 HU,** *785* **HU, 790 HU,** *795* **HU,** and **801 HU,** respectively. The feed rate generator **82** may similarly determine the density values DV of the anatomical data *65* within the intersection **I** for the other slices **C, D.**

[00130] Once the feed rate generator **82** identifies the density values DV within the intersection **I** for each slice **A,** B, **C, D,** the feed rate generator **82** collects the density values DV. The feed rate generator **82** may collect the density values DV **by** computing or determining one or more of: an average, a median, range, mode, a maximum, or a minimum density value DV of the density values DV for each slice **A,** B, **C, D.** For example, in the instance of **FIG. 8,** pixels PX1-PX6 of slice B have an average radiodensity value DV of **791** Hounsfield units **(HU).** The feed rate generator **82** may then store the average radiodensity value DV of pixels PX1-PX6 in memory, as shown in column **83** of **FIG. 9.** The feed rate generator **82** may similarly collect and store the density values DV within the intersection **I** for slices **C, D.**

[00131] During step **M8,** the feed rate generator **82** can compute a tool contact factor that relates to an extent to which the tool contacts the anatomical volume AV at the identified point. For example, the tool contact factor can expose whether the tool 20, at the given point, brushes against or grazes the anatomical volume AV or whether the tool 20 burrs into the anatomical volume AV or is performing any air cutting. In this way, the cut plan data **79** accounts for the extent of contact between the tool 20 and the anatomical volume AV at the point P. The cut plan data **79** includes a planned feed rate factor FR that accounts for the extent of the tool contact at a point P.

[00132] In one example, the tool contact factor is an intersection ratio related to the geometry of the tool 20 within the intersection **I** relative to the geometry of the tool 20 outside of the intersection **I** at a point P. As will be described herein, the intersection ratio may be determined based on the quantity of pixels within the intersection **I** for each slice **A,** B, C, **D.** However, in other instances, the intersection ratio may be determined using any other suitable method.

[00133] The feed rate generator **82** may determine the intersection ratio **by** determining individual intersection ratios for each slice **A,** B, C, **D.** The feed rate generator **82** computes the individual intersection ratios **by** computing a ratio between a first quantity of the geometry of the tool 20 that is located within the intersection **I** and a second quantity of the geometry of the tool that is located beyond the intersection for each slice **A,** B, C, **D.** For example, the feed rate generator **82** may compute the intersection ratios based on a quantity of pixels PX of the tool 20 located within the intersection **I** and a quantity of pixels PX of the tool 20 located beyond the intersection I. In other instances, the feed rate generator **82** may compute the intersection ratios based on a quantity of pixels PX of the tool 20 located within the intersection **I** and a total number of pixels PX of the tool 20.

[00134] Referring to the example of Slice B in **FIG. 8,** the feed rate generator **82** may determine that the energy applicator 24 at this slice occupies or intersects twenty-six total pixels, with six pixels located within the intersection **I** and twenty pixels located beyond the intersection. As such, the feed rate generator **82** may calculate the intersection ratio for slice B to be **(6/26)** or **0.2308.** Other ways of computing similar ratios are contemplated and need not necessarily be a ratio of intersecting pixels/total pixels of the tool 20. The feed rate generator **82** may then store the intersection ratio for slice B in column **85** of **FIG. 9.** The feed rate generator **82** may similarly determine and store the intersection ratio for slices **C, D.** In another example, the intersection ratio is based on voxel intersection in the same manner described with respect to pixels.

[00135] The tool contact factor can alternatively or additionally be based on other computations. For example, the feed rate generator **82** can evaluate the surface, circumference, perimeter, outline, or **2-D** or **3-D** boundary of the tool geometry relative to the anatomical volume. For example, the feed rate generator **82** can determine in **FIG. 8** what amount of the circumference of the tool geometry is passing through or touching the anatomical volume AV as compared with air. This amount can be a length (e.g., arc length), degree measurement, or ratio of the geometrical boundary. Alternatively, an area or volume of the tool geometry can be evaluated relative to the anatomical volume AV, with or without regard to any pixels/voxels. The feed rate generator **82** can supplement a geometrical approach to evaluating the tool contact **by** evaluating or comparing a hardness of the tool relative to density values DV of the anatomical volume AV. This tool hardness evaluation can be used to determine individual contact forces that may be applied to each pixel/voxel.

[00136] During step M10, the feed rate generator **82** sets a planned feed rate factor FR for the tool 20 at a path segment **PS** corresponding to the point P based on the determined density values DV and the computed tool contact factor. In some instances, it is contemplated that the feed rate generator **82** can set the planned feed rate factor FR for the tool 20 based on the computed tool contact factor, without regard to the determined density values DV. During step M10, the feed rate generator **82** may optionally calculate a bone mineral density (BMD) factor based on the determined density values DV and the computed tool contact factor. The feed rate generator **82** then sets the planned feed rate factor for the tool based on the calculated BMD factor.

[00137] The feed rate generator **82** may calculate the BMD factor **by** multiplying the radiodensity values DV collected for each intersection slice during step **M7 by** the tool contact factor calculated for each intersection slice during step **M8.** To calculate the BMD factor in

this way, the feed rate generator **82** converts the radiodensity values DV that were previously collected for each intersection slice during step **M7.** Referring to **FIG. 9,** the feed rate generator **82** converts the radiodensity values DV **by** calculating a maximum of the collected radiodensity values DV **(805 HU).** In other instances, the feed rate generator **82** may convert the radiodensity values DV using an average, median, and/or minimum radiodensity value DV. The feed rate generator **82** also converts the tool contact factors that were previously calculated for each slice during step **M8.** Referring to the example of **FIG. 9,** the feed rate generator **82** can convert the tool contact factors **by** calculating an average of the intersection ratios **(0.7436).** In other instances, the feed rate generator **82** may convert the radiodensity values DV using a median, maximum, and/or minimum radiodensity value DV. As follows, the feed rate generator **82** calculates the BMD factor to be **598.598.**

[00138] In some instances, the BMD factor is utilized as a standardization factor to account for variable density values DV, whether such density values are normalized or raw density values. For example, based on the density values DV, the BMD factor may be chosen from a standardized scale between 1 and **100.** The standardized scale may take into account different normalization factors depending on, e.g., the imaging modality, the scanner used to image the anatomical volume, parameters of a density phantom, or measured forces on the tool, as described above.

[00139] The feed rate generator **82** may access a look-up table to determine the planned feed rate factor FR based on the calculated BMD. Specifically, the feed rate generator **82** may access a look-up table defining associations between predefined BMD factors and predefined feed rate factors FR. An example look-up table is shown in **FIG. 10.** The feed rate generator **82** identifies, in the look-up table, the predefined BMD factor that is closest to the calculated BMD factor and sets the planned feed rate factor FR based on the predefined feed rate factor associated with the closest identified predefined BMD factor. In the example of **FIG. 9,** the feed rate generator **82** calculates the BMD factor to be **598.598.** As such, the feed rate generator **82** may determine that the predefined BMD factor of **600** is closest to **598.598.** The feed rate generator **82** may then set the planning feed rate factor FR for the path segment **PSI** to be **90** mm/sec.

[00140] The look-up table shown in **FIG. 10** serves as an example look-up table. In other instances, the planned feed rate factors FR and the BMD factors may vary based on a preference for optimizing cutting performance. For example, in instances where the control system **60** is more or less sensitive to variations in the density values DV of the anatomical volume AV, a difference between successive BMD factors in the look-up table may be reduced

or increased. As another example, in instances where the control system **60** reduces or increases variations in the planned feed rate factor FR, a difference between successive planned feed rate factors FR may be reduced or increased. Furthermore, while the look-up table in **FIG. 10** features evenly spaced BMD factors (from **100** to **1000),** in some instances, the look-up table may include additional BMD factors and corresponding planned feed rate factors FR around a predetermined range (e.g., *505, 510, 515, 520,* etc.) to increase a resolution of determining a planned feed rate factor FR around the predetermined range of BMD factors.

[00141] In some instances, the feed rate generator **82** may set the planning feed rate factor FR for a path segment **PS** to be a maximum feed rate factor in response to determining that the calculated BMD factor is below a minimum threshold. For example, referring to the look-up table of **FIG. 10,** the feed rate generator **82** may set the planning feed rate factor FR to be **5** mm/sec (a minimum feed rate of the tool 20) if the BMD factor is less than **100.** In some instances, setting the planned feed rate factor to be a minimum feed rate factor in response to determining that the calculated BMD factor is above a maximum threshold. For example, referring to the look-up table of **FIG. 10,** the feed rate generator **82** may set the planning feed rate factor FR to be 400 mm/sec (a maximum feed rate of the tool 20) if the BMD factor is greater than **1000.** In practice, the feed rate FR of the tool 20 is typically between **5** and 400 mm/sec. However, the feed rates FR can be greater or less than this range depending on the situation.

[00142] In some instances, the feed rate generator **82** may obtain a default planned feed rate factor FR for each path segment **PS.** For example, the feed rate generator **82** may, after obtaining the path data **73** during step M1, set a default planned feed rate factor FR for each path segment **PS** of the tool path TP. During step **M8,** the feed rate generator **82** may modify the default feed rate FR for a path segment **PS** based on the calculated BMD factor. For example, referring to **FIG. 10,** the feed rate generator **82** may obtain a default planned feed rate factor FR of **90** mm/sec for each path segment **PS** along a tool path TP. The feed rate generator **82** may then modify the default planned feed rate FR from **90** mm/sec to a different planned feed rate (e.g., **80** mm/sec, **100** mm/sec) based on the calculated BMD factor. In this way, the feed rate generator **82** may retain the default planned feed rate FR for some path segments **PS** of the tool path TP. The look-up table of **FIG. 10** may vary based on a desirability of the user to modify the planned feed rate FR from the default planned feed rate FR. For example, in instances where the user prefers to leave the planned feed rate FR as the default planned feed rate FR, a difference between successive BMD factors may be increased. In such instances, additional BMD factors may be set to correspond to the default planned feed rate

FR. In instances where the user prefers to modify the planned feed rate FR from the default planned feed rate FR, a difference between successive BMD factors may be reduced. In such instances, a number of BMD factors corresponding to default planned feed rate FR may be reduced.

[00143] d. Disregarding Previously Analyzed Anatomical Regions

[00144] During step M9, the feed rate generator **82** is optionally configured to disregard portions (pixels/voxels/areas/volume) of the anatomical volume VM that were previously evaluated during the process shown in **FIG.** 4. The purpose of this step is to consider/disregard these previously analyzed regions on the presumption that these previous regions would have been removed **by** the tool 20 along the tool path TP. Disregarding the density values of previously removed parts of the anatomical volume AV helps generate more accurate feed rate FR determinations for the current point. This approach is useful, for example, when a distance between successive points P along the tool path TP is smaller than a size of the tool 20 or when the tool path TP passes through the same anatomical region twice. In such instances, the feed rate generator **82** need not factor in the density values DV corresponding to the previously removed parts of the anatomical volume AV.

[00145] FIG. 11 illustrates an example instance of step M9. **FIG.** 11 includes a slice of the tool geometry and an imaged slice of the anatomical volume AV when the tool 20 is at a first point P1 and at a successive second point P2 along the tool path TP. The tool 20 at the first point P1 is indicated using a solid line and the tool 20 at the second point P2 is indicated using a dotted line. The tool 20 is shown intersecting the anatomical model AM at the first point P1 at intersection Il and shown intersecting the anatomical model AM at the second point P2 at intersection 12.

[00146] As shown, the respective intersections **I1,** 12 of the tool 20 and the anatomical volume AV at points P1 and P2 include common pixels PX. These common pixels PX illustrate that, at point P2, the tool 20 is expected to intersect a part of the anatomical volume AV that was previously removed **by** the tool 20 when the tool 20 was at point P1. As such, the feed rate generator **82** is configured to disregard the common pixels PX when determining the cut plan data **79** for point P2.

[00147] In the instance of **FIG. 11,** the feed rate generator **82** first generates and stores the pixels PX corresponding to intersection Il for point P1. These pixels PX indicate locations of the intersection Il and are referred to herein as "interaction coordinates". The feed rate generator **82** can also store density values DV corresponding to the interaction coordinates. These determined density values DV of the intersection **I1** will be referred to herein as

"previously determined density values DV". These interaction coordinates need not be specifically limited to the specific coordinates of pixels/voxels. Instead, any technique described above in relation to the tool contact factor can be similarly utilized to determine previous interaction of the tool 20 with the anatomical volume AV. Also, the coordinates can be identified relative to a coordinate system (with or without regard to pixel/voxel location), using the tool path TP coordinate system, anatomical coordinate system, or the merged coordinate system.

[00148] Continuing with the example of **FIG. 11,** the feed rate generator **82** has proceeded through steps M4-M8 for the second point P2. During step M9, the feed rate generator **82** disregards the previously determined interaction coordinates. To do this, the feed rate generator **82** first compares interaction coordinates (e.g., pixels PX) for the second point P2 to the interaction coordinates for the first point P1. The feed rate generator **82** may then disregard any density values DV of the second point P2 that have interaction coordinates identical to the interaction coordinates of the first point P1. In **FIG. 11,** these common interaction coordinates of intersections I1 and I2 include pixels PXA-PXF. As such, the feed rate generator **82** disregards the density values DV associated with pixels PXA-PXF when determining the cut plan data **79** for the second point P2. Disregarding such values can mean that the feed rate generator **82** nullifies or zeroes out these the density values at such coordinates. Furthermore, although the points P1, P2 evaluated in the context of this process were successive points, P2 could be any point subsequent in time to P1, and not necessarily immediately successive to P1.

[00149] In some instances, the feed rate generator **82** may be configured to disregard a previously determined density value DV depending on the amount of prior pixel/voxel interaction with the tool geometry. For example, the feed rate generator **82** may be configured to disregard a previously determined density value DV if more than X% of the pixel PX corresponding to the previously determined density value DV was previously interacted with. For example, referring to **FIG. 11,** pixel PXC may not be disregarded because less than *50%* of pixel PXC was interacted with **by** the tool 20 at the first point P1. However, pixels PXA, PXB, PXD, PXE, PXF may be disregarded because greater than *50%* of pixels PXA, PXB, PXD, PXE, PXF were interacted with **by** the tool 20 at the first point P1. In another instance, the feed rate generator **82** may be configured to disregard a previously determined density value DV only if **100%** of the pixel PX associated with the previously determined density value DV was interacted with. For example, referring to **FIG. 11,** pixels PXA, PXC, PXE, PXF may not be disregarded because less than **100%** of pixels PXA, PXC, PXE, PXF were interacted with

by the tool geometry at the first point P1. However, pixels PXB, PXD may be disregarded because **100%** of pixels PXB, PXD were interacted with **by** the tool geometry at the first point P1. In other examples, the tool contact factor can be considered for purposes of determining whether or not to disregard prior interaction coordinates.

[00150] In other instances, instead of disregarding density values DV at previous interaction coordinates, the feed rate generator **82** may be configured to use a scaled version or residue of the previously determined density value DV. The scaled previously determined density value DV may be based on a measure of the previous interaction. For example, referring to **FIG. 11,** the tool geometry interacted with approximately **25%** of pixel PXC at point P1. As such, instead of disregarding pixel PXC from the determination of the cut plan data **79** for point P2, the feed rate generator **82** may scale the density value DV corresponding to pixel PXC based on the interaction at point P1. For example, the feed rate generator **82** may determine the cut plan data **79** for point P2 using **75%** of the density value DV corresponding to pixel PXC **(606 HU).**

[00151] e. Outputting the Cut Plan Data

[00152] During step **M11,** the feed rate generator **82** outputs the cut plan data **79** for the tool path TP. Referring to **FIG. 3,** the feed rate generator **82** may output the cut plan data **79** to the behavior controller 74. The behavior controller 74 may then control the motion controller **76** based on the cut plan data **79.** In this way, the control system **60** controls the manipulator 14 to move the tool 20 along the tool path TP at the planned feed rates FR based on the cut plan data **79.** Additionally, referring to **FIG. 3,** the cut plan data **79** may be output to the clinical application **80.** As such, a user operating the clinical application **80** may view the cut plan data **79** prior to performing or during a surgical procedure. Furthermore, a user operating the clinical application **80** may adjust the cut plan data **79** prior to performing or during a surgical procedure.

[00153] As shown in **FIG. 6,** the cut plan data **79** includes the tool path TP. However, the cut plan data 79 also includes planned feed rate factors FR1...FRN for path segments **PS1...PSN** along the tool path TP. In this way, the cut plan data **79** may be an enhanced or augmented version of the originally obtained tool path TP. Additionally, in some instances, once the feed rate generator **82** generates the cut plan data **79,** the cut plan data **79** may replace the original tool path TP.

[00154] Furthermore, in some instances, the feed rate generator **82** may evaluate the cut plan data **79** to determine that it is prudent to alter the original tool path TP. Such alteration can be based on evaluating any consideration, factor or step described herein, such as the

planned feed rate factors FR1...FRN, the tool contact factors, disregarded interaction coordinates, etc. For example, the feed rate generator **82** can alter the tool path TP to optimize cutting performance, cut time, and the like. For instance, if the planned feed rate FR at one point is excessively slow or fast, the feed rate generator **82** can alter the tool path TP **by** changing the location of the point or removing the point altogether. In another example, if the tool contact factor at one point is excessively high or low, the feed rate generator **82** can alter the tool path TP **by** changing the location of the point. In another example, if at one point P, the feed rate generator **82** detects an excessive amount of identified previous interaction from a previous point, the feed rate generator **82** can alter the tool path TP **by** changing the location of the point P or the previous point so as to reduce cutting time. In an instance where the path data **73** includes a set of potential tool paths TP, the feed rate generator **82** may determine which of the potential tool paths TP optimizes cutting performance, cut time, and the like. The feed rate generator **82** may then select the determined tool path TP for the cut plan data **79** while disregarding the other tool paths TP.

[00155] The altered tool path TP can be automatically determined and implemented **by** the feed rate generator **82.** Alternatively, the proposed alteration can be presented to the user for confirmation.

[00156] In some instances, cutting of a resection volume during a surgical procedure may be repeated until the control system **60** determines that the resection volume is fully removed. In some instances, the tool 20 may encounter an error such that the tool 20 may not follow the original tool path TP, resulting in the resection volume not being fully removed. In other instances, an altered tool path TP, when followed **by** the tool 20, may not **fully** remove the resection volume. In such instances, cutting of the resection volume may be repeated (e.g., after the error and/or after the tool 20 moves according to the altered tool path TP) **by** restarting the surgical procedure and moving the tool 20 according to the original tool path TP or according to an altered tool path TP. The surgical procedure may be restarted and repeat as many times as necessary until the resection volume is fully removed. In some instances, the user may be notified that the resection volume is not fully removed and may be presented with an option of restarting and repeating the surgical procedure according to the original tool path TP, or according to an altered tool path TP.

[00157] f. Additional Implementations

[00158] In some implementations, the cut plan data **79** may be determined based additionally or alternatively on a tissue parameter. In such implementations, the anatomical data **65** may include a tissue parameter, which may include any tissue parameter data. For

example, the tissue parameter may include density values DV of the anatomical volume AV, and/or may include other tissue parameter data. For example, a type of tissue of the anatomical volume AV may be determined from the tissue parameter data. In such an example, the control system **60** may determine that a tissue of the anatomical volume AV is cancellous, cortical, cortical, cartilage, or soft tissue based on the tissue parameter data. Tissue parameter data can also include an electrical parameter of the tissue, such as permittivity or conductivity. Tissue parameter data can also include blood flow parameter, volume, voxel size, area, pixel size, thickness, cortical thickness, weight, fat fraction, total fat, heat parameters, thermal conductivity, thermal expansion, tensile strength, acoustic parameters, elasticity, bone surface density, bone surface/volume ratio, and the like.

[00159] In some implementations, the cut plan data **79** may be determined based on a predefined pose of the shaft **33.** For example, a predefined pose of the shaft **33** may affect the simulated interaction **I** between the geometry of the tool 20 and the anatomical volume AV at a point P. Specifically, a predefined pose of the shaft **33** may affect how the tool 20 contacts the anatomical volume AV at the intersection **I** depending on the geometry of the tool 20. For example, in an instance where a cutting surface of the energy applicator 24 includes a triangular or tapered cross-section or a flat cutting tip, the predefined pose of the shaft **33** affects the intersection **I** of the tool 20 and the anatomical volume AV. As such, to more accurately identify the intersection **I** during step **M6,** the control system **60** may be configured to obtain the path data **73 by** obtaining a planned pose of the TCP during step M1.

[00160] In some implementations, the cut plan data **79** may include an output pose of the shaft **33** associated with at least one point P of the tool path TP. In such implementations, the control system **60** determines the output pose for the shaft **33** as the energy applicator 24 travels along one or more individual path segments **PS** of the tool path TP to optimize cutting performance. The output pose of the shaft **33** may be a state (e.g., a position and/or orientation) of the shaft **33** with respect to the manipulator coordinate system **MNPL. By** outputting the output pose of the shaft **33,** the control system **60** provides the manipulator controller **26** with instructions for 14 for moving the tool 20.

[00161] The control system **60** may determine the output pose of the shaft **33** based on the anatomical data **65** (e.g., density values DV and/or a tissue parameter), the path data **73,** and the tool data **69.** For example, the control system **60** may determine the output pose based on the geometry of the tool 20. For instance, the cutting surface of the energy applicator 24 may include a tapered cross-sectional area. In such an instance, the control system **60** may determine the output pose to position and orient the tool 20 to optimize cutting with the tapered

cross-sectional area. As another example, the control system **60** may determine the output pose based on a preferred use of the tool 20. For instance, the cutting surface of the energy applicator 24 may be positioned at a side of the energy applicator 24 to promote cutting using sides of the energy applicator 24, instead of a tip of the energy applicator 24. In such an instance, the control system **60** may determine the output pose to position and orient the tool 20 such that the side of the energy applicator 24 performs a majority of the cutting. As yet another example, the control system **60** may determine the output pose based on a preferred cutting depth of the tool 20. For instance, the tool 20 may be preferably used for shallower cuts. In such an instance, the control system **60** may determine the output pose to position and orient the tool 20 to perform a shallower cut.

[00162] The control system **60** may set the output pose of the shaft **33** during step M10 of the above-described method. Furthermore, the control system **60** may output the cut plan data **79,** including the output pose, during step **M11.** Additionally, the control system **60** may execute the above-described steps M1-M9 to determine the output pose. The control system **60** may output the output pose of the shaft **33** in addition to, or as an alternative to, outputting the planned feed rate FR of the tool 20.

[00163] In some implementations, the feed rate generator **82** may determine the planned feed rate FR and/or adjust the cut plan data **79** to achieve a predetermined motor current on a motor of the tool 20. For example, the feed rate generator **82** may determine the planned feed rate FR and/or adjust the cut plan data **79** to maintain a constant motor current on a motor of the tool 20. As another example, the feed rate generator **82** may determine the planned feed rate FR and/or adjust the cut plan data **79** to ensure that a motor current on a motor of the tool 20 is within a predetermined range of motor current values.

[00164] In some implementations, the control system **60** may monitor a performance of the tool 20 during a surgical procedure. Specifically, the control system **60** may monitor a performance of the tool 20 while the tool 20 cuts a resection volume of the anatomical volume AV according to the cut plan data **79.** The control system **60** may monitor a contact force of the tool 20 applied to the anatomical volume AV, a rotational speed of the tool 20, an actual feed rate FR of the tool 20, a temperature of the tool 20, a current of a motor of the tool 20, and/or any other suitable measure of performance of the tool 20. The control system **60** may then modify the cut plan data **79** based on monitoring the performance of the tool 20. For example, the control system **60** may modify the density values DV of the anatomical volume AV, the planned feed rate FR, the tool path TP, the BMD factors, a geometry of the tool 20, and/or any other parameter used in the determination of the cut plan data **79.**

[00165] III. Density Value Parameterized Virtual Object

[00166] With reference to **FIGS.** 12 and **13,** described herein are techniques for the control system **60** to create or modify a virtual object **71** such that the virtual object **71** is characterized **by,** coded with, or otherwise associated with properties, parameter(s) or factors derived from the density values DV. This virtual object **71** can be used **by** the control system **60** to modify an operation of the manipulator 14 or the tool 20 based on the tool interacting with the virtual object **71.**

[00167] As described above, the state of the tool 20, TCP, or energy applicator 24 can be measured relative to the virtual object **71** for purposes of determining forces to be applied to a virtual model of the tool 20 in a virtual simulation. In the virtual simulation, model of the tool 20 can be represented as the virtual rigid body model or virtual volume. Forces are computed with respect to the virtual model in response to the virtual model interacting with one or more polygonal elements **99** of the virtual object **71.** These forces applied to the virtual model result in an output which the control system **60** can use to modify operation of the manipulator 14 or the tool 20. In response, the control system **60** may compute a reactive force to modify an operation of the manipulator 14 **by** preventing the tool 20 from penetrating the virtual object **71.** In response to the interaction, the control system **60** can also modify a feed rate of the tool 20. The techniques evaluating tool interaction with a virtual object **71** can be like that described in **U.S.** Patent Publication No. **2018/0353253,** filed on June **6, 2018,** and entitled "Robotic Surgical System And Method For Producing Reactive Forces To Implement Virtual Boundaries", the entire contents of which are hereby incorporated **by** reference.

[00168] Tool interaction with the virtual object **71,** and the techniques described herein, can occur, or be implemented in any mode of operation for the manipulator 14, including autonomous, manual, or guided-manual modes. The autonomous and manual modes have been described above. In the guided manual mode, the control system **60** obtains the tool path TP for the tool 20 and defines virtual constraints on movement of the tool 20 along the tool path TP with respect to two degrees of freedom each being normal to the tool path TP. In this way, the virtual constraints are defined to constrain movement of the tool 20 to be along the tool path TP. Additionally, in the guided manual mode, the control system **60** receives an input from the force/torque sensor **S** in response to user forces and torques manually applied to the tool 20 **by** a user. The control system **60** then simulates dynamics of the tool 20 in the virtual simulation based on the virtual constraints and the input from the force/torque sensor **S** and commands the manipulator 14 to advance the tool 20 along the tool path TP based on the virtual simulation. For example, the control system **60** may compute and simulate a reactive

force to the virtual object **71** in the virtual simulation and commands the manipulator 14 to advance the tool 20 along the tool path TP based on the virtual simulation. The guided manual mode is further described in **U.S.** Patent Publication No. **2020/0281676,** which is incorporated herein **by** reference.

[00169] According to this technique, the control system **60** obtains the anatomical data **65** and the virtual object data **97** associated with the virtual object **71.** The control system **60** obtains anatomical data **65,** which includes a geometry and density values DV of the anatomical volume AV. The anatomical data **65** is illustrated in **FIG.** 12 as the anatomical model AM of the anatomical volume AV, including density values DV. The anatomical data 65 can be mapped on an anatomical data coordinate system X_A , Y_A , Z_A . The control system **60** also obtains virtual object data, which includes a geometry of the virtual object **71** having a mesh of polygonal elements. The virtual object data **97** is illustrated in **FIG.** 12 includes the virtual object 71, which is mapped on a virtual object coordinate system X_V, Y_V, Z_V . As shown, the virtual object **71** includes a mesh of polygonal elements **99.** In **FIG.** 12, the polygonal elements **99** are triangular. However, in other instances, each individual polygonal element **99** may be any suitable polygon.

[00170] Referring to **FIG.** 12, the control system **60** merges the anatomical data **65** and the virtual object data to create a merged model **101,** which can be mapped on a merged coordinate system X_M , Y_M , Z_M , or any other coordinate system described, such as the anatomical data coordinate system X_A , Y_A , Z_A , the virtual object coordinate system X_V , Y_V , Zv, or a new, different, or arbitrary coordinate system. This merger can, but need not be, provided or performed in visual form. For instance, the merger can be purely computational and unseen to a user. Alternatively, aspects of these steps can be visualized for the user, using e.g., the clinical application **80** so that the user can experience, or interact with the virtual object **71** and the anatomical data **65.**

[00171] FIG. 12 provides two views of the merged model **101:** a first view where the merged model 101 is shown in the X_M , Y_M coordinate system, and a second view where the merged model 101 is shown in the X_M , Z_M coordinate system. In both views, a polygonal element **99** of the virtual object **71** and the anatomical model AM are superimposed.

[00172] For illustrative purposes, the polygonal element **99** shown may be exaggerated relative to the size of the density values DV regions, and hence, not to scale. Deepening on the size of the polygonal elements **99** and density value DV regions, any number of polygonal elements **99** may fit inside one density value DV region, and any number of density value DV regions may fit inside one polygonal element **99.**

[00173] Once merged, the virtual object **71** can intersect the anatomical volume AV and/or can be spaced apart from the anatomical volume AV. Any number of virtual objects **71** may be utilized in this technique and these virtual objects **71** can have any suitable shape (e.g., planar, or complex shapes) or purpose (e.g., keep-out zone, keep-in zone, boundary, etc.). In one example, the virtual object **71** can be like boundaries described in **US20160338782A1,** filed on May **18, 2016,** entitled, "System And Method For Manipulating An Anatomy", the entire contents of which are hereby incorporated **by** reference. The virtual object **71** can have any number of polygonal elements **99.** The virtual object **71** may generated **by** the boundary generator **66,** as described above.

[00174] Once the control system **60** merges the anatomical data **65** and the virtual object **71,** the control system **60** determines a parameter to associate with one or more polygonal elements **99** of the virtual object **71.** This parameter can define an effect, an influence, and/or a reaction that a polygonal element **99** has on the virtual model of the tool as applied in the virtual simulation. The parameter can define a first parameter of the polygonal element **99** or the parameter can over-write or replace an existing parameter. In one example, the parameter is a tuning parameter related to stiffness of the polygonal element **99.** This tuning parameter can define spring or damper parameters related to the polygonal element **99.** In another example, the parameter can influence the feed rate of the tool 20. For example, the feed rate generator **82** may be coupled to the behavior controller 74 and can be made aware of any interaction between the model of the tool 20 with any polygonal element **99** parameterized as described herein. From there, the feed rate generator **82** can define or adjust the feed rate of the tool 20 based on such interaction.

[00175] Although pixels PX are used as an example below, any aspect of the techniques described herein that involves using pixels PX can be implemented in other ways that do not involve pixels PX. For instance, voxels VX of the anatomical volume AV may be used as well. The voxels VX can include density values DV. Any other type of **2-D** or **3-D** unit or measurement can be utilized when comparing the geometries described herein.

[00176] Referring to the first view of the merged model **101** of **FIG.** 12, the control system **60** in one example may determine the parameter of illustrated polygonal element **99 by** accounting for the density values DV of the pixels PX that are encapsulated **by** a perimeter of the polygonal element **99** in the **Xm, Ym** coordinate system. The control system **60** can also determine the parameter for the polygonal element **99 by** accounting for the density values DV of the pixels PX at least partially encapsulated by the polygonal element 99 in the X_M , Y_M coordinate system. In other instances, the control system **60** may determine the parameter for

the polygonal element **99 by** accounting for the density values DV of the pixels PX that are completely encapsulated **by** the polygonal element **99.** The control system **60** may also disregard the density values DV of the pixels PX if less than $X\%$ of the pixel PX is encapsulated **by** the polygonal element **99.**

[00177] Referring to the second view of the merged model **101** of **FIG.** 12, the control system **60** may additionally, or alternatively, determine the parameter of polygonal element **99 by** accounting for the density values DV of the pixels PX that are intersected **by** a plane of the polygonal element **99** in the **Xm, Zm** coordinate system. The control system **60** may determine the parameter for the polygonal element **99 by** accounting for the density values DV of the pixels PX at least partially intersected **by** the polygonal element **99.** In other instances, the control system **60** may determine the parameter for the polygonal element **99 by** accounting for the density values DV of the pixels PX within a predetermined or measured depth or distance from the polygonal element 99, shown as PX_{depth} shown in FIG. 12. The depth PX_{depth} may be any suitable depth and be in any suitable units. For example, the depth PX_{depth} may be predetermined, e.g., 1mm below the virtual object **71** or may be **3** pixels PX below the virtual **object 71.**

[00178] In some instances, the control system **60** may determine the parameter for the polygonal element **99** using density values DV of pixels PX below the virtual object **71** depending on how the tool 20 or the virtual model of the tool 20 penetrates the virtual object **71.** In such instances, the control system **60** may account for the density values DV of the pixels PX below the virtual object **71** that are interacted with **by** the tool 20 or a virtual model of the tool 20. For example, the control system **60** may account for any density values DV that intersect the virtual model of the tool 20.

[00179] Once the control system **60** identifies the density values DV that should be accounted for, the control system **60** may determine the parameter for the polygonal element(s) **99** in many ways, including, but not limited to, **by** computing or determining one or more of: an average, a median, range, mode, a maximum, or a minimum density value DV of the density values DV that are proximate to, interacting with, related to, or intersecting the polygonal elements **99.** Although the parameter value is based on the density values DV, the parameter value need not correspond to a density value resulting from the computation related to the accounted for density values DV. Instead, the parameter value can be a standardized or normalized value.

[00180] Once the control system **60** determines the parameter for the polygonal elements **99** of the virtual object **71,** the control system **60** may modify operation of the tool 20 in response to the tool 20 interacting with the polygonal elements **99.**

[00181] In the example of **FIG. 13A,** the energy applicator 24 exhibits a scenario where it slides along the virtual object **71** at a first feed rate. The first feed rate can be predetermined or based on a user applied force, where the manipulator is controlled in a manual or guided-manual mode in response to user applied force. In these modes, the user has freedom to move the tool 20 in a way which may cause the tool 20 to slide along the virtual object **71.** In turn, this may result in the virtual model of the tool 20 skimming or partially penetrating the polygonal elements **99** in the virtual object **71.** In such instances, the control system **60** may compute a second feed rate according to the parameter of polygonal elements **99** that the tool 20 interacts with. The control system **60** may then command the robotic manipulator to move the tool 20 at the second feed rate. For example, a user may move the tool 20 along the virtual object **71** at the illustrated direction with the first feed rate of 2mm/s. The polygonal element **99** with which the tool 20 interacts during this motion may have a parameter of *0.5,* which may be a one-half feed rate scaling factor. In response, the control system **60** may control the manipulator 14 according to the second feed rate, which will be one-half of the first feed rate, i.e., 1mm/s. The parameter, hence, is can scale an existing feed rate so that, for example, the density of the anatomy is considered for tool 20 interaction with the virtual object **71.**

[00182] In the example of **FIG.** 13B, the energy applicator 24 penetrates the polygonal element **99** of the virtual object **71.** In such an instance, the control system **60** modifies operation of the tool 20 based on applying a reactive force RXF derived from the virtual simulation between the model of the tool and the polygonal element(s) **99.** The control system **60** computes the reactive force RXF according to the parameter of polygonal element(s) **99** that the tool 20 interacts with and applies the reactive force RXF to the virtual model in the virtual simulation to reduce penetration of the polygonal elements **99 by** the virtual model. The control system **60** then commands the manipulator 14 to move the tool 20 in accordance with application of the reactive force RXF to constrain movement of the tool 20 relative to the virtual object **71.** This reactive force parameter technique can be utilized separately, or in combination with the feed rate parameter technique.

[00183] Several embodiments have been described in the foregoing description. The embodiments discussed herein are not intended to be exhaustive or limited to any particular form. The terminology which has been used is intended to be in the nature of words of description rather than of limitation. Many modifications and variations are possible in light

of the above teachings, and the invention may be practiced otherwise than as specifically described. Furthermore, the headings used in this document are introduced solely for reference and readability purposes and should not be understood to limit the content of the section solely **by** the subject matter of the heading.

CLAIMS

1. A computer-implemented surgical planning method comprising:

obtaining anatomical data comprising a geometry and density values of an anatomical volume;

obtaining path data comprising a tool path along which a robotic manipulator will move a tool to interact with the anatomical volume, the tool path defined **by** points between which the tool will successively pass;

obtaining tool data including a geometry of the tool that will interact with the tool path; merging the path data and the anatomical data; and

for at least one point of the tool path:

identifying a location of the point relative to the anatomical data,

loading, from the tool data, the geometry of the tool at the identified location,

at the identified location, identifying an intersection between the geometry of the tool and the anatomical volume,

determining density values of the anatomical data within the intersection,

computing a tool contact factor related to an interaction between the geometry of the tool and the anatomical volume,

setting a planned feed rate factor for the tool based on the determined density values and the computed tool contact factor, and

associating the planned feed rate factor with the at least one point; and

outputting cut plan data comprising the tool path including the planned feed rate factor associated with the at least one point of the tool path.

2. The computer-implemented surgical planning method of claim **1,** wherein obtaining anatomical data further includes obtaining a bone model associated with the anatomical volume.

3. The computer-implemented surgical planning method of claim 2, wherein obtaining path data further includes obtaining the tool path being predetermined based on one or more of:

a planned resection volume of the bone model of the anatomical volume; and geometry of an implant model selected for the bone model.

4. The computer-implemented surgical planning method of claim **1,** wherein obtaining anatomical data further includes obtaining imaging data including slices of the anatomical volume.

5. The computer-implemented surgical planning method of claim 4, wherein obtaining imaging data further includes obtaining **DICOM** data comprising intercept and slope values, slice thickness, and patient position at a time of imaging.

6. The computer-implemented surgical planning method of claim 4, wherein at the identified location, identifying the intersection between the geometry of the tool and the anatomical volume further comprises:

identifying one or more slices of the imaging data exhibiting the intersection between the geometry of the tool and the anatomical volume.

7. The computer-implemented surgical planning method of claim **6,** wherein determining density values of the anatomical data within the intersection further comprises:

for each identified slice, determining radiodensity values of the imaging data located within the intersection; and

collecting radiodensity values located within the intersections of each of the one or more identified slices.

8. The computer-implemented surgical planning method of claim **7,** wherein setting the planned feed rate factor for the tool based on the determined density values further comprises:

calculating a bone mineral density (BMD) factor of the anatomical volume relative to the identified location based on the collected radiodensity values; and

setting the planned feed rate factor for the tool based on the calculated BMD factor.

9. The computer-implemented surgical planning method of claim **8,** wherein:

obtaining imaging data further comprises obtaining **CT** slices of the anatomical volume; and

the geometry of the tool comprises a **3-D** geometry of the tool, and for the at least one point of the tool path:

loading the **3-D** geometry of the tool at the identified location, and

at the identified location, identifying **CT** slices for which there is a cross sectional intersection between the **3-D** geometry of the tool and the anatomical volume; for each identified **CT** slice, determining a Hounsfield unit for each pixel within the cross-sectional intersection; and

collecting the Hounsfield units from the pixels within the cross-sectional intersections of each of the identified **CT** slices.

10. The computer-implemented surgical planning method of claim **8,** wherein:

collecting the radiodensity values located within the intersection of each of the one or more identified slices further includes identifying one or more of: an average, a median, and a maximum radiodensity value from the collected radiodensity values; and

calculating the BMD factor further includes converting the one or more of: the average, the median, and the maximum radiodensity value into the BMD factor.

11. The computer-implemented surgical planning method of claim **10,** further comprising, for the at least one point of the tool path, and after identifying slices of the imaging data exhibiting the intersection between the geometry of the tool and the anatomical volume, for each identified slice, computing the tool contact factor **by** computing an intersection ratio related to the geometry of the tool within the intersection relative to the geometry of the tool outside of the intersection.

12. The computer-implemented surgical planning method of claim **11,** wherein converting the one or more of: the average, the median, and the maximum radiodensity value into the BMD factor further comprises multiplying the one or more of: the average, the median, and the maximum radiodensity value with the intersection ratio.

13. The computer-implemented surgical planning method of claim **11,** wherein, for each identified slice, determining a quantity of pixels within the geometry of the tool having Hounsfield units exceeding a predetermined threshold.

14. The computer-implemented surgical planning method of claim **1,** further comprising:

calculating a bone mineral density (BMD) factor of the anatomical volume relative to the identified location based on the determined density values; and

wherein setting the planned feed rate factor for the tool based on the determined density values further comprises setting the planned feed rate factor based on the calculated BMD factor.

15. The computer-implemented surgical planning method of claim 14, further comprising:

accessing a look-up table defining associations between predefined BMD factors and predefined feed rate factors; and

wherein, for the at least one point of the tool path, setting the planned feed rate factor based on the calculated BMD factor further comprises:

identifying, in the look-up table, the predefined BMD factor that is closest to the calculated BMD factor; and

setting the planned feed rate factor based on the predefined feed rate factor associated with the closest identified predefined BMD factor in the look-up table.

16. The computer-implemented surgical planning method of claim **15,** wherein, for the at least one point of the tool path, setting the planned feed rate factor based on the calculated BMD factor further comprises:

setting the planned feed rate factor to be a maximum feed rate factor in response to determining that the calculated BMD factor is below a minimum threshold; and/or

setting the planned feed rate factor to be a minimum feed rate factor in response to determining that the calculated BMD factor is above a maximum threshold.

17. The computer-implemented surgical planning method of claim **1,** further comprising:

for one point of the tool path, storing interaction coordinates obtained from the intersection between the geometry of the tool and the anatomical volume at the location of the one point, the interaction coordinates indicative of locations of simulated interaction between the geometry of the tool and the anatomical volume at the location of the one point; and

for a second point of the tool path successive to the one point;

identifying a location of the second point relative to the anatomical data,

loading, from the tool data, the geometry of the tool at the identified location of the second point,

at the identified location of the second point, identifying an intersection between the geometry of the tool and the anatomical volume,

determining density values of the anatomical data within the intersection at the location of the second point,

comparing coordinates of the determined density values to the interaction coordinates; and

disregarding any density values having coordinates that are identical to the interaction coordinates.

18. The computer-implemented surgical planning method of claim **1,** further comprising, for the at least one point of the tool path:

disregarding any density values located beyond the intersection between the geometry of the tool and the anatomical volume.

19. The computer-implemented surgical planning method of claim **1,** wherein merging the path data and the anatomical data further includes merging the path data and anatomical data into a common coordinate system.

20. The computer-implemented surgical planning method of claim **1,** wherein the cut plan data comprises the tool path along which a robotic manipulator will move a tool in an autonomous mode to interact with the anatomical volume.

21. The computer-implemented surgical planning method of claim **1,** further comprising:

for each point of the tool path:

identifying the location of the point relative to the anatomical data,

loading, from the tool data, the geometry of the tool at the identified location,

at the identified location, identifying the intersection between the geometry of the tool and the anatomical volume,

determining density values of the anatomical data within the intersection,

setting the planned feed rate factor for the tool based on the determined density values, and

associating the planned feed rate factor with the point; and

wherein outputting the cut plan data further comprises the tool path including the planned feed rate factor associated with each point of the tool path.

22. **A** non-transitory computer readable medium, having stored thereon instructions which, when executed **by** one or more processors, implement a computer-implemented surgical planning software configured to:

obtain anatomical data comprising a geometry and density values of an anatomical volume;

obtain path data comprising a tool path along which a robotic manipulator will move a tool to interact with the anatomical volume, the tool path defined **by** points between which the tool will successively pass;

obtain tool data including a geometry of the tool that will interact with the tool path; merge the path data and the anatomical data; and

for at least one point of the tool path:

identify a location of the point relative to the anatomical data,

load, from the tool data, the geometry of the tool at the identified location,

at the identified location, identify an intersection between the geometry of the tool and the anatomical volume,

determine density values of the anatomical data within the intersection,

compute a tool contact factor related to an interaction between the geometry of the tool and the anatomical volume,

set a planned feed rate factor for the tool based on the determined density values and the computed tool contact factor, and

associate the planned feed rate factor with the at least one point; and

output cut plan data comprising the tool path including the planned feed rate factor associated with the at least one point of the tool path.

23. The non-transitory computer readable medium of claim 22, wherein, when executed, the surgical planning software obtains anatomical data **by** further being configured to obtain a bone model associated with the anatomical volume.

24. The non-transitory computer readable medium of claim **23,** wherein, when executed, the surgical planning software obtains path data **by** further being configured to obtain the tool path being predetermined based on one or more of:

a planned resection volume of the bone model of the anatomical volume; and geometry of an implant model selected for the bone model.

25. The non-transitory computer readable medium of claim 22, wherein, when executed, the surgical planning software obtains anatomical data **by** being further configured to obtain imaging data including slices of the anatomical volume.

26. The non-transitory computer readable medium of claim *25,* wherein, when executed, the surgical planning software obtains imaging data **by** being further configured to obtain **DICOM** data comprising intercept and slope values, slice thickness, and patient position at a time of imaging.

27. The non-transitory computer readable medium of claim *25,* wherein, when executed, the surgical planning software identifies the intersection between the geometry of the tool and the anatomical volume at the identified location **by** being further configured to:

identify one or more slices of the imaging data exhibiting the intersection between the geometry of the tool and the anatomical volume.

28. The non-transitory computer readable medium of claim **27,** wherein, when executed, the surgical planning software determines density values of the anatomical data within the intersection **by** being further configured to:

for each identified slice, determine radiodensity values of the imaging data located within the intersection; and

collect radiodensity values located within the intersections of each of the one or more identified slices.

29. The non-transitory computer readable medium of claim **28,** wherein, when executed, the surgical planning software sets the planned feed rate factor for the tool based on the determined density values **by** being further configured to:

calculate a bone mineral density (BMD) factor of the anatomical volume relative to the identified location based on the collected radiodensity values; and

set the planned feed rate factor for the tool based on the calculated BMD factor.

30. The non-transitory computer readable medium of claim **29,** wherein, when executed, the surgical planning software obtains imaging data **by** being further configured to obtain **CT** slices of the anatomical volume; and

the geometry of the tool comprises a **3-D** geometry of the tool, and

for the at least one point of the tool path, the surgical planning software:

loads the **3-D** geometry of the tool at the identified location, and

at the identified location, identifies **CT** slices for which there is a cross-sectional intersection between the **3-D** geometry of the tool and the anatomical volume;

for each identified **CT** slice, determines a Hounsfield unit for each pixel within the cross-sectional intersection; and

collects the Hounsfield units from the pixels within the cross-sectional intersections of each of the identified **CT** slices.

31. The non-transitory computer readable medium of claim **29,** wherein the surgical planning software is further configured to:

collect the radiodensity values located within the intersection of each of the one or more identified slices **by** being further configured to identify one or more of: an average, a median, and a maximum radiodensity value from the collected radiodensity values; and

calculate the BMD factor **by** being further configured to convert the one or more of: the average, the median, and the maximum radiodensity value into the BMD factor.

32. The non-transitory computer readable medium of claim **31,** wherein the surgical planning software is configured to compute the tool contact factor **by** computing, for the at least one point of the tool path, and after identifying slices of the imaging data exhibiting the intersection between the geometry of the tool and the anatomical volume, for each identified slice, an intersection ratio related to the geometry of the tool within the intersection relative to the geometry of the tool outside of the intersection.

33. The non-transitory computer readable medium of claim **32,** wherein, when executed, the surgical planning software converts the one or more of: the average, the median, and the maximum radiodensity value into the BMD factor **by** being further configured to multiply the one or more of: the average, the median, and the maximum radiodensity value with the intersection ratio.

34. The non-transitory computer readable medium of claim **32,** wherein the surgical planning software is further configured to, for each identified slice, determining a quantity of pixels within the geometry of the tool having Hounsfield units exceeding a predetermined threshold.

35. The non-transitory computer readable medium of claim **23,** wherein the surgical planning software is further configured to:

calculate a bone mineral density (BMD) factor of the anatomical volume relative to the identified location based on the determined density values; and

wherein the surgical planning software sets the planned feed rate factor for the tool based on the determined density values **by** being further configured to set the planned feed rate factor based on the calculated BMD factor.

36. The non-transitory computer readable medium of claim **35,** wherein the surgical planning software is further configured to:

access a look-up table defining associations between predefined BMD factors and predefined feed rate factors; and

wherein, for the at least one point of the tool path, the surgical planning software sets the planned feed rate factor based on the calculated BMD factor **by** being further configured to:

identify, in the look-up table, the predefined BMD factor that is closest to the calculated BMD factor; and

set the planned feed rate factor based on the predefined feed rate factor associated with the closest identified predefined BMD factor in the look-up table.

37. The non-transitory computer readable medium of claim **36,** wherein, when executed, the surgical planning software, for the at least one point of the tool path, sets the planned feed rate factor based on the calculated BMD factor **by** being further configured to:

set the planned feed rate factor to be a maximum feed rate factor in response to determining that the calculated BMD factor is below a minimum threshold; and/or

set the planned feed rate factor to be a minimum feed rate factor in response to determining that the calculated BMD factor is above a maximum threshold.

38. The non-transitory computer readable medium of claim **23,** wherein the surgical planning software is further configured to:

for one point of the tool path, store interaction coordinates obtained from the intersection between the geometry of the tool and the anatomical volume at the location of the one point, the interaction coordinates indicative of locations of simulated interaction between the geometry of the tool and the anatomical volume at the location of the one point; and

for a second point of the tool path successive to the one point:

identify a location of the second point relative to the anatomical data,

load, from the tool data, the geometry of the tool at the identified location of the second point,

at the identified location of the second point, identify an intersection between the geometry of the tool and the anatomical volume,

determine density values of the anatomical data within the intersection at the location of the second point,

compare coordinates of the determined density values to the interaction coordinates; and

disregard any density values having coordinates that are identical to the interaction coordinates.

39. The non-transitory computer readable medium of claim **23,** wherein the surgical planning software is further configured to, for the at least one point of the tool path:

disregard any density values located beyond the intersection between the geometry of the tool and the anatomical volume.

40. The non-transitory computer readable medium of claim **23,** wherein, when executed, the surgical planning software merges the path data and the anatomical data **by** being further configured to merge the path data and the anatomical data into a common coordinate system.

41. The non-transitory computer readable medium of claim **23,** wherein the cut plan data comprises the tool path along which a robotic manipulator will move a tool in an autonomous mode to interact with the anatomical volume.

42. The non-transitory computer readable medium of claim **23,** wherein the surgical planning software is further configured to:

for each point of the tool path:

identify the location of the point relative to the anatomical data,

load, from the tool data, the geometry of the tool at the identified location,

at the identified location, identify the intersection between the geometry of the tool and the anatomical volume,

determine density values of the anatomical data within the intersection,

set the planned feed rate factor for the tool based on the determined density values, and

associate the planned feed rate factor with the point; and

wherein, when executed, the surgical planning software is further configured to output the cut plan data **by** being further configured to output the tool path including the planned feed rate factor associated with each point of the tool path.

43. **A** surgical system comprising:

a robotic manipulator configured to support and move a tool; and

a control system coupled to the robotic manipulator, and comprising:

one or more processors; and

a non-transitory computer readable medium, having stored thereon instructions which, when executed **by** the one or more processors, implement a computer implemented surgical planning software configured to:

obtain anatomical data comprising a geometry and density values of an anatomical volume;

obtain path data comprising a tool path along which a robotic manipulator will move a tool to interact with an anatomical volume, the tool path defined **by** points between which the tool will successively pass;

obtain tool data including a geometry of the tool that will interact with the tool path;

merge the path data and the anatomical data; and

for at least one point of the tool path:

identify a location of the point relative to the anatomical data,

load, from the tool data, the geometry of the tool at the identified location,

at the identified location, identify an intersection between the geometry of the tool and the anatomical volume,

determine density values of the anatomical data within the intersection,

compute a tool contact factor related to an interaction between the geometry of the tool and the anatomical volume,

set a planned feed rate factor for the tool based on the determined density values and the computed tool contact factor, and

associate the planned feed rate factor with the at least one point; and

output cut plan data comprising the tool path including the planned feed rate factor associated with the at least one point of the tool path; and

wherein the control system utilizes the outputted cut plan data to control the robotic manipulator to move the tool along the tool path according to the planned feed rate factor associated with the at least one point of the tool path for enabling the tool to interact with the anatomical volume.

44. **A** computer-implemented surgical planning method comprising:

obtaining anatomical data comprising a geometry of an anatomy;

obtaining path data comprising a tool path along which a robotic manipulator will move a tool to interact with the anatomy, the tool path defined **by** points between which the tool will pass;

obtaining tool data including a geometry of the tool;

merging the path data and the anatomical data;

for at least one point of the tool path:

identifying a location of the point relative to the anatomical data,

loading, from the tool data, the geometry of the tool at the identified location,

computing a tool contact factor related to an interaction between the geometry of the tool and the anatomy,

setting a planned feed rate factor for the tool based on the computed tool contact factor, and

associating the planned feed rate factor with the at least one point; and outputting cut plan data comprising the tool path including the planned feed rate factor associated with the at least one point of the tool path.

45. **A** computer-implemented method comprising:

obtaining anatomical data comprising a geometry and density values of an anatomical volume;

obtaining virtual object data comprising geometry of a virtual object having a mesh of polygonal elements;

merging the anatomical data and the virtual object data to determine a parameter for one or more polygonal elements of the mesh based on the density values;

implementing a virtual simulation wherein a tool is represented as a virtual model being adapted to interact with the one or more polygonal elements of the virtual object; and

modifying operation of a tool based on the parameter in response to the virtual model of the tool interacting with to the one or more polygonal elements of the virtual object.

46. The computer-implemented method of claim *45,* comprising:

commanding robotic manipulator to move the tool according to a first feed rate;

while the tool moves according to the first feed rate, detecting interaction between the virtual model and the one or more polygonal elements of the virtual object; and

computing a second feed rate based on the parameter associated with the one or more polygonal elements; and

wherein modifying operation of the tool includes commanding the robotic manipulator to move the tool at the second feed rate.

47. The computer-implemented method of claim *45,* comprising:

commanding robotic manipulator to move the tool;

penetrating, with the virtual model of the tool, the one or more polygonal elements of the virtual object;

computing a reactive force based on the parameter associated with the one or more polygonal elements; and

applying the reactive force to the virtual model in the virtual simulation to reduce penetration of the one or more polygonal elements **by** the virtual model; and

wherein modifying operation of the tool includes commanding the robotic manipulator to move the tool in accordance with application of the reactive force to the virtual model in the virtual simulation to constrain movement of the tool relative to the virtual object.

48. **A** computer-implemented method comprising:

obtaining anatomical data comprising a geometry and density values of an anatomical volume;

obtaining virtual object data comprising geometry of a virtual object having a mesh of polygonal elements; and

merging the anatomical data and the virtual object data to determine a parameter for one or more polygonal elements of the mesh based on the density values.

49. **A** non-transitory computer readable medium, having stored thereon instructions which, when executed **by** one or more processors, implement a computer-implemented surgical planning software configured to:

obtain anatomical data comprising a geometry and a tissue parameter of an anatomical volume;

obtain path data comprising a tool path defined **by** points;

obtain tool data including a geometry of a tool that will interact with the tool path;

merge the path data and the anatomical data; and

for at least one point of the tool path:

identify a location of the point relative to the anatomical data,

load, from the tool data, the geometry of the tool at the identified location,

at the identified location, identify an intersection between the geometry of the tool and the anatomical volume,

determine the tissue parameter of the anatomical data within the intersection,

compute a tool contact factor related to an interaction between the geometry of the tool and the anatomical volume,

set a planned feed rate factor for the tool based on the determined tissue parameter and the computed tool contact factor, and

associate the planned feed rate factor with the at least one point; and

output cut plan data comprising the tool path including the planned feed rate factor associated with the at least one point of the tool path.

50. The non-transitory computer readable medium of claim 49, wherein the computer-implemented surgical planning software is further configured to set the planned feed rate factor for the tool based on achieving a predetermined motor current on a motor of the tool.

51. The non-transitory computer readable medium of claim 49, wherein the computer-implemented surgical planning software is further configured to:

set an output pose for the tool based on the determined tissue parameter and the computed tool contact factor;

associate the output pose with the at least one point; and

output the cut plan data comprising the tool path including the output pose associated with the at least one point of the tool path.

52. The non-transitory computer readable medium of claim 49, wherein the computer-implemented surgical planning software is configured to obtain path data **by** being further configured to obtain a predefined pose of the tool with respect to at least one point of the tool path.

53. A non-transitory computer readable medium, having stored thereon instructions which, when executed **by** one or more processors, implement a computer-implemented surgical planning software configured to:

obtain anatomical data comprising a geometry and a tissue parameter of an anatomical volume;

obtain path data comprising a tool path defined **by** points;

obtain tool data including a geometry of a tool that will interact with the tool path;

merge the path data and the anatomical data; and

for at least one point of the tool path:

identify a location of the point relative to the anatomical data,

load, from the tool data, the geometry of the tool at the identified location,

at the identified location, identify an intersection between the geometry of the tool and the anatomical volume,

determine the tissue parameter of the anatomical data within the intersection,

compute a tool contact factor related to an interaction between the geometry of the tool and the anatomical volume,

set an output pose for the tool based on the determined tissue parameter and the computed tool contact factor, and

associate the output pose with the at least one point; and

output cut plan data comprising the tool path including the output pose associated with the at least one point of the tool path.

54. The non-transitory computer readable medium of claim **53,** wherein the computer-implemented surgical planning software is configured to obtain path data **by** being further configured to obtain a predefined pose of the tool with respect to at least one point of the tool path.

55. A non-transitory computer readable medium, having stored thereon instructions which, when executed **by** one or more processors, implement a computer-implemented surgical planning software configured to:

obtain anatomical data comprising a geometry and a tissue parameter of an anatomical volume;

obtain path data comprising a tool path defined **by** points;

obtain tool data including a geometry of a tool that will interact with the tool path;

merge the path data and the anatomical data; and

for at least one point of the tool path:

identify a location of the point relative to the anatomical data,

load, from the tool data, the geometry of the tool at the identified location,

at the identified location, identify an intersection between the geometry of the tool and the anatomical volume,

determine the tissue parameter of the anatomical data within the intersection,

compute a tool contact factor related to an interaction between the geometry of the tool and the anatomical volume,

set a planned feed rate factor for the tool based on the determined tissue parameter, the computed tool contact factor, and achieving a predetermined motor current on a motor of the tool, and

associate the planned feed rate factor with the at least one point; and

output cut plan data comprising the tool path including the planned feed rate factor associated with the at least one point of the tool path.

56. A non-transitory computer readable medium, having stored thereon instructions which, when executed **by** one or more processors, implement a computer-implemented surgical planning software configured to:

obtain anatomical data comprising a geometry and a tissue parameter of an anatomical volume;

obtain path data comprising a tool path defined **by** points;

obtain tool data including a geometry of a tool that will interact with the tool path;

merge the path data and the anatomical data; and

for at least one point of the tool path:

identify a location of the point relative to the anatomical data,

load, from the tool data, the geometry of the tool at the identified location,

at the identified location, identify an intersection between the geometry of the tool and the anatomical volume,

determine the tissue parameter of the anatomical data within the intersection,

compute a tool contact factor related to an interaction between the geometry of the tool and the anatomical volume,

set a tool operation parameter based on the determined tissue parameter and the computed tool contact factor, and

associate the tool operation parameter with the at least one point; and output cut plan data comprising the tool path including the tool operation parameter associated with the at least one point of the tool path.

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FIG. 3

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Slice B at Point P1

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 $\begin{picture}(20,17) \put(0,0){\line(1,0){155}} \put(15,0){\line(1,0){155}} \$

Average Ratio = 0.7436 ; Max Radiodensity = 805 Hu

BMD Factor = 0.7436×805 Hu = 598.598

FIG. 9

FIG. 10

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