

가 , () 가 .

" - " 2 1 ()

가 , () ()

2 " " 가 2

가 2 가 가 2

가 2 가 1

C. Berrou " Near Shannon Limit Error - Correcting, Coding and Decoding: Turbo - codes91)" , Proc. IEEE Int. Conf. on Communications ICC'93, Genua, 1993, Pages 1064 - 1070 가

1 BAHL
가 2 VITERBI -

MAP(Maximum a - Posteriori) - 가 1
MAP - 가 (MAP -)
가

2 MAP - 가 - P. Jung " Analys e und Entwurf digitaler Mobilfunksysteme" , Stuttgart, B.G. Teubner, 1997, Pages 343 - 368, E. 2

가 . ,

가 , ()

D. Raphaeli Y, Zarai " Combined Turbo Equalization and Turbo Decoding" , IEEE Communications Letters, Bd. 2, Nr. 4, 1998, Pages 107 - 109 , () - " - "

(" - ") MAP - 2 MAP - 1 MAP - 2 가 , 가

가 , - 가 (,) 가 , - 가

P. Jung " Novel low complexity decoder for turbo - codes" , Electronics Letters, Bd. 31, Nr. 2, 1995, Pages 86 to 87 , - 가

(,) SUBMAP - 1 2 가

2 가 , 2

1 1 2 2

6

1 2 MAP -

P. Jung (1 MAP -
, E.3.3 " Rekursive MAP - Symbolschaetzung" , Pages 353 - 361

).

2 , 2 1 1 2
(가)

AP - 1 2 1 1 3 M

1 / 2

6

" 가 1 1 2 2 3
(2 : 0, 1) "

2 , 1 2 2

" - " 가 , " - "

가

1 - - ,

2 1 RSC - ,

2a ,

3 ,

4 3 - ,

5 4 - ,

(3)
- (TCOD)가 1

(TCOD) 2 2 (RSC1 RSC2) , 2
 RSC - (Recursive Systematic Convolutional -)
 (RSC2) (IL)가 , 2 (RSC1 RSC2)
 (PKT1 PKT2) (MUX) .

$$U = (u_1, \dots, u_N) \quad (1)$$

(U) , , (TCOD) , n = 1, 2, ..., N U_n =

$$R_1 = (r_{1,1}, \dots, r_{1,N})$$

(R1 R2) (RSC1 RSC2) , N 2 (R1 R2)

$$R_2 = (r_{2,1}, \dots, r_{2,N}) \quad (2)$$

$$C = (c_1, \dots, c_K) \quad (3)$$

$$\begin{pmatrix} R_1 & R_2 \\ (R_1 & R_2) \end{pmatrix} \begin{pmatrix} PKT1 & PKT2 \\ (MUX) \end{pmatrix} , K (U) 2$$

$$C = (c_1, \dots, c_K) \quad (3)$$

$$R_c = N/K \quad (R_e) , - 가 (C) (U) 2$$

$$R_c = 1/2 가 (C) (U) 2$$

(N)가 , (PKT1 PKT2) (MUX)
 (C) :

$$c_{2n-1} = u_n \quad n = 1, \dots, N$$

$$c_{4n-2} = r_{1,2n-1} \quad n = 1, \dots, N/2$$

$$c_{4n} = r_{2,2n} \quad n = 1, \dots, N/2 \quad (4)$$

$$N = 4 , - (TCOD) (C)가 :$$

$$C = (u_1, r_{1,1}, u_2, r_{2,2}, u_3, r_{1,3}, u_4, r_{2,4}) \quad (5)$$

$$U = (u_1, \dots, u_N) \quad (C)$$

(5) .

$$\begin{pmatrix} (C) & N \\ (R) \end{pmatrix} : \begin{pmatrix} (R1 & R2) \\ (R) \end{pmatrix} 가 .$$

$$R = (r_1, \dots, r_N) \quad (6)$$

r_2 = r_{2,2} , r_3 = r_{1,3} , r_4 = r_{2,4} .

$$K = 2N \quad (C) \quad (U) \quad N \quad (R) \quad N$$

(C) , () ,

2 RSC - 가 RSC1 / RSC2 RSC - (T)
 RSC - (RSC1) 1 가 (ADD1) 가 (ADD1) 4 가 2
 가 (ADD2) RSC - (RSC1) (R1) ,
 (r_{1,n})가 (U) (U_n) (R1)
 D1) 2 () 4 (L) ,가 (AD
 5가 .

(U) (R1) 2
 (TCOD) (C)가 (4)
 (trellis) - RSC1 - (TCOD -) R1(C)
 .4 RSC1 - - M_T = 2⁴
 가 , 가 (u = 0 1) 2
 2 (m') () 1 (m) -
 (R1) RSC1 - -

3 (DEC) .
 , DEC :
 DEC 1 (I1) 가 가 ,
 E = (e₁, ..., e_K)(7),

(C) (C₁ C_K) K
 (C) (E) , (U)

X = (x₁, ..., x_N)(8), (R)(6) -
 Y = (y₁, ..., y_N)(9)

(5 6) (y_n) 1 RSC - (RSC1) (r_{1,n}) 2 RSC - (RSC2)
 (r_{2,n}) 가 , Y :
 Y = (y_{1,1}, y_{2,2}, y_{1,3}, y_{2,4}, ...)(10). , 2 - (Y1 Y2) Y = Y1
 + Y2 :

Y1 = (y_{1,1}, 0, y_{1,3}, 0, ...)(10a)
 Y2 = (0, y_{2,2}, 0, y_{2,4}, ...)(10b).

(4) , 1 (I1) (E)가 가 ,
(X, Y1 X, Y2) 가 .

DEC () 2 (I2) , () (a-priori) - (L_A(U))가 가 (L_A(U)) :

L_A(U) = (L_A(u₁), ..., (L_A(u_N))), 2 :

$$L_A(u_n) = \log \left\{ \frac{P(u_n = 1)}{P(u_n = 0)} \right\} \quad n = 1, \dots, N. \quad (11)$$

(, P(u_n = 1) P(u_n = 0) u_n = 1 0 . 2가 가
n = 1, ..., N) 가 가 , L_A(U) = (0, ..., 0)가 .

DEC 1 (O1) 1 가 .

P(u_n = 1 | E) P(u_n = 0 | E) 1 , (E)가
u_n = 1 0 " (a posteriori) " ,
((E)) (u₁ u_N)

2 (u) 1 : , N u (u_n), n = 1, ..., N

u' = (u'1), ..., (u'N) (12)

(u' (u_N)) (u₁ u_N) 가 , (U)

$$\Lambda(u_n) = \log \left\{ \frac{P(u_n = 1|E)}{P(u_n = 0|E)} \right\} \quad (13)$$

(u₁, ..., u_N) - (L_A(U)) 가 ,
P(u_n = 1 | E, L_A(U)) P(u_n = 0 | E, L_A(U)) 1 .

DEC 2 (O2) 2 가 .

P(c_K = 1 | E) P(c_K = 0 | E) 2 , (E)가
c_K = 1 0 (u₁, ..., u_N) - (L_A(U))
A(U) 가 , P(c_K = 1 | E, L_A(U)) P(c_K = 0 | E, L_A(U))

$$\mu_n^i(E, m', m) \tag{17}$$

가 E () " 가 AWGN - (Additive White Gaussian Noise -) , 가 :

$$\mu_n^i(E, m', m) = \left\{ \frac{a_n}{\sigma^2} x_n + \frac{1}{\sigma^2} L_A(u_n) \right\} (2i-1) + \frac{a_n}{\sigma^2} y_{1,n} (2r_{1,n} - 1) \tag{18}$$

가 , i 가 , $y_{1,n}$, a_n e_n , $r_{1,n}$, $L_A(u_n)$ (2) (10a)

$$\delta_n(m) = \max_{m' < m} \{ \mu_n^1(E, m', m) + \delta_{n-1}(m'), \mu_n^0(E, m', m) + \delta_{n-1}(m') \} \tag{19a}$$

$$\varepsilon_n(m) = \max_{m' > m} \{ \mu_{n+1}^1(E, m, m') + \varepsilon_{n+1}(m'), \mu_{n+1}^0(E, m, m') + \varepsilon_{n+1}(m') \} \tag{19b}$$

, m $m' < m$ - m () m' , $m' > m$

1 가 :

$$A(u_n) = \max_{m \Leftarrow m'} \{ \delta_n(m) + \mu_n^1(E, m, m') + \varepsilon_{n+1}(m') \} - \max_{m \Leftarrow m'} \{ \delta_n(m) + \mu_n^0(E, m, m') + \varepsilon_{n+1}(m') \} \tag{20}$$

m m' - (m, m')

, 2 (c) 가 :

" (R) , 2 (C)가 () (U) "

2 : (R) 가 , 1

$$\Lambda(r_n) = \max_{m \leftrightarrow m'} \{ \delta_n(m) + \mu_n^{r_n=1}(E, m, m') + \varepsilon_{n+1}(m') \} - \max_{m \leftrightarrow m'} \{ \delta_n(m) + \mu_n^{r_n=0}(E, m, m') + \varepsilon_{n+1}(m') \} \quad (21)$$

r_n n (, u_n) , (C)

2 , 2 가 :

$$\Lambda(r_n) = \text{sign}(\Lambda(u_n) \cdot \Lambda(u_{n-1}) \cdot \dots \cdot \Lambda(u_{n-L+1})) \max_{RPT} \{ \Lambda(u_n), \Lambda(u_{n-1}), \dots, \Lambda(u_{n-L+1}) \} \quad (22)$$

u_{n-L+1}) 가 , (-) (r_n)가 L (22) 2 ($u_n, u_{n-1}, \dots, u_{n-L+1}$) RTP , " "

, 2 (RPT) :

2 () , L = 5 가 , 2

$$\Lambda(r_n) = \text{sign}(\Lambda(u_n) \cdot \Lambda(u_{n-4})) \max \{ \Lambda(u_n), \Lambda(u_{n-4}) \}, \quad (22a)$$

, (RPT) 1 L (L - 4) , (r_n)가 (u_n, u_{n-4})

2 (RSC1)(가 L = 5) , 2 가

$$\Lambda(r_n) = \text{sign}(\Lambda(a_n) \cdot \Lambda(a_{n-4})) \max \{ \Lambda(a_n), \Lambda(a_{n-4}) \}$$

재귀 과정에 의해서

$$\Lambda(a_n) = \text{sign}(\Lambda(u_n) \cdot \Lambda(a_{n-1}) \cdot \dots \cdot \Lambda(a_{n-4})) \max \{ \Lambda(u_n), \Lambda(a_{n-1}), \dots, \Lambda(a_{n-4}) \},$$

(22b)

a_{n-4}) (r_n) (2) $(r_{1,n})$)가 $(a_n$
 4 2 (DEC1, DEC2) - (TDEC)
 Y2(RSC2) (DMUX) (E)가 X(), Y1(RSC1)
 X Y1 1 (DEC1) 1 (I1) (DEC1) 3
 (DEC) , 1 (I1) (DMUX)
 (E)가 () (X Y1)
 1 (DEC1) 2 (I2) (L_A(U))가 가 ,
 (U) 2 (DEC2) 1
 1 (DEC1) (20) 1 / 1_u
 DEC1 1 (O1) . 1 (DEC1) 2 / 1_c
 (21) (22)((22a, b)) DEC1 (O2)
 1 (/ 1_u) 가 (AD1) (IL1) 2 (DEC2) 2 (I2)
 , 가 가 L_A(U) . 2 (DEC2) 1 (I1)
 가 - - (Y2) (IL2) (X)가
 2 (DEC2) 1 (20) / 2_u
 DEC2 1 (O1) . 2 (DEC2) 2 / 2_c
 (21) (22)((22a, b)) DEC2 (O2)
 DEC2 1 (/ 2_u) 가 (AD2) , 가 2 (D
 EC2) 2 (I2) . 가 (AD2) (DIL1)
 (L_A(U)) 1 (DEC1)
 DEC2 1 (/ 2_u) (U) 가 ((= ((1, ..., (N))
 = 0 , / 2_u(u_n) > 0 / 2_u (TL) , / 2_u(u_n) 0 (n
 (TL) (DIL2) , (()

2 (1c, 2c) , " - " 가 (ED)
 . - , 4 (TDEC)

ED LA(U), 1c 2c 가 가 (AD3, AD4 AD5) , 가
 X, Y1 Y2 가 (AD3, AD4 AD5) (C)
 , (ED)가 .

5 , - (TEQU) . (가
) (EQU) 1 (E) ,
 HF - (, A/D - ,) (EQU) ,
 () , (E) (

(EQU) 가 (AD6) 1 , 가 (BDI
 L) (BDIL) (C) (E)가
 . (TDEC) (ED) (BIL) 가 (AD6) 2
 - (TDEC) (EQU) . 2 ,
 가

(57)

1.

- (e1, e2, ..., eK) (E) ,
 - (e1, e2, ..., eK) (E)가 (u1, u2, ...,
 uN) (U) n- (un) i
 (un) 1 (U(un)) ,

- (e1, e2, ..., eK) (E)가 , (C)
 k- (ck) i (ck) 2
 (U(c_k)) ,

2 가 (μ_nⁱ(E, m, m')), (n(m)) (TCOD) (m, m')
 , (n+1 (m'))

$(R_1, R_2; R)$ 가 (u_1, u_2, \dots, u_N) (U) $(c_1, c_2, \dots,$
 $c_K)$ (C) 가 가 , ,
 $(TCOD)$ (m, m')
 i 2 $(\int_C c(c_k))$,

$$\{\epsilon_n(m) + \mu_n^{P_K(n)=i}(E, m, m') + \epsilon_{n+1}(m')\}$$

$c_{K(n)}$ n - (U_n) (c_K) .

2.

- (e_1, e_2, \dots, e_K) (E) ,
 - (E)가 (U)
 n - (u_n) i (u_n) 1
 $(\int_U u(u_n))$,

- (e_1, e_2, \dots, e_K) (E)가 (C)
 k - (c_k) i (c_k) 2
 $(\int_C c(c_k))$,

$(R_1, R_2; R)$ 가 (u_1, u_2, \dots, u_N) (U) $(c_1, c_2, \dots,$
 $c_K)$ (C) 가 가 , ,
 1 $(\int_U u(u_n))$ 2 $(\int_C c(c_k))$

3.

1 2 ,
 - 1 가 $(\mu_n^i(E, m, m'))$, $(u_n(m))$ (TCOD) (m, m')
 $(u_{n+1}(m'))$,

- 1 ,

$$\{ \varepsilon_n(m) + \mu_n^i(E, m, m') + \varepsilon_{n+1}(m') \}$$

i n - (u_n) .

4.

1 3 ,

- (u₁, u₂, ..., u_N) (U) - (L_A(U)) ,

- (L_A(U)) 1 / 2 (/ u; / c)

5.

1 4 ,

(c₁, c₂, ..., c_K) (C) (u₁, u₂, ..., u_N) (U)

6.

- (e₁, e₂, ..., e_K) (E) 1 (I1),

- 1 (/ u(u_n)) 1 (O1),

- 2 (/ c(c_k)) 2 (O2) ,

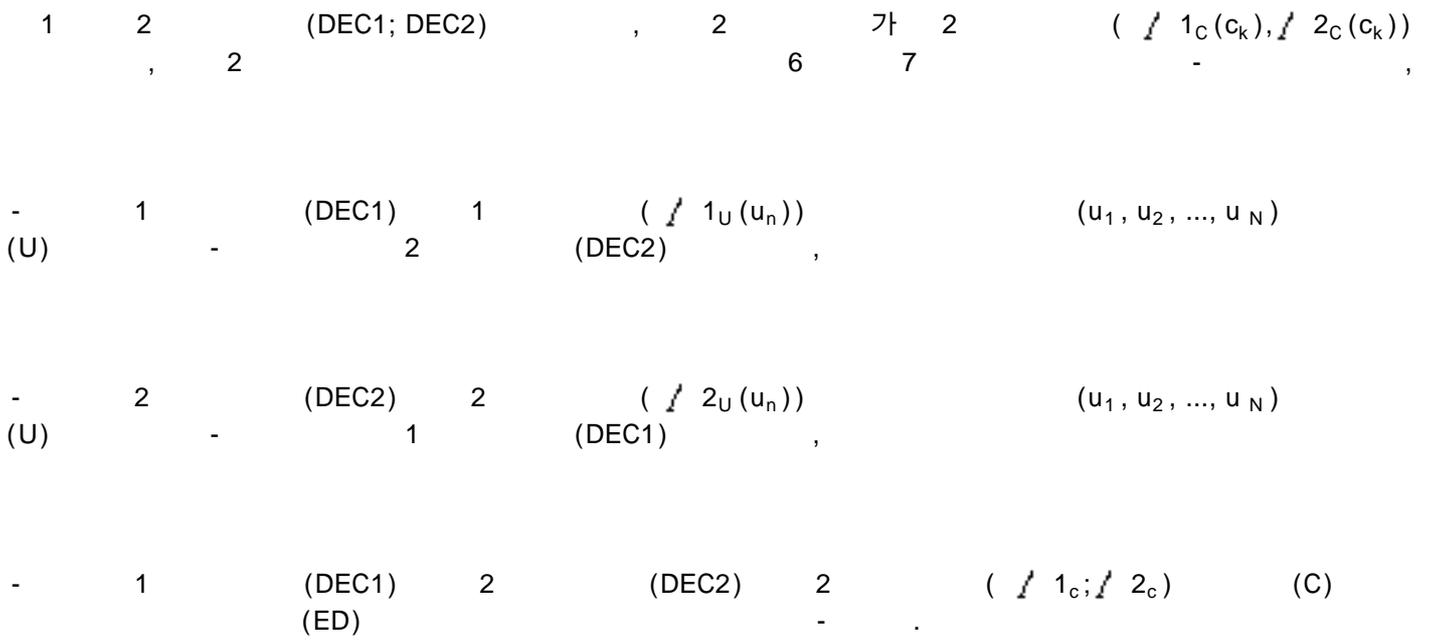
2 (/ c(c_k)) .

7.

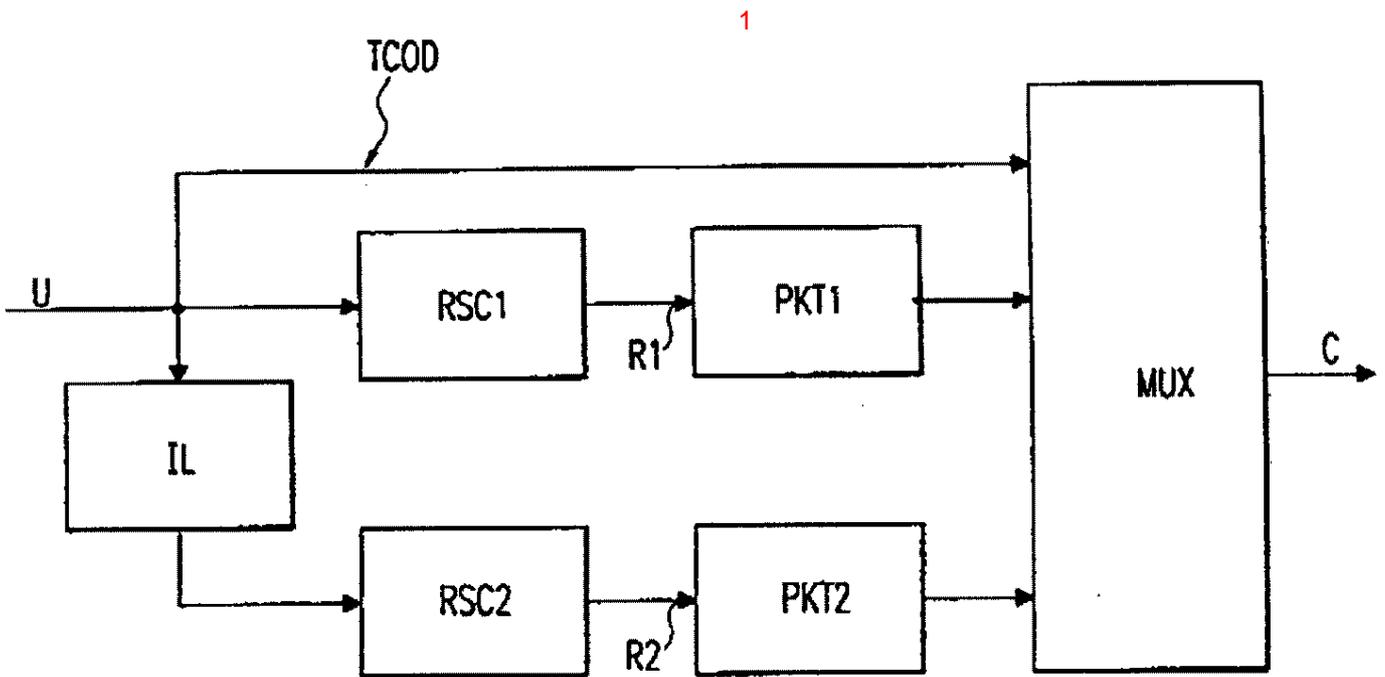
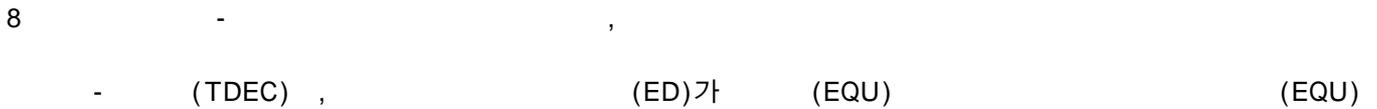
6 ,

(DEC; DEC1, DEC2)가 3 (O3) 가 , (u₁, u₂, ..., u_N) 가 (/ 1, ..., / N)

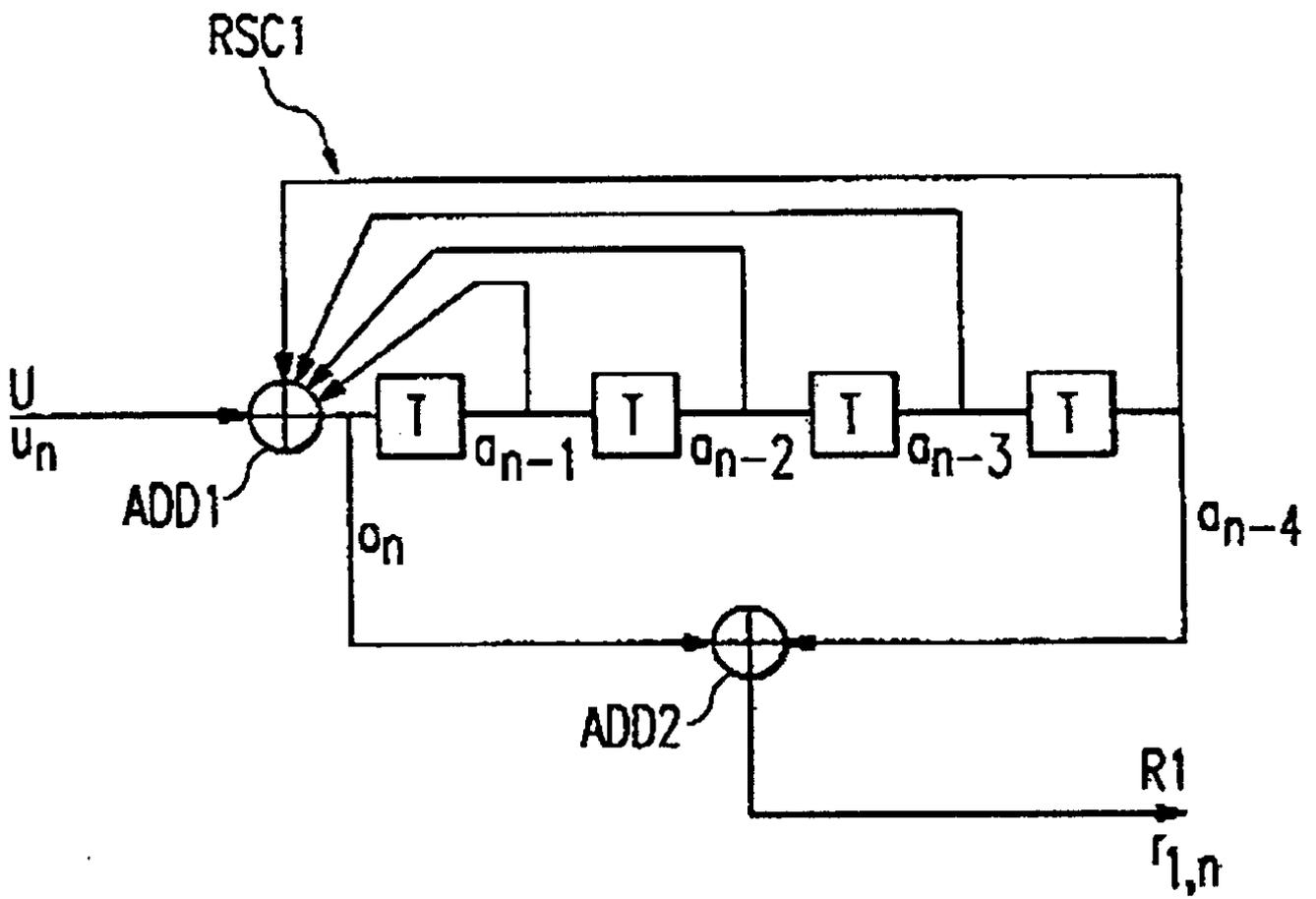
8.



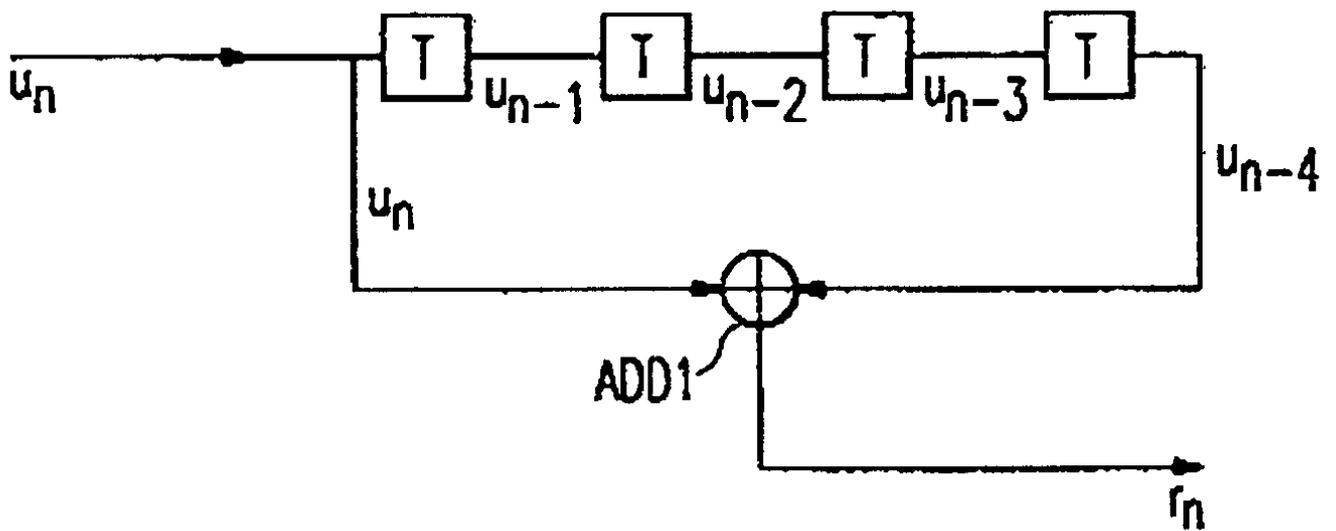
9.



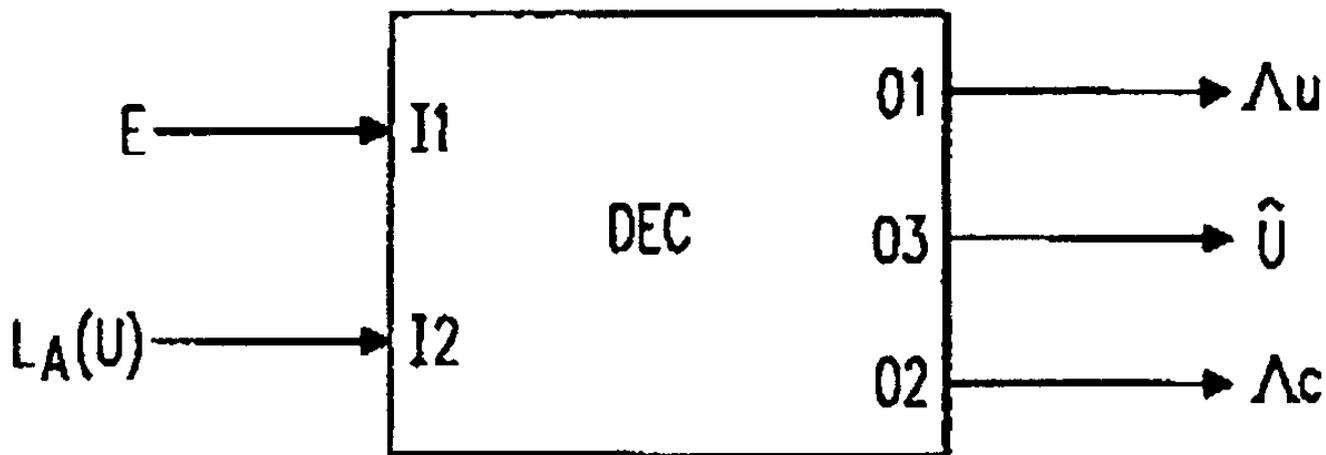
2



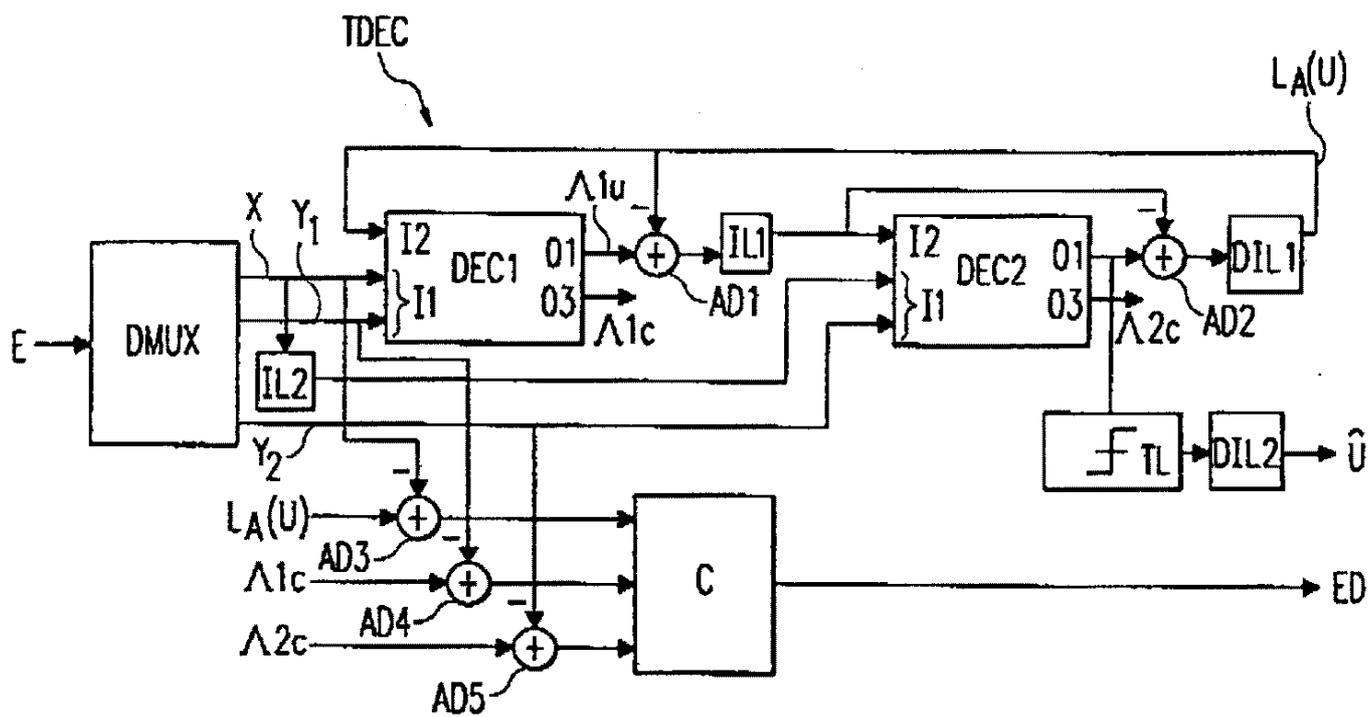
2a



3



4



5

