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ARTIFICIAL TRANSFORMER

2 Sheets-Sheet 1









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#### 2,923,784

#### ARTIFICIAL TRANSFORMER

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#### 15 Claims. (Cl. 330-85)

This invention relates generally to the coupling of a 15 source of electric signals to a load and to the continuous maintenance of prescribed conditions of impedance match between them despite variations of the self impedance of either one.

In an ideal close-coupled transformer, the ratio of pri- 20 mary to secondary voltage is directly proportional to the ratio  $(N:1)$  of the number of turns in the primary winding to the number in the secondary winding. Similarly, the ratio of primary to secondary current is inversely proportional to the turns-ratio,  $(N:1)$ . The impedance presented at the primary terminals of the transformer is by the square of the turns-ratio  $(N^2)$ . Uses of such transformers are manifold. portional to the turns-ratio,  $(N:1)$ . The impedance pre- 25

transformers are manifold. Variable transforiners wherein the effective turns-ratio 30 is altered in discrete steps by sliding contacts are well known; however, such transformers typically are usable only over a restricted range of frequencies and are char acterized by noise generated as the tap is moved discon tinuously from turn to turn. Moreover, servo-mech- 35 anisms to effect dynamic variations of the position of the movable tap are complex and cumbersome. A transformer designed for use at very low frequencies requires a bulky and heavy iron core to obtain the necessary self inductance to permit linear operation at such low fre-40 quencies. For many laboratory uses such an iron core transformer is prohibitively expensive, and an unacceptable time delay in development work may attend the fabrication of such special units.

fabrication of such special units.<br> **It is an object of this invention to provide a compact,** lightweight unit which will simulate in external characteristics an ideal transformer with continuously variable of frequencies from the very lowest frequencies to the megacycle range. 50

Another object of this invention is to provide an artificial transformer by which the apparent impedance of a passive network may be altered without destroying its desired frequency response characteristics.

Another object of this invention is to provide an arti- 55 ficial transformer with a control by which the varying impedance of a load may be continuously matched to that of a generator.

Another object of this invention is to provide a device that will transform the sign as well as the magnitude of a passive impedance (for example, a positive resistance can be made to appear as a negative resistance of arbi trary magnitude, or an inductive reactance can be made to appear as a capacitive reactance of arbitrary magni

tude). To these ends, the invention consists of certain novel connections of a voltage amplifier and a current amplifier; namely, that each amplifier is connected in a feedback relation to the other to form the functional lent of a magnetic transformer with effective turns-ratio responsive to a controlled variation of the amplifier gains.

The principles governing the fabrication and use of

2

such artificial transformers, together with further objects and advantages thereof, will best be comprehended by ref erence to the following description of illustrative embodi ments thereof, taken in connection with the accompany-<br>ing drawings, in which:<br>Fig. 1 is a circuit diagram of an ordinary close-coupled

10 ratio N:1; magnetic transformer which transforms a primary voltage  $e_1$  and a primary current  $i_1$  into a secondary voltage  $e_2$  and a secondary current  $i_2$  in accordance with a turns-

Fig. 2 is a block diagram of an ideal artificial transformer device constructed in accordance with this in

Fig. 3 is a more detailed block diagram representative of a practical embodiment of the invention;

Fig. 4 is a partial schematic diagram showing substantially the same circuit shown in Fig. 3 with the ele ments further broken down and grouped in a functional manner:

Fig. 5 is a schematic diagram representative of a specific embodiment of the invention which has been found to be useful in the laboratory; and

Fig. 6 is a schematic diagram of a simple transmission system incorporating the invention.

Referring now to the drawings, Fig. 1 represents a con ventional close-coupled magnetic transformer having a primary winding 1 and a secondary winding 2. Both windings link a common core 3. The turns-ratio, N, of the number of primary winding turns around the core to the number of secondary turns determines the voltage and current ratios of the transformer.

Externally, the transformer presents four terminals, two input terminals 4 and 5 connected to the primary winding and two output terminals  $6$  and  $7$  connected to the secondary winding. The input current,  $i_1$ , and the input voltage,  $e_1$ , are related to the output current  $i_2$  and output voltage  $e_2$  through the turns-ratio. Thus

 $\frac{i_2}{i_1} = N$  (1)

and

$$
\frac{e_2}{e_1} = \frac{1}{N} \tag{2}
$$

45 Further, a secondary load impedance,  $Z_2$ , "viewed" from the primary is multiplied by the square of the turns ratio, i.e.:

$$
\frac{e_1}{i_1} = N^2 Z_2 \tag{2a}
$$

and conversely, for a primary impedance  $Z_1$ , viewed from the secondary side:

$$
\frac{e_2}{i_2} = \frac{Z_1}{N^2} \tag{2b}
$$

60 These equations describe an "ideal' close-coupled trans former. They quite accurately define the performance of a conventional close-coupled iron cored transformer over a band of frequencies. For a well designed transformer these relations can be made to hold for about seven cctaves in frequency.

70 the input terminals 16 and 17 of the circuit. The output Consider now the circuit of Fig. 2. In it an ideal current amplifier 10, connected to transfer signals from<br>left to right, is interconnected with an ideal voltage amplifier 11, connected to transfer signals from right to left. The input terminals 12 and 13 of the current amplifier 10 are connected in series with the output ter minals 4 and 5 of the voltage amplifier 11 and with terminals 18 and 19 of the current amplifier 10 and the input terminals 20 and 21 of the voltage amplifier 11 are connected in parallel with the output terminals 22 and 23 of the circuit. In other words, the amplifiers are connected together in the specified manner to form a feedback loop. In consequence, the input current  $i_1$ of the circuit is equal to the input current of the current -5 amplifier 10, and the input voltage of the amplifier 11 is the output voltage  $e_2$  of the device. The ideal current amplifier 10 has a constant ratio  $K_i$  of output current  $i_0$  to input current  $i_1$ , i.e.:

$$
\frac{i_0}{i_1} = K_1
$$
 (3) 10

An ideal current amplifier has a zero input resistance so that its insertion in the circuit does not affect the ent solely upon the input current. Since, by hypothesis, the output current  $i_0$  depends only on input current,  $i_1$ , it is independent of output voltage,  $e_2$ , that is, current to be measured and the output current is depend- 15

$$
\left(\frac{\mathbin{\grave{O}} i_0}{\mathbin{\grave{O}} e_2}\right)_{i_1=\text{constant}}
$$

vanishes, and its reciprocal, the output impedance

$$
\Big(\frac{\mathfrak{d} e_2}{\mathfrak{d} i_0}\Big)_{i_1=\text{constant}}
$$

is infinite. Accordingly, the ideal current amplifier 10 may be characterized by a zero input impedance, an infinite output impedance, and a constant gain factor. By itself it is both asymmetrical and unidirectional; a current applied to the output does not generate a current at the input. 25 30

Similarly, the ideal voltage amplifier 11 has a constant ratio  $K_e$  of output voltage  $e_0$  to input voltage  $e_2$ , i.e.:

$$
\begin{array}{c}\n e_0 \\
e_2 = K_e\n \end{array}
$$
\n(4)  $\begin{array}{c}\n 3\n \end{array}$ 

Since output voltage  $e_0$  depends only on input voltage  $e_2$ , the output impedance

$$
\left(\frac{\mathfrak{d} e_0}{\mathfrak{d} i_1}\right)_{e_2=\text{constant}}
$$

vanishes. Additionally, since a voltage amplifier prefer ably should not load the source of input voltage, its input impedance is preferably infinite. Accordingly, the ideal voltage amplifier  $11$  is characterized by an infinite  $45$ input impedance, a Zero output impedance, and a con stant gain factor. It is also asymmetrical and unidirec tional. These characteristics of ideal amplifiers must hold whether the gain factors are greater or less than unity. Thus, as used in this specification, and in the 50 appended claims, the input and output terminals of voltage amplifiers and of current amplifiers are designated with respect to impedance levels rather than signal levels.

It will be apparent that in Fig. 2 the output current  $i_0$  of the current amplifier 10 is the total output current  $55$  $i_2$  of the device, i.e.:

$$
i_0 \equiv i_2 \tag{5}
$$

and the output voltage  $e_0$  of the voltage amplifier 11 is equal to the voltage input  $e_1$  of the device, i.e.:

$$
e_0 \equiv e_1 \tag{6}
$$

Accordingly, the device of Fig. 2 is governed by the following relations:

$$
\frac{e_2}{e_1} = \frac{1}{K_e}
$$
\n
$$
\frac{i_2}{i_1} = K_i
$$
\n(7)\n(8)

$$
\quad \text{and} \quad
$$

$$
\frac{e_1}{i_1} = K_e K_i \frac{e_2}{i_2}
$$
 (9)

 $K_1$  and  $K_e$ , being gain constants of the amplifiers, may be selected as a matter of design choice and made 75 4.

variable by well known expedients. Four cases are of interest:<br>Case 1.—If  $K_e = K_i = N = a$  positive and real constant.

then the circuit functions as an ideal, close-coupled transformer. The transformer neither consumes nor generates power. Then

and 
$$
e_1 = Ne_2, i_2 = Ni_1
$$
 (10)

20

$$
\frac{e_1}{i_1} = N^2 \frac{e_2}{i_2} \tag{11}
$$

moreover, instantaneous power in $=$ 

$$
e_1 i_1 = \frac{1}{N} e_1 \cdot N i_1 = e_2 i_2 \tag{12}
$$

 $\equiv$ instantaneous power out.

Case 2.—If  $K_e \neq K_i$ , but both are positive and real, the general terminal Relations 7, 8 and 9 still hold out:

$$
0 \ \ \text{instantaneous power in} = e_1 i_1 = K_e e_2 \frac{i_2}{K_1} = \frac{K_e}{K_1} e_2 i_2
$$

$$
= \left(\frac{K_e}{K_i}\right)
$$
 (power out) (13)

(13) and power out may be greater or less than power in, depending upon the ratio  $K_e/K_i$ ; the transformer may consume power or act as a source of power.

- Case 3.—If  $K_i$  and  $K_e$  are real, and either (but not both) is negative, then the transformer functions as a negative, impedance converter, transforming a positive impedance at the other pair of terminals; i.e., the transformer changes the sign of a given impedance  $R \rightarrow -R$
- 35 for resistive loads; and  $(r+ix) \rightarrow -(r+ix)$  for reactive loads. In this case the transformer circuit supplies power to the driving source.

Case 4.-If  $K_i$  and  $K_e$  are complex quantities; i.e., if the amplifiers exhibit phase shift, then

$$
K_i = |K_i|e^{j\theta_i} \tag{14}
$$

$$
K_e = |K_e|e^{j\theta_e} \tag{15}
$$

and the complex voltages, currents and impedances may be manipulated by adjusting the phase characteristics of the amplifiers. If:

$$
e_1 = |e_1| e^{j\theta s_1}, e_2 = |e_2| e^{j\theta s_2}
$$
  
\n
$$
i_1 = |i_1| e^{j\theta i_1}, i_2 = |i_2| e^{j\theta i_2}
$$
\n(16)

then

40

$$
e_1 = |K_e|e^{j\theta_e}|e_2|e^{j\theta_{e_2}} = |K_e||e_2|e^{j(\theta + \theta_{e_2})}
$$
 (17)

$$
i_2 = |K_i| \epsilon^{j\theta_i} |i_1| \epsilon^{i\theta_{\bullet_1}} = |K_i| |i_1| \epsilon^{i(\theta_i + \theta_{\bullet_2})}
$$
(18)

and

$$
e_1/i_1 = |K_e||K_i|e^{j(\theta_\bullet + \theta_i)}(e_2/i_2)
$$
 (19)

60 amplifiers, various effects can be produced. The first  $65$  where  $\theta_2$  is the phase angle of the load impedance, then By properly adjusting the phase characteristics of the three cases are just particular forms of this fourth and general case. For example, a complex load impedance may be made to appear as its complex conjugate at the other terminals if:  $|K_i|$   $|K_e|=1$  and  $(\theta_e+\theta_i) = -(2\theta_2)$ 

or 
$$
|Z_1|e^{j\theta_1} = |K_e||K_i|e^{j(\theta_1+\theta_1)}|Z_2|e^{j\theta_2}
$$
 (20)

70

$$
|Z_1|\epsilon^{j\theta_1} = |Z_2|\epsilon^{-j\theta_2} = \text{conjugate of } |Z_2|\epsilon^{j\theta_2} \tag{21}
$$

By this choice of phase characteristics, the sign of the imaginary or reactive term of the load impedance has been changed. A similar choice of phase can be made to change the sign of the real part (or resistive come ponent). 5

Fig. 3 represents a device having output and input impedances more representative of practical amplifiers, when connected as described for the device of Fig. 2.<br>Here the circuit is driven from a source  $e_s$  with self Here the circuit is driven from a source  $\epsilon_{\rm s}$  with self impedance  $Z_1$  connected to the primary side, and a load impedance  $Z_2$  is connected across the secondary terminals.

A resistor 38 of value R is connected between input terminals 32 and 33 of the current amplifier 30. Re sistor 39 of value  $r_1$  is connected effectively in series 10 with output terminals 34 and 35 of the voltage amplifier 31, and the output resistance 40 of value  $r_2$  shunts the output terminals 36 and 37 of the current amplifier 30.  $Z_1$  represents the source impedance of the circuit driving the primary with a source voltage  $e_s$  as seen from 15 the input terminals 16 and 17 of the device.  $Z_2$  represents a secondary circuit load impedance as seen from the output terminals 22 and 23 of the device. In Fig. 3 (where the circuit is assumed to be driven from the primary side and loaded on the secondary side), the out-  $20$ put  $i_0$  of the current amplifier is not exactly identical to secondary current  $i_2$ , and the output  $e_0$  of the voltage amplifier is not exactly equal to the primary voltage  $e_1$ , but rather:

and

and

$$
\frac{e_2}{i_2} = Z_2 \tag{25}
$$

 $e_1=e_0+i_1(r_1+R)$  (22)<br>  $e_2 = +K_2e_2$  (23)

Wherefore, combining Equations 22 through 25, it fol lows that the input terminals present an apparent im pedance given by:

 $e_0 = +K_e e_2$ 

 $+K_i i_1 = i_2 + \frac{e_2}{r_2}$ 

$$
\frac{e_1}{i_1} = \frac{K_1 \left[K_e Z_2 + \frac{i_1}{i_2} (r+R)\right]}{1 + \frac{Z_2}{r_2}}
$$
\n(26)

if

then

and

 $\frac{1}{K}$ , or  $i_2 \cong K_i i_1$  (29)

and since

Further, if

or

$$
\frac{Z_2}{r_2}{\ll}1
$$

Equation 26 simplifies to:

$$
\frac{e_1}{i_1} \cong K_i K_e Z_2 + (r_1 + R) \tag{30} 60
$$

 $(r_1 + R) \leq \leq K_i K_e Z_2$  (31)

$$
e_1/i_1 \cong K_i K_e Z_2 \tag{32}
$$
\nor

\n
$$
e_1 \cong K_e e_2 \tag{33}
$$

Essentially the same conditions apply when the circuit is driven from a source connected to the secondary ter minals and a load impedance is connected to the pri mary terminals. Equations 27 and 31 means that the output impedance  $(r_2)$  of the current amplifier must be high compared to the impedance level of the secondary circuit, and the sum of the output impedance 75 70

 $(0, t_1)$  of the voltage amplifier and the input impedance (R) of the current amplifier must be low compared with the impedance reflected at the primary terminals. Both of these conditions can be easily realized to a satisfac tory degree in practical circuits, of which Fig. 5 is an example.

Many varieties of amplifiers may be employed in practicing the invention; but stability and the range of useful operation will depend upon the degree to which the amplifiers employed have the characteristics of ideal

 $(22)$   $25$  $(24)$  30 Fig. 4 is a partial schematic diagram of an embodiment comprising a voltage amplifier 31 represented as the alternating current equivalent circuit for a triode tube, and a current amplifier 30 represented by a con ventional alternating current equivalent circuit 50 for a pentode tube, together with the resistor R and a phase inverting stage 55, proportioned to provide a voltage gain  $-K_3$ . This circuit will be recognized as equivalent to Fig. 2 wherein  $K_1$  is replaced by the product R  $K_2$ .  $K_3$  and  $K_6$  is replaced by  $K_1$ . To permit grounded operation of both amplifiers, the points 33 and 34 are grounded. The input to the current amplifier, appearing across the resistor R is, then, in opposite phase to the output of the voltage amplifier. Accordingly, an the output of the voltage amplifier. additional phase reversal in one of the amplifiers, as indicated by the negative sign of  $(-K_3)$ , is necessary to correspond to the feedback arrangement of Figs. 2 and 3. Both the triode and pentode stages of Fig. 4 produce phase inversions of 180 degrees so that the net effect of the circuit is exactly identical to that of the circuit in Fig. 3.

35 so that The device exhibits the characteristics of a trans former with turns-ratio N when the factors are adjusted

$$
K_1 = K_2 K_3 R = N \tag{34}
$$

40 tion in equivalent turns-ratio. The control of amplifier gain factors to achieve wide variations of N may be 45 and secondary connections. Variations of  $K_1$  and the other factors in a manner to preserve the Relations 34 result in a corresponding varia tion in equivalent turns-ratio. The control of amplifier gain factors to achieve wide variations of N may be accomplished by means well known in the art. As a practical matter there is usually no need for N to be less than unity since one may simply reverse the primary

50 The maximum value of N that can be achieved is determined largely by stability margins of the circuit as a feedback device. N's in the range from one to ten have been attained with relatively little attention to the phase characteristics of the circuit.

Fig. 5 is a schematic diagram of an artificial trans former which has been employed to couple passive net-<br>works in connection with electrical analog studies of

55 The voltage amplifier 31 comprises the pentode  $V_1$  in tandem with the cathode follower  $V_2$ . The current amacoustical systems.<br>The voltage amplifier 31 comprises the pentode  $V_1$  in plifier comprises the two pentode stages  $V_3$  and  $V_4$  which amplify the voltage produced across the resistance, R, by the input current. As in the circuit of Fig. 3, grounded operation of the amplifiers requires that the output of the voltage amplifier and input of the current amplifier be connected series opposed rather than series aiding. The 65. the voltage amplifier at point 41. Each amplifier is thus connected series opposed rather than series aiding. output of the current amplifier appearing at point 37 is connected through coupling capacitors to the input grid of connected in feedback relation to the other as in Fig. 4<br>Both tubes  $V_1$  and  $V_3$  are of the remote cutoff type to provide a convenient means for varying the gain constants (i.e. 'turns-ratio") in response to a variable bias control voltage. The transconductance of  $V_4$  is maintained substantially constant by operating the stage in a conventional maner with fixed bias. Variation of the turns-ratio is ef fected by jointly varying the gain constants  $K_1$  and  $K_3$  by means of the bias voltages  $e_{c1}$  and  $e_{c2}$ , respectively. The circuit is designed so that the current and voltage gains.

$$
\begin{array}{c} \mathbb{E} \left( \mathcal{B} \right) \\ \mathbb{E} \left( \mathcal{A} \right) \leq \mathbb{E} \left( \mathcal{A} \right) \end{array}
$$

 $Z_2 \leq \leq r_2$  (27)

 $\frac{1}{r_2} \ll t_2$  (28)

5

are maintained equal for a reasonably wide range of N, the equivalent control functions  $K_e$  versus  $e_{c1}$  and  $K_i$  versus  $e_{c2}$  are made to "track" and by proper adjustment of the two potentiometers 61, 62, the biases  $e_{c1}$  and  $e_{c2}$ can be derived from the single control voltage source 69.

The conventional fixed turns-ratio transformer 63 shown connected to the input of the device is a useful adjunct to the circuit in that it permits "grounded" operation of both primary and secondary circuits, as shown.<br>Fig. 6 represents a telephone-type repeated amplifier 71

feeding a long section of transmission ine 72 (for ex ample, a section of undersea cable). To optimize the power transmitted to the receiving end of the line, and to minimize objectionable reflections of energy due to im looking into the cable (i.e. essentially the characteristic impedance of the cable,  $Z_0$ , if it is a long section) matched in magnitude to the internal impedance,  $R_i$ , of the signal source (or repeater amplifier). This match usually is effected by a transformer having a turns-ratio equal to  $N$  20 where, recalling Equation 2a: 10 pedance miscatches, it is desirable to have the impedance 15

$$
N = \left[\frac{|R_i|}{Z_0}\right]^{1/2} \tag{35}
$$

Often, however, because of variations in environmental 25 conditions (such as temperature changes caused by ocean currents) the impedance looking into the sending end of the cable may vary continuously with time. (The im pedance of the source usually is constant and usually is resistive. In general  $Z_0$  also is predominantly resistive.) If a proper impedance match, i.e.  $R_1=N^2|Z_0|$ , is to be maintained at all times, the turns-ratio of the transformer should be varied so that  $N^2|Z_0|$  is always constant and equal to  $R_i$ . Continuous variation of the turns-ratio can only be approximated with conventional close-coupled  $35$ only be approximated with conventional, close-coupled, tapped transformers. With the electronic transformer of the invention, however, such continuous variation of N is possible. 30

The circuit of Fig.6 is an illustration of how such an impedance match may be maintained constantly and automatically. The long transmission line 72 with charac teristic impedance  $Z_0$  is to be fed from the source 71 with constant resistive internal impedance, R<sub>i</sub>. The variable transformer is used to match  $Z_0$  to  $R_i$ . To do this, an impedance bridge continuously makes a measurement of the  $\frac{45}{15}$  output. impedance  $|Z_x|$ , namely the parallel combination,

### $R_iN^2Z_0$  $R_1 + N^2 Z_0$

of the source  $\pi$  and the load as seen through the trans- $\delta\theta$ former. The measurement is made at a frequency not used for communication, for example, in a guard band between two speech channels in a carrier transmission system. The impedance bridge is arranged to be balanced when  $Z_x$  is equal to  $R_i/2$ . When unbalanced, a smoothed error signal e proportional to  $(|Z_x|-R_i/2)$  is developed by the detector 73. This control voltage may be additively combined with a manually set voltage  $E_N$  (set originally to give the proper match) and the sum,  $e_c$ , is used to determine the turns-ratio of the transformer. This control loop acts to maintain the proper impedance match when  $Z_0$  varies by automatically adjusting the turns-ratio N. **<sup>00</sup>.** 

The control circuit functions in the following manner, Suppose  $E_N$  is set to give the right value of N when the line is first connected, but, for some reason,  $Z_0$  is later caused to increase appreciably. Then, recalling Equation 35,  $N^2|Z_0| > R_i$  and mismatch occurs. Simultaneously, however, the parallel combination of  $N^2|Z_0|$  and R<sub>i</sub> also increases so: **BK** 

$$
|Z_x| > R_i/2 \tag{36}
$$

$$
\epsilon = (|Z_x| - R_i/2) > 0 \tag{37}
$$

The resulting increased correction voltage  $(e+E_N)$  reduces the turns-ratio, N, of the transformer until 75

8 to the second contract of  $\sim$  $N^2|Z_0| \approx R_i$ . (The preciseness with which the adjustment is made is dependent upon the gain around the control loop.)

The invention has been described above as a substitute for a simple variable coupling transformer and as applied to match impedances in a transmission system. Many other applications of these principles may be found which fall within the scope of the invention, the particular embodiments described above being ones in which the invention performs a function peculiar to its nature and produces results previously unobtainable except through the use of more complex and otherwise less satisfactory apparatus.

What is claimed is:<br>1. An impedance transformer comprising a voltage amplifier having two input terminals and two output terminals, a current amplifier having two input terminals and two output terminals, the input terminals of said current amplifier being connected in series relationship to the output terminals of said voltage amplifier, and the input terminals of said voltage amplifier being connected in parallel with the output terminals of said current am plifier.

2. A transformer as defined in claim 1 wherein said voltage amplifier comprises an electron tube amplifier, and wherein said current amplifier comprises an electron tube amplifier.

3. A transformer as defined in claim 2 wherein said voltage amplifier comprises a variable mu tube input stage and an output stage in cathode follower connection connected in tandem therewith, and wherein said current amplifier comprises a variable mu tube input stage and an emplifier comprehensive stage connected in tandem amplifier relationship with said second named variable mu tube.

4. A transformer in accordance with claim 3 wherein said variable mu tubes are resistively connected to a voltage source arranged to alter the current and voltage amplification ratios equally and synchronously.

40 amplifier having an input and an output, and a current 5. An impedance transformer comprising a voltage amplifier having an input and an output, and a current amplifier having an input and an output, said voltage amplifier input being connected in parallel with said current amplifier output, and said current amplifier input being connected in series with said voltage amplifier

6. An artificial transformer comprising a current amplifier having an input and output, and a voltage amplifier having an input and an output, said amplifiers having equal gain factors and the input of each amplifier being amplifier is in feedback relation to the other.

7. An artificial transformer comprising a voltage am having an input and an output, said amplifiers having<br>the same amplification ratio, said voltage amplifier input<br>being connected in parallel with said current amplifier<br>output, and said current amplifier input being connec

O 7 and unicontrol means to adjust said amplification ratio 8. In combination, apparatus in accordance with claim whereby the effective turns-ratio of said artificial trans former is varied.

9. Apparatus in accordance with claim 1, wherein said electron tube amplifiers of the variable mu type, said tubes being connected to adjustable sources of bias volt age, whereby the amplification ratios of said current am plifier and said voltage amplifier may be equalized.

70 sources of bias voltage are simultaneously variable there 10. Apparatus in accordance with claim 9 wherein said by changing the effective turns-ratio of said transformer.<br>11. The apparatus in accordance with claim 10 where-

in said bias sources comprise a pair of potentiometer resistors connected in parallel across a common source of variable voltage, one resistor being tapped to supply

and

bias for said voltage amplifier, the other resistor being tapped to supply bias for said current amplifier.<br>12. In combination, a source of electrical communication signals; a transmission line terminated at its distal

end by substantially its characteristic impedance; a  $\tilde{\mathbf{p}}$ variable artificial transformer having input terminals, out said source and the proximal end of said transmission line to match the impedance of said source to that of said line; an impedance bridge connected at the common 10 terminals of said source and said transformer to measure the apparent parallel impedance at said common termi nals; and a detector converting the error signal of said bridge to a control signal connected to a control terminal of said transformer whereby the apparent turns-ratio of 15 said transformer is adjusted to maintain a proper termi nation of said proximal end.

13. In combination, an artificial transformer having in put terminals, output terminals, and control terminals, comprising a current amplifier and a voltage amplifier, 20 the input of said current amplifier and the output of said voltage amplifier being in series with said input terminals, the output of said current amplifier and the input of said voltage amplifier being in parallel with said output ter minals, and said control terminals being connected to 25 control elements of said amplifiers to alter the current and voltage amplification ratios equally and synchronous ly; a source of electrical communication signals con nected to the input of said transformer; a transmission line terminated at its distal end by substantially its charac- 30

teristic impedance and at its proximal end connected to bridge connected at the junction of said source and said transformer to measure the apparent parallel impedance at said juncture; and a detector converting the unbalanced signal of said bridge to a control signal connected to said control terminals whereby the apparent turns-ratio of said transformer is adjusted to maintain a proper termi

14. A transformer as described in claim 2 wherein said voltage amplifier comprises a variable mu pentode electron tube and a triode tube connected in tandem<br>therewith in cathode follower connection, and wherein said current amplifier comprises a variable mu pentode tube the control grid of which is connected to said input terminals, and an output pentode tube connected in tandem amplifier relationship with said second named variable mu pentode tube, the anode of said output tube being connected to said output terminals.

15. A transformer in accordance with claim 14 where in said variable mu pentodes are resistively connected to current and voltage amplification ratios equally and syn-<br>chronously.

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