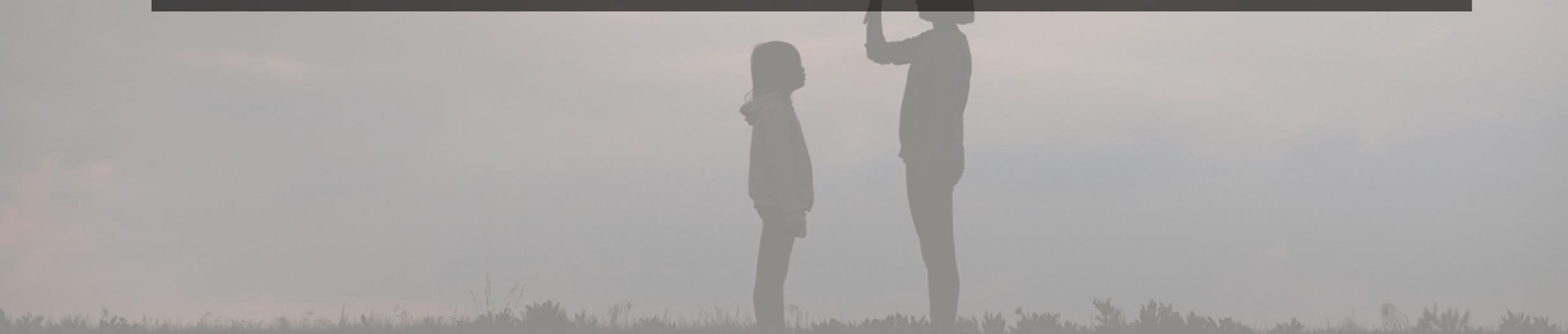
REASONING A BOUT PROBABLITY

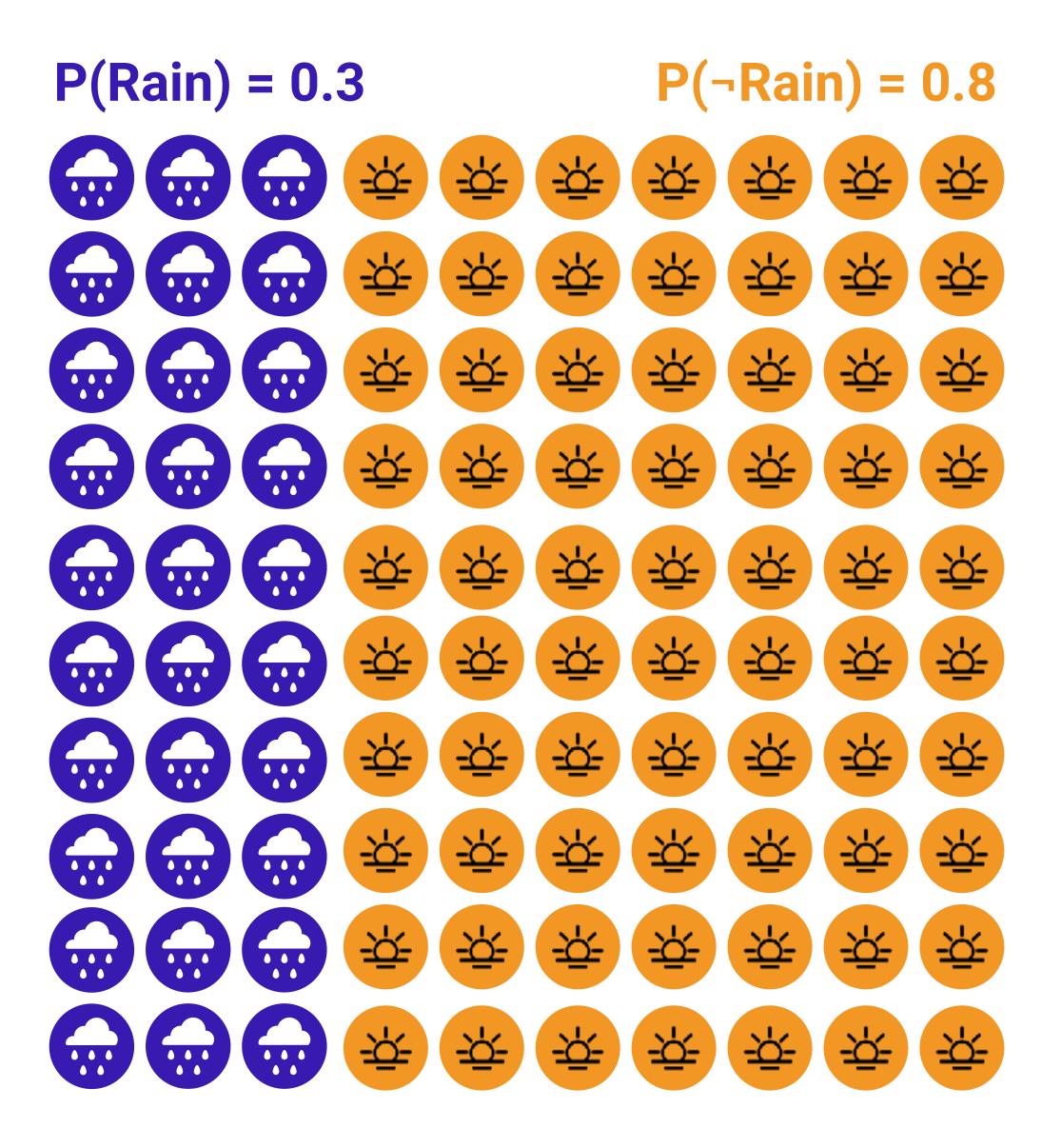




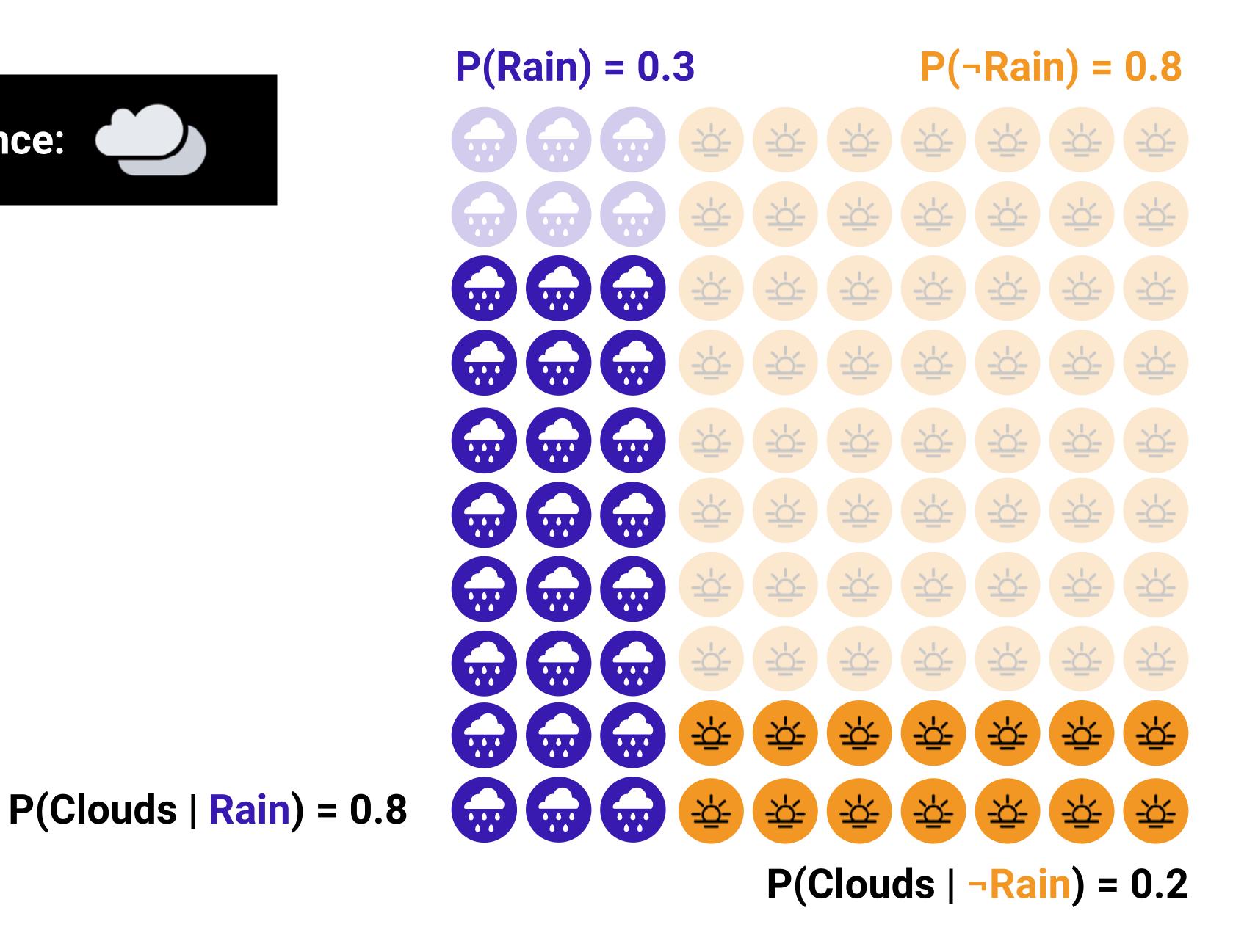


P("Rain") = 0 absolutely certain that it won't rain P("Rain") = 1 absolutely certain that it rains



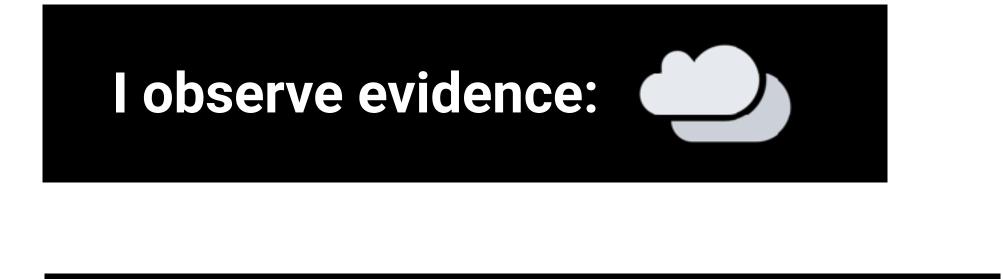


I observe evidence:

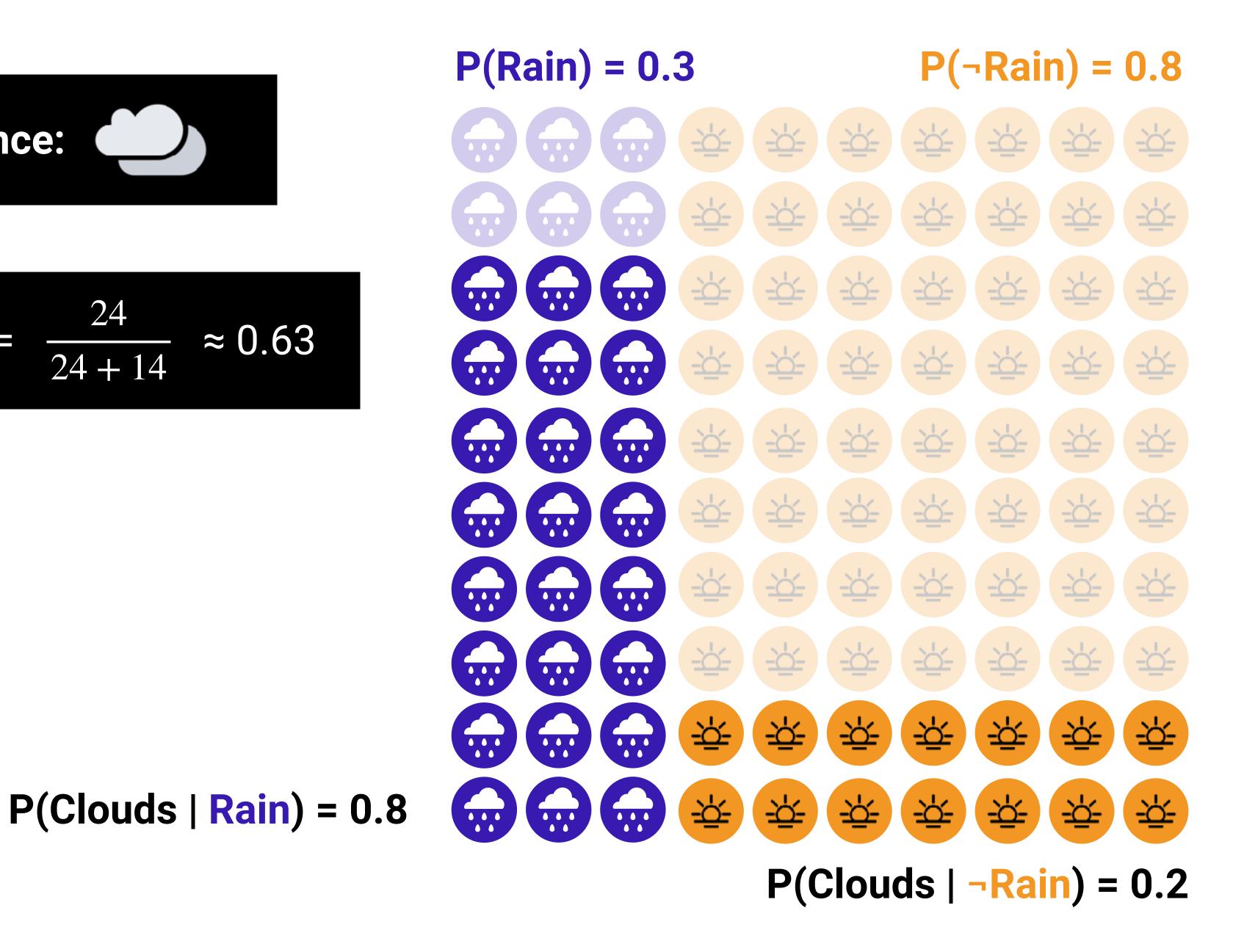


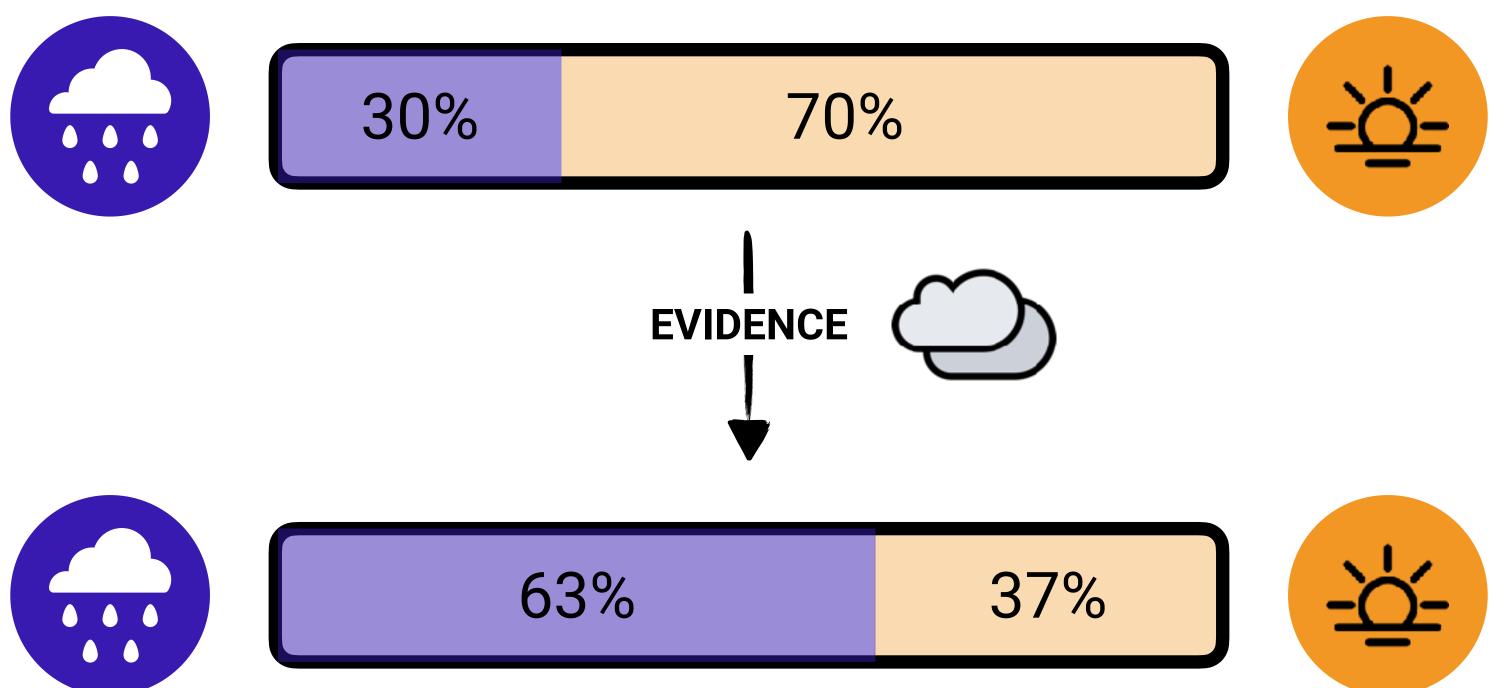
DO I CHANGE MY GUESS?

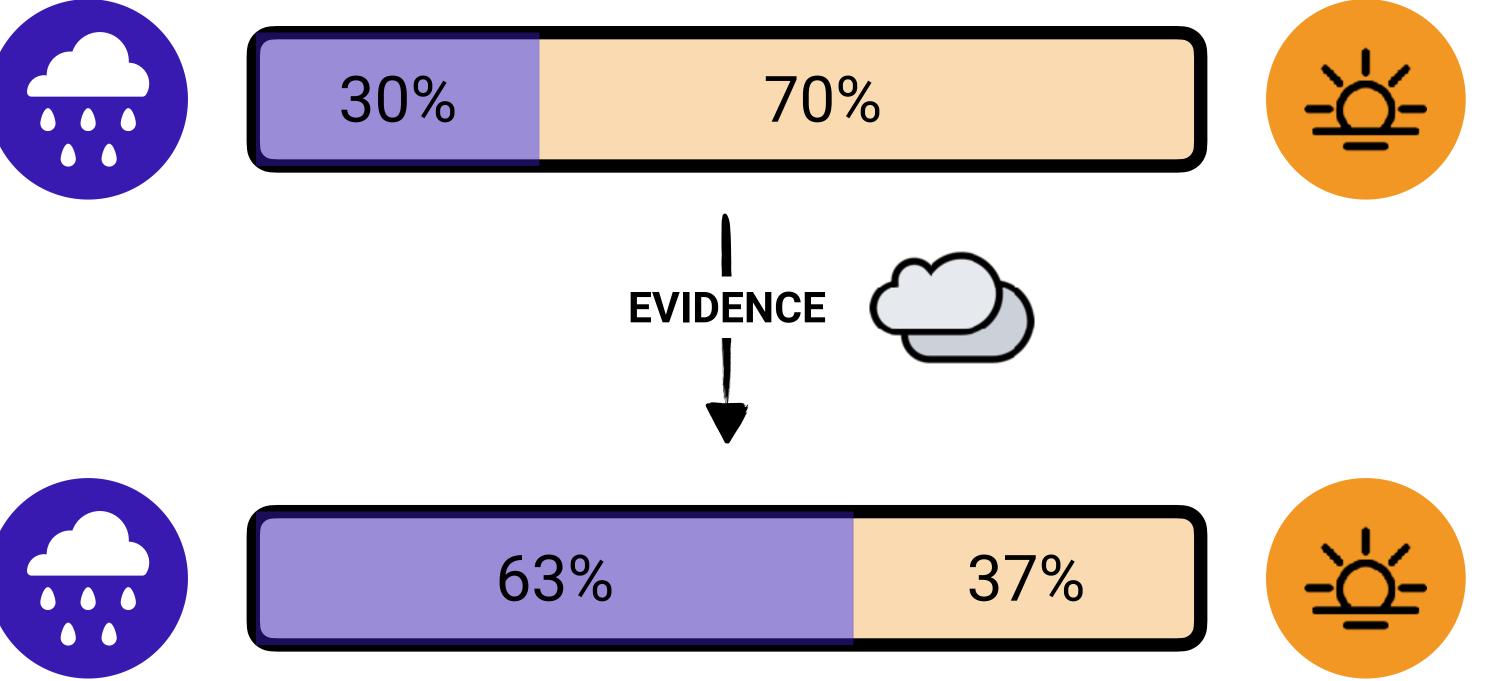




$$P(\text{Rain} | \text{Clouds}) = \frac{24}{24 + 14} \approx 0.63$$







You have a hypothesis: You have observed evidence:



There are dark clouds It's gonna rain

When to use Bayes' theorem

You want to know:

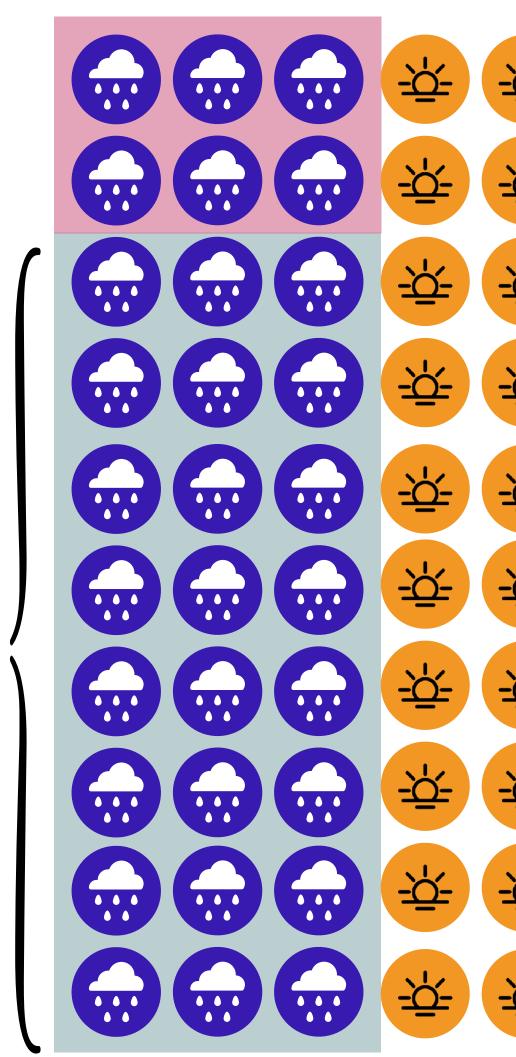
P(H | E)hypothesis given evidence

"Prior" → *P*(Hypothesis) = 30 / 100 = 0.3



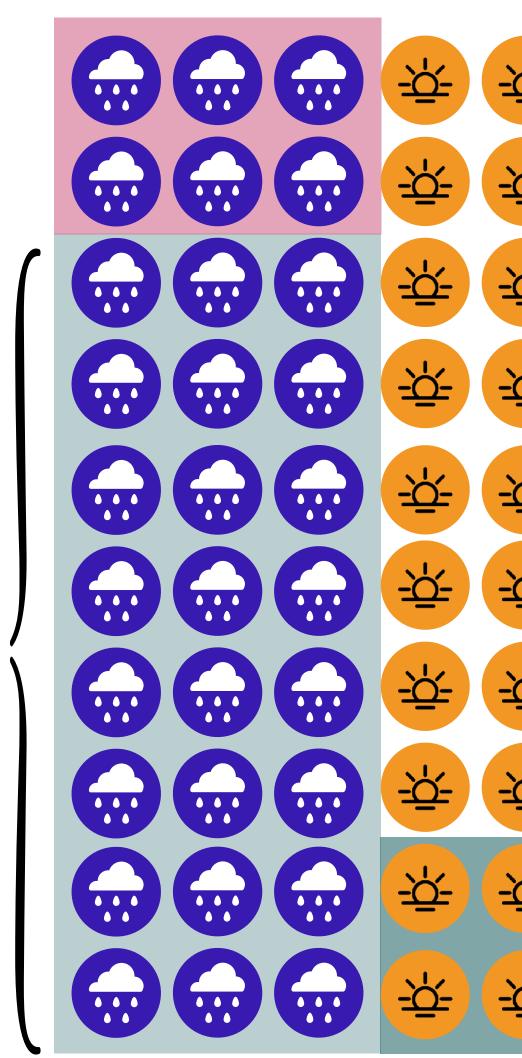
"Prior" → P(Hypothesis) = 30 / 100 = 0.3

"Likelihood" P(Evidence | H) = 0.8

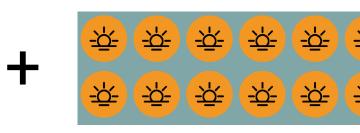


"Prior" → P(Hypothesis) = 30 / 100 = 0.3

"Likelihood" P(Evidence | H) = 0.8



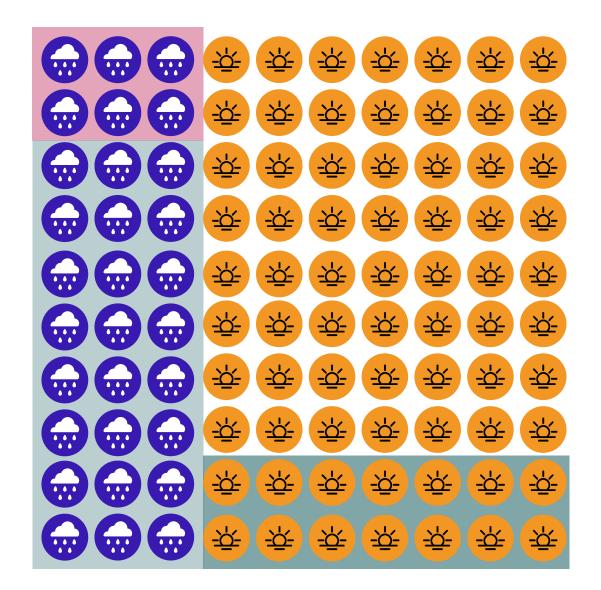
 $\bigcirc \bigcirc \bigcirc \bigcirc \bigcirc$ $\bigcirc \bigcirc \bigcirc \bigcirc \bigcirc$ $\bigcirc \bigcirc \bigcirc \bigcirc$ $\bigcirc \bigcirc \bigcirc \bigcirc$ $\mathbf{\mathbf{\Theta}}\mathbf{\mathbf{\Theta}}\mathbf{\mathbf{\Theta}}$ $\Theta \Theta \Theta$



P(H) = 0.3

P(H | E) =

P(E | H) = 0.8



"Prior" "Likelihood" P(H) P(E|H) $P(H)P(E|H)+P(\neg H)P(E|\neg H)$

 $P(\neg H) = 0.7$

 $P(E | \neg H) = 0.2$

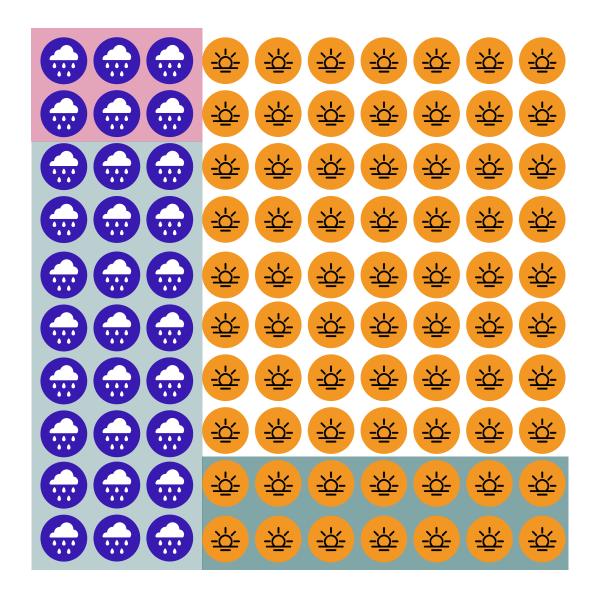


P(H) P(E|H)P(H | E) =*P*(E)



P(H) = 0.3

P(E | H) = 0.8



"Prior" "Likelihood" P(H) P(E|H) $P(H)P(E|H)+P(\neg H)P(E|\neg H)$

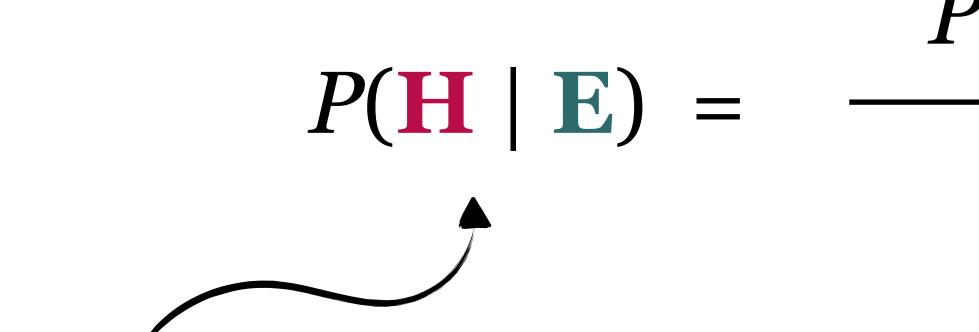
 $P(\neg H) = 0.7$

 $P(E | \neg H) = 0.2$

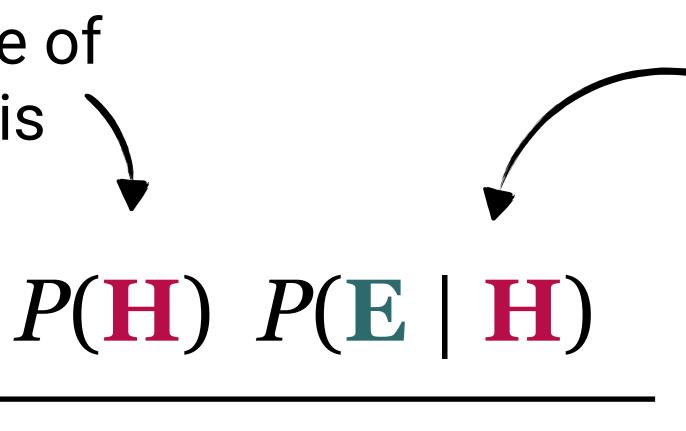


This is Bayes Theorem

prior: initial degree of belief in hypothesis



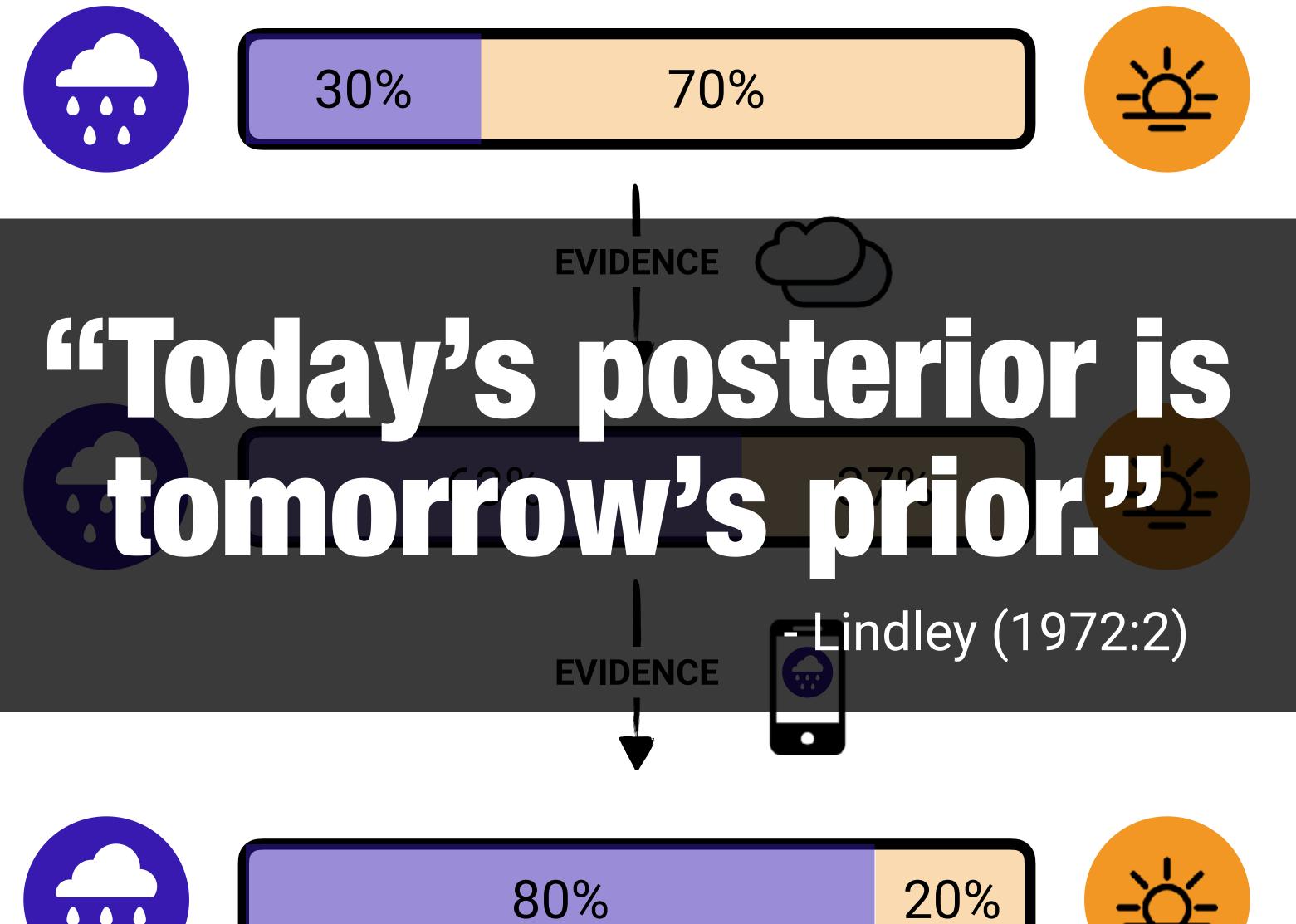
posterior: degree of belief in hypothesis, after seeing evidence

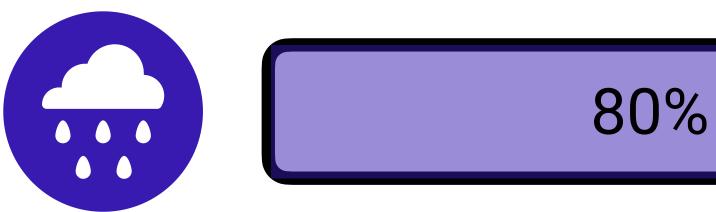


 $P(\mathbf{E})$

likelihood: the probability of the evidence given the hypothesis







-()-

DO I BRING MY UMBRELLA?



What is more likely?



Steve is very **shy and withdrawn**, invariably helpful but with very little interest in people or in the world of reality. A **meek and tidy soul**, he has a need for order and structure, and a passion for detail.

librarian





