

Predicting Dynamic Embedding Trajectory in Temporal Interaction Networks



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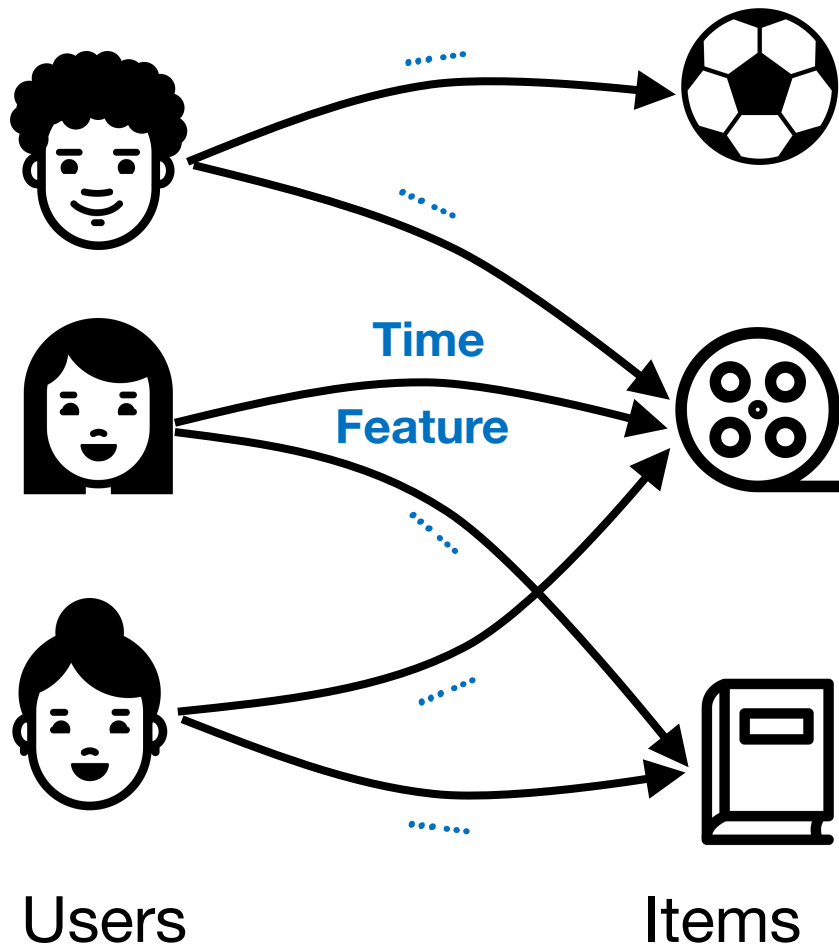
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Code and Data: <https://snap.stanford.edu/jodie>

Temporal Interaction Networks

Flexible way to represent time-evolving relations



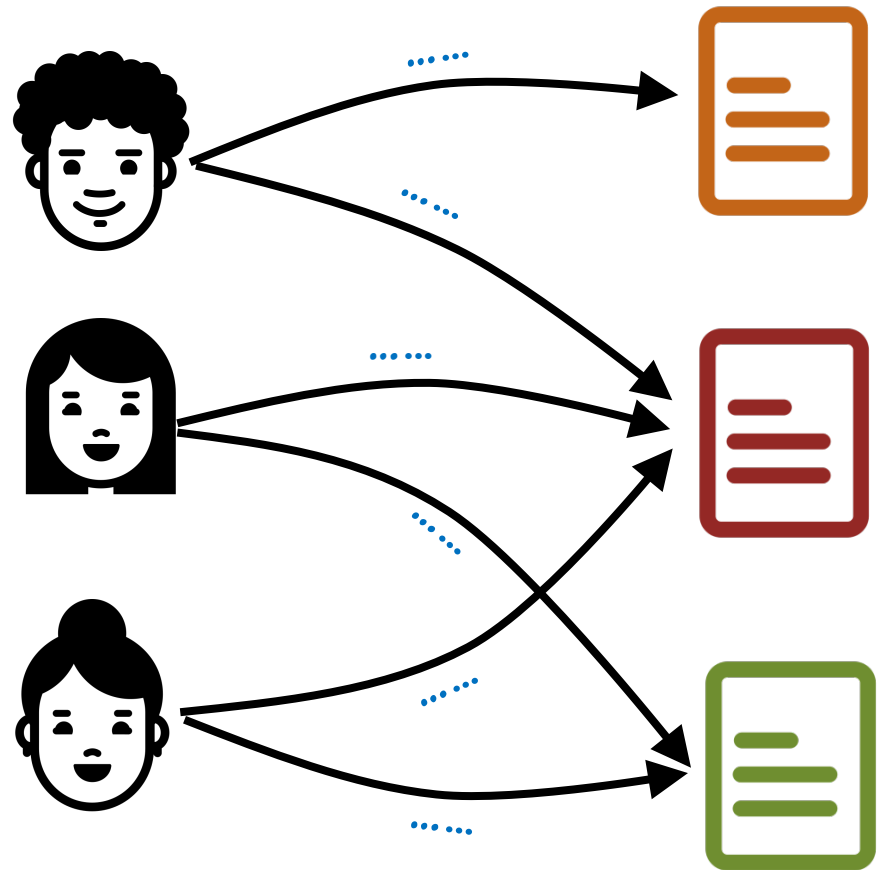
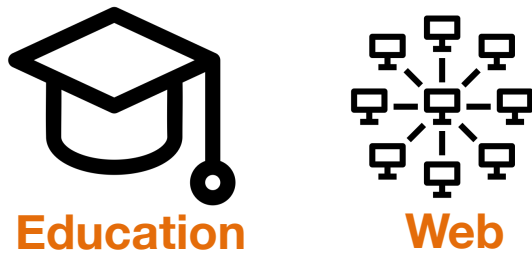
Represented as a sequence of interactions, sorted by time:

$$S_r = (u_r, i_r, t_r, f_r)$$

↑
↑
↑
↑
↑

interaction user item time features

Temporal Interaction Networks



Application domains

Accounts

Posts

Temporal Interaction Networks



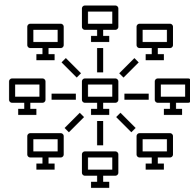
E-commerce



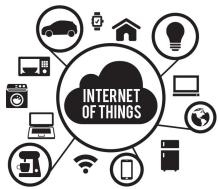
Social media



Education



Web



IoT



Finance



Students



Students



Students



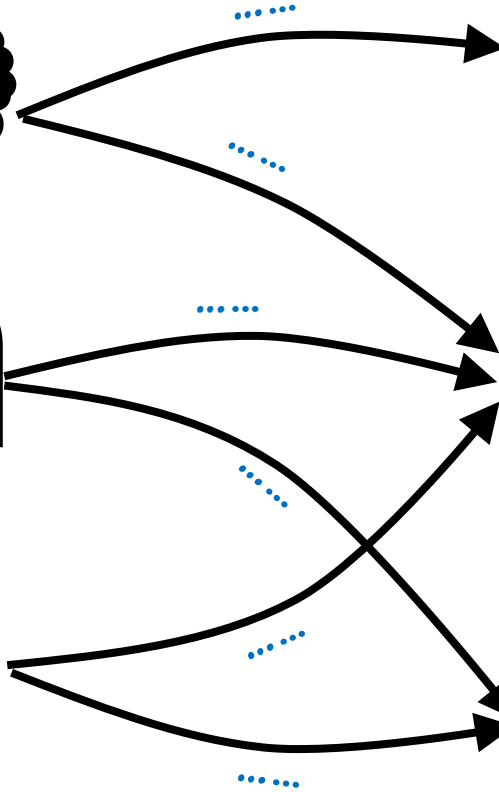
Courses



Courses



Courses



Application domains

Problem Setup

Given a temporal interaction network

$$S_r = (u_r, i_r, t_r, f_r)$$

\uparrow interaction \uparrow user \uparrow item \uparrow time \uparrow features

where $u_r \in \mathcal{U}, i_r \in \mathcal{I}, t_r \in \mathbb{R}^+, 0 < t_1 \leq \dots \leq T, f_r \in \mathbb{R}^d$

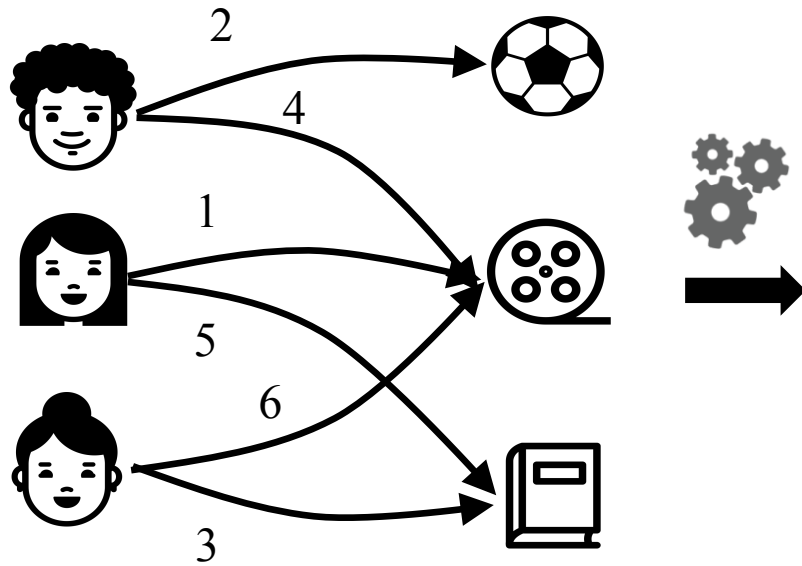
generate an embedding trajectory of every user

$$\mathbf{u}(\mathbf{t}) \in \mathbb{R}^n \quad \forall u \in \mathcal{U}, \forall t \in [0, T]$$

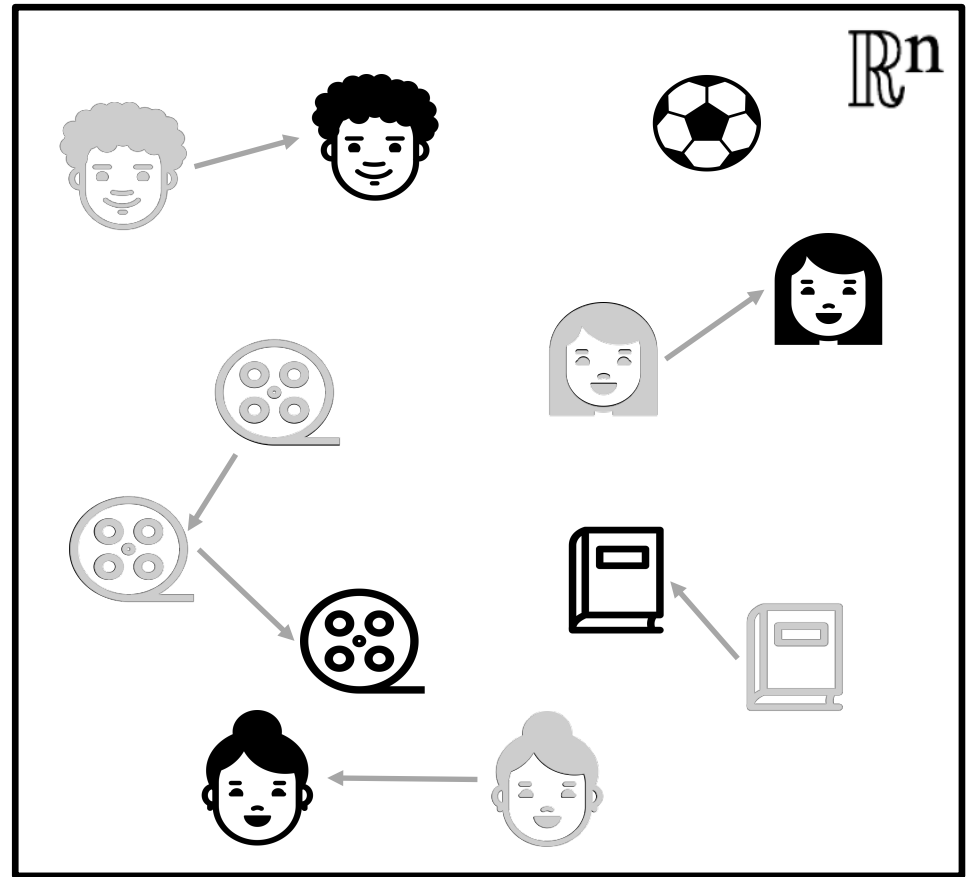
and an embedding trajectory of every item

$$\mathbf{i}(\mathbf{t}) \in \mathbb{R}^n \quad \forall i \in \mathcal{I}, \forall t \in [0, T]$$

Goal: Generate Dynamic Trajectory



Input: Temporal interaction network



Output: Dynamic trajectory in embedding space

Challenges

Challenges in modeling:

- **C1:** How to learn inter-dependent user and item embeddings?
- **C2:** How to generate embedding for every point in time?

Challenges in scalability:

- **C3:** How to scalably train models on temporal networks?

Existing Methods

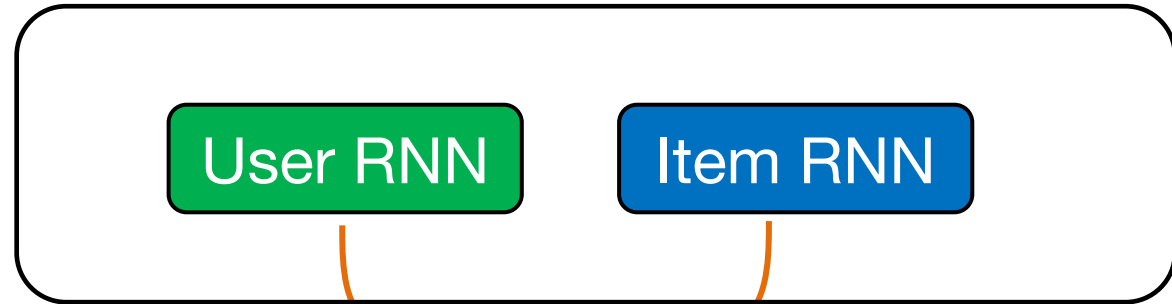
	C1 Co- influence	C2 Embed any time	C3 Train in batches
Deep recommender systems <ul style="list-style-type: none"> Time-LSTM (IJCAI 2017) Recurrent Recommender Networks (WSDM 2017) Latent Cross (WSDM 2018) 			✓
Dynamic co-evolution <ul style="list-style-type: none"> Deep Coevolve (DLRS, 2016) 	✓		
Temporal network embedding <ul style="list-style-type: none"> CTDNE (BigNet, 2018) 	✓		✓
Our model: JODIE	✓	✓	✓

Our Model: JODIE

JODIE: Joint Dynamic Interaction Embedding

- Mutually-recursive recurrent neural network framework

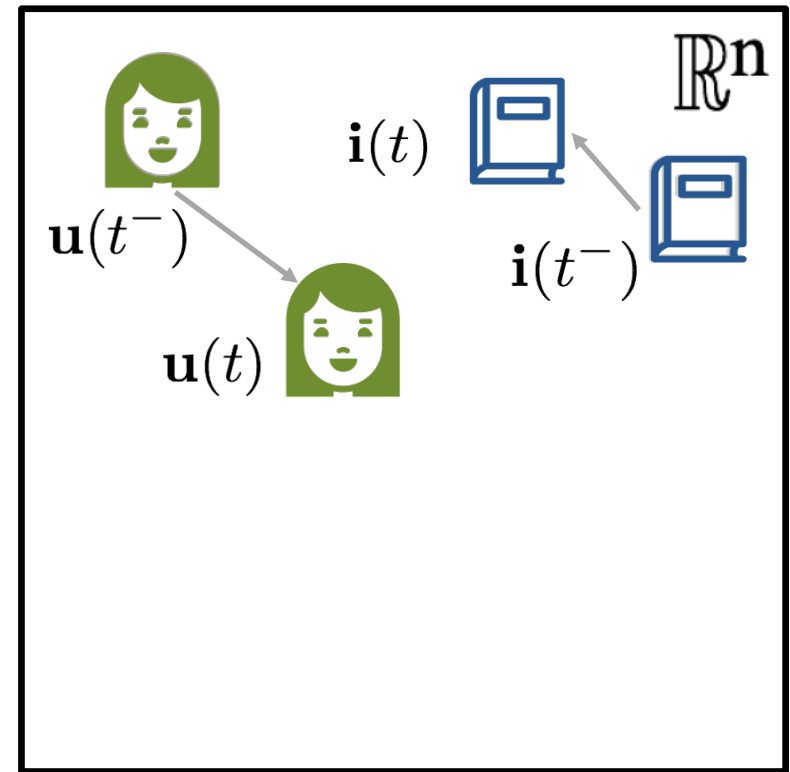
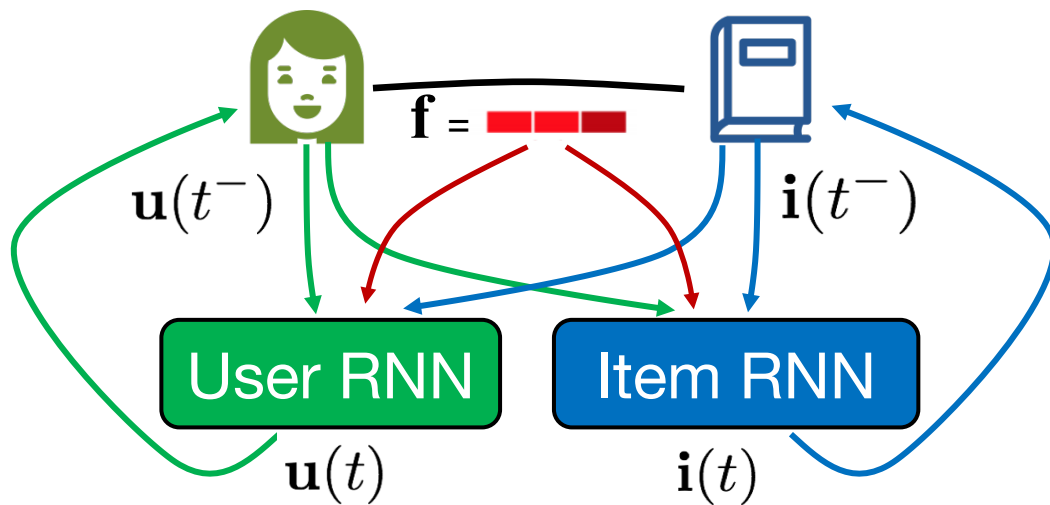
**Update
Component**



**Project
Component**



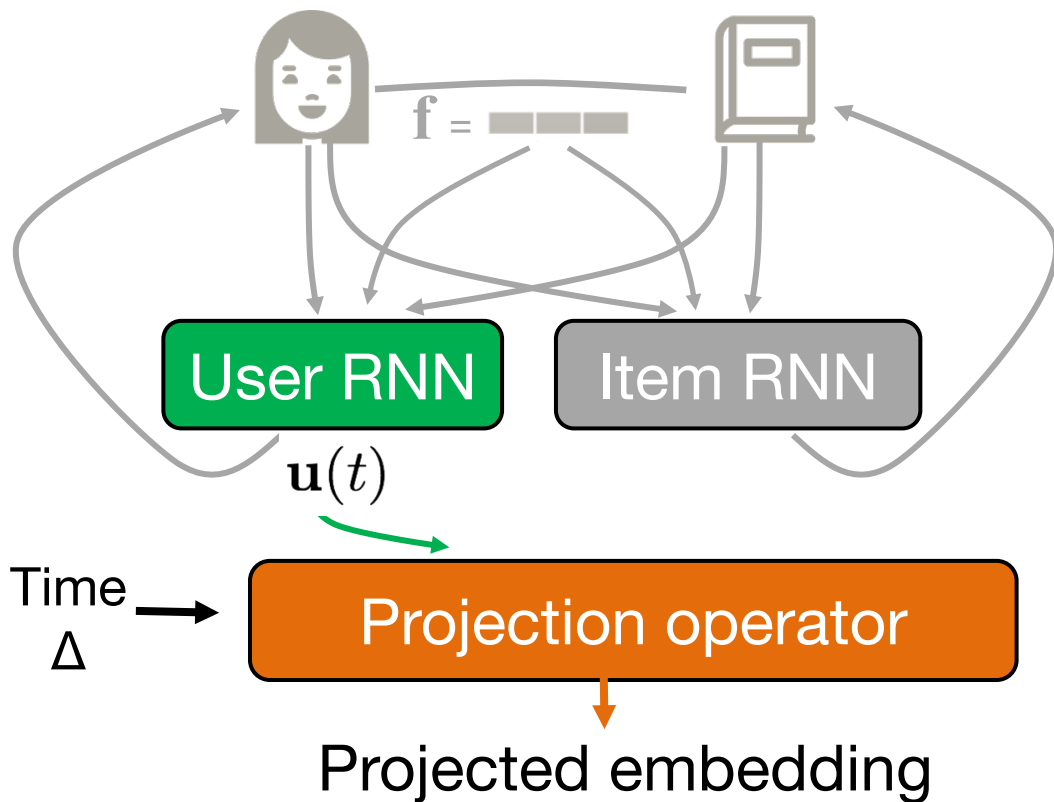
JODIE: Update Component



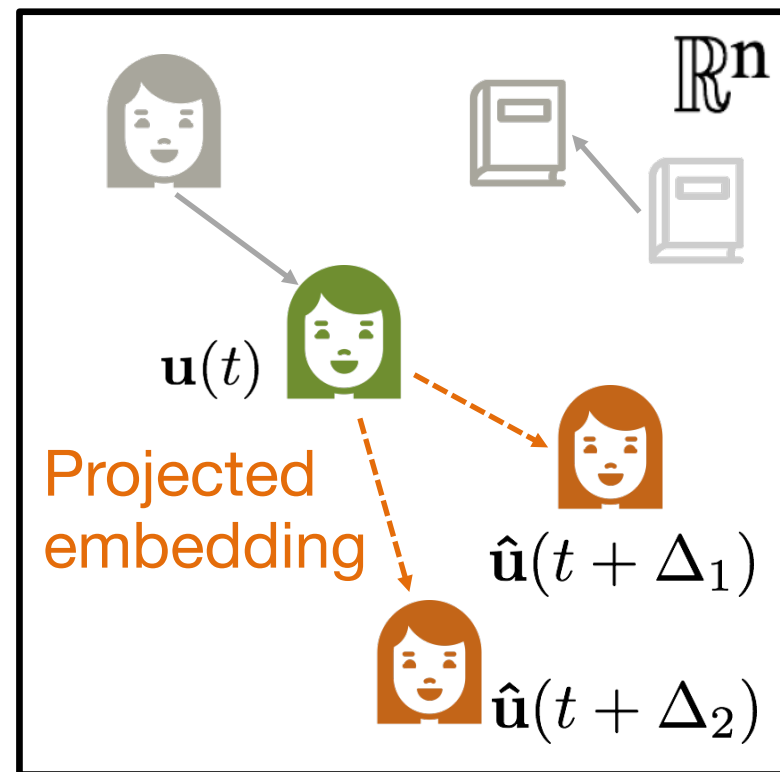
$$\left. \begin{aligned} \mathbf{u}(t) &= \sigma(W_1 \mathbf{u}(t^-) + W_2 \mathbf{i}(t^-) + W_3 \mathbf{f}) \\ \mathbf{i}(t) &= \sigma(W_4 \mathbf{i}(t^-) + W_5 \mathbf{u}(t^-) + W_6 \mathbf{f}) \end{aligned} \right\} \text{Weight matrices } W \text{ are trainable}$$

- All users share the User-RNN parameters. Similar for items.

JODIE: Project Component



$$\hat{u}(t + \Delta) = (1 + w \cdot \Delta) * u(t)$$



How can we predict the next item?

- Rank items using distance in the embedding space

Summary: JODIE Formulation

Update embeddings:

$$\mathbf{u}(t) = \sigma(W_1 \mathbf{u}(t^-) + W_2 \mathbf{i}(t^-) + W_3 \mathbf{f})$$

$$\mathbf{i}(t) = \sigma(W_4 \mathbf{i}(t^-) + W_5 \mathbf{u}(t^-) + W_6 \mathbf{f})$$

Project user embedding:

$$\hat{\mathbf{u}}(t + \Delta) = (1 + w \cdot \Delta) * \mathbf{u}(t)$$

Predict next item:

$$\tilde{\mathbf{j}} = W_7 \hat{\mathbf{u}}(t + \Delta) + B$$

Loss:

$$\sum_{S_r:(u,i,t,f)} \|\tilde{\mathbf{j}}(t) - \mathbf{i}(t^-)\|_2 + \lambda_U \|\mathbf{u}(t) - \mathbf{u}(t^-)\|_2 + \lambda_I \|\mathbf{i}(t) - \mathbf{i}(t^-)\|_2$$

Predicted next item is close to the real item embedding

Smoothness in evolving embeddings

Challenges in Dynamic Trajectories

Challenges in learning:

- **C1:** How to learn inter-dependent user and item embeddings? **Solution: Update component**
- **C2:** How to generate embedding for every point in time? **Solution: Project component**

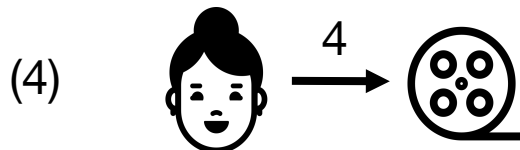
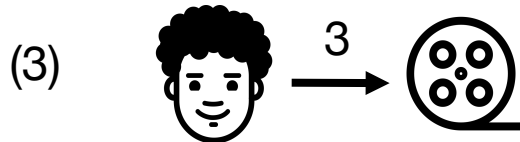
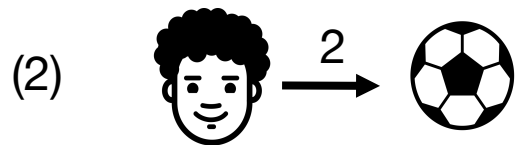
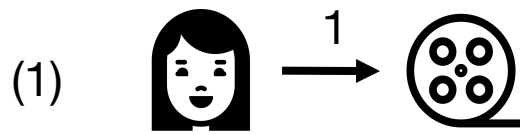
Challenges in scalability:

- **C3:** How to scalably train models on temporal networks?



Standard Training Processes: N/A

Training must maintain temporal order



⋮
⋮
⋮

Sequential processing:
not scalable

User 1



1



User 2



2



User 3



4



Batch 1



5



3



6



Temporal inconsistency

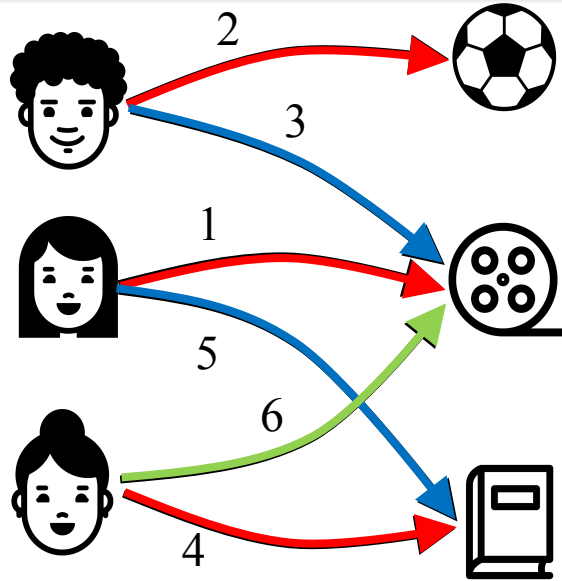
Split by user (or item):
not allowed

T-batch: Batching for Scalability

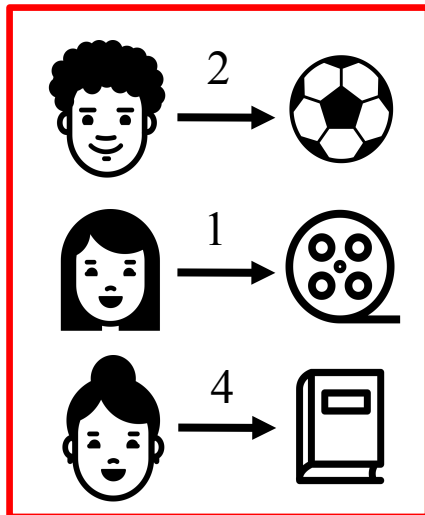
T-batch: Temporal data batching algorithm

- **Main idea: create each batch as an independent edge set**
- **Create a sequence of batches**
 - Interactions in each batch are processed in parallel
 - Process the batches in sequence to maintain temporal ordering

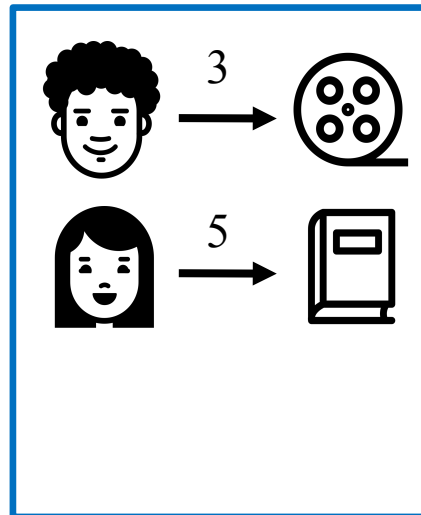
T-batch: Batching for Scalability



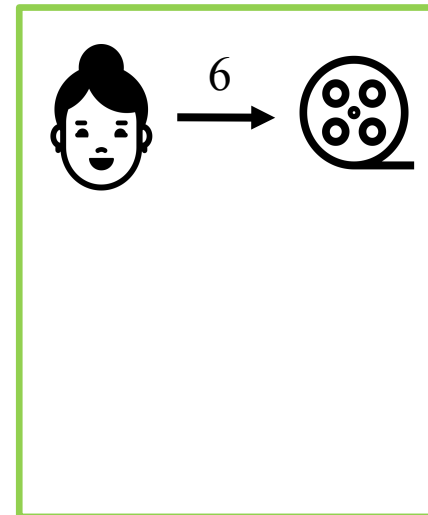
Iteratively
select the
maximal
independent
edge set.



Batch 1



Batch 2



Batch 3

Challenges in Dynamic Trajectories

Challenges in learning:

- **C1:** How to learn inter-dependent user and item embeddings? **Solution: Update component**
- **C2:** How to generate embedding for every point in time? **Solution: Project component**

Challenges in scalability:

- **C3:** How to scalably train models on temporal networks? **Solution: T-batch Algorithm**

Experiments: Prediction Tasks

- **Temporal Link Prediction:**
 - Which item $i \in I$ will user u interact with at time t ?
- **Temporal Node Classification:**
 - Does a user u become anomalous after an interaction?
- **Settings:**
 - **Temporal Splits:** 80%, 10%, 10%
 - **Metrics:** Mean reciprocal rank, Recall@10, AUROC

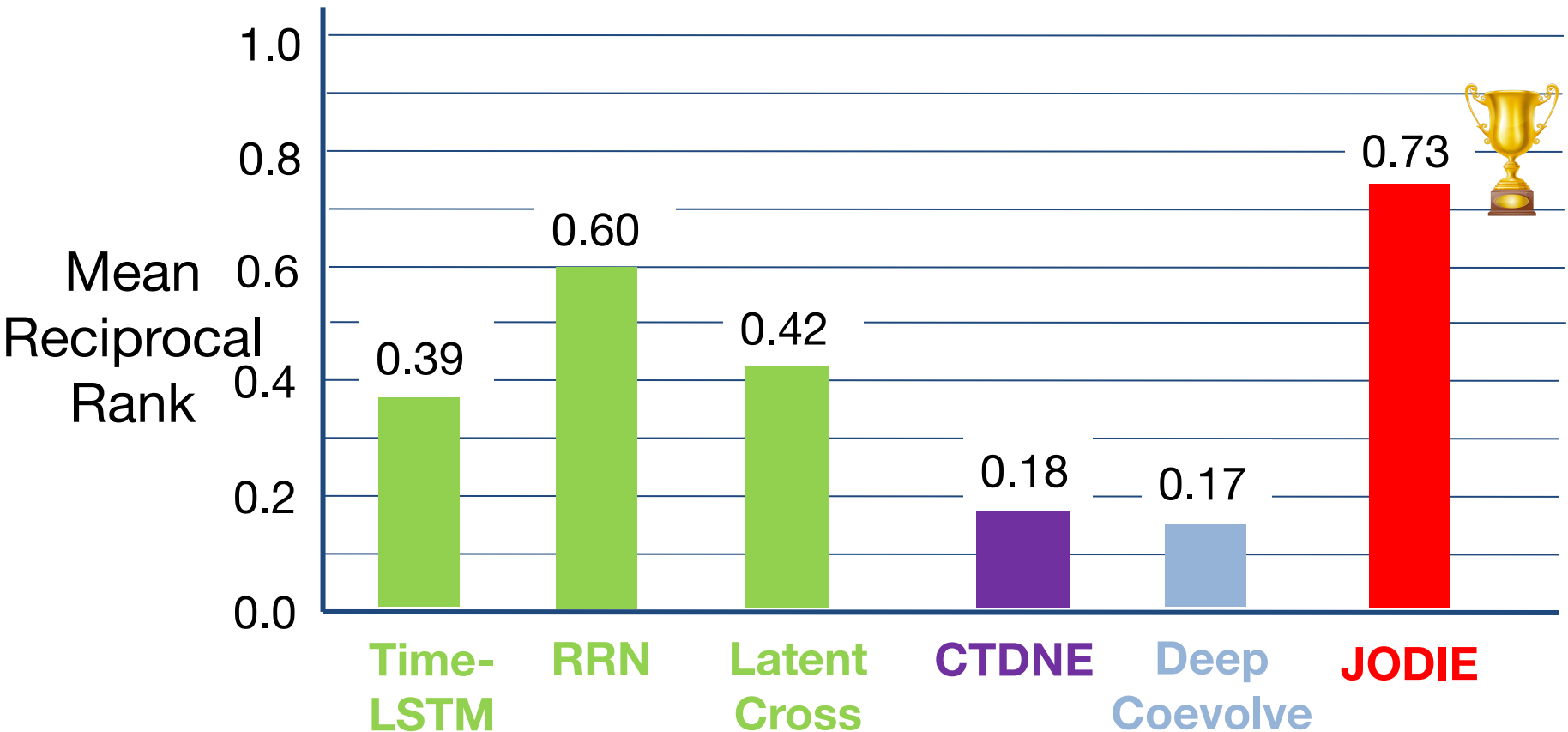
Code and Data: <https://snap.stanford.edu/jodie>

Datasets

Dataset	Users	Items	Interactions	Temporal Anomalies	
Reddit	10,000	984	672,447	366	NEW!
Wikipedia	8,227	1,000	157,474	217	NEW!
LastFM	980	1,000	1,293,103	-	
MOOC	7,047	97	411,749	4,066	

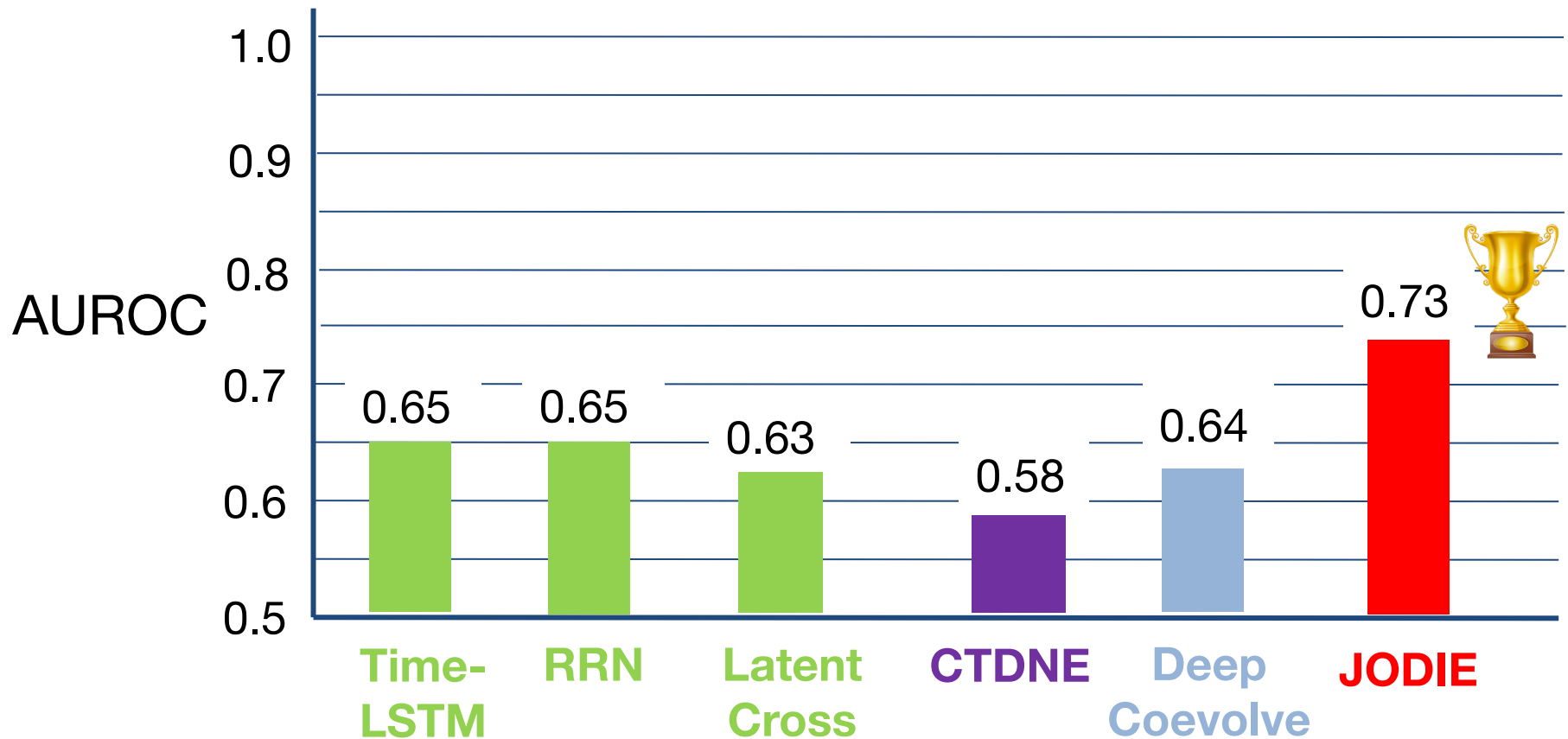
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Experiment 1: Link Prediction



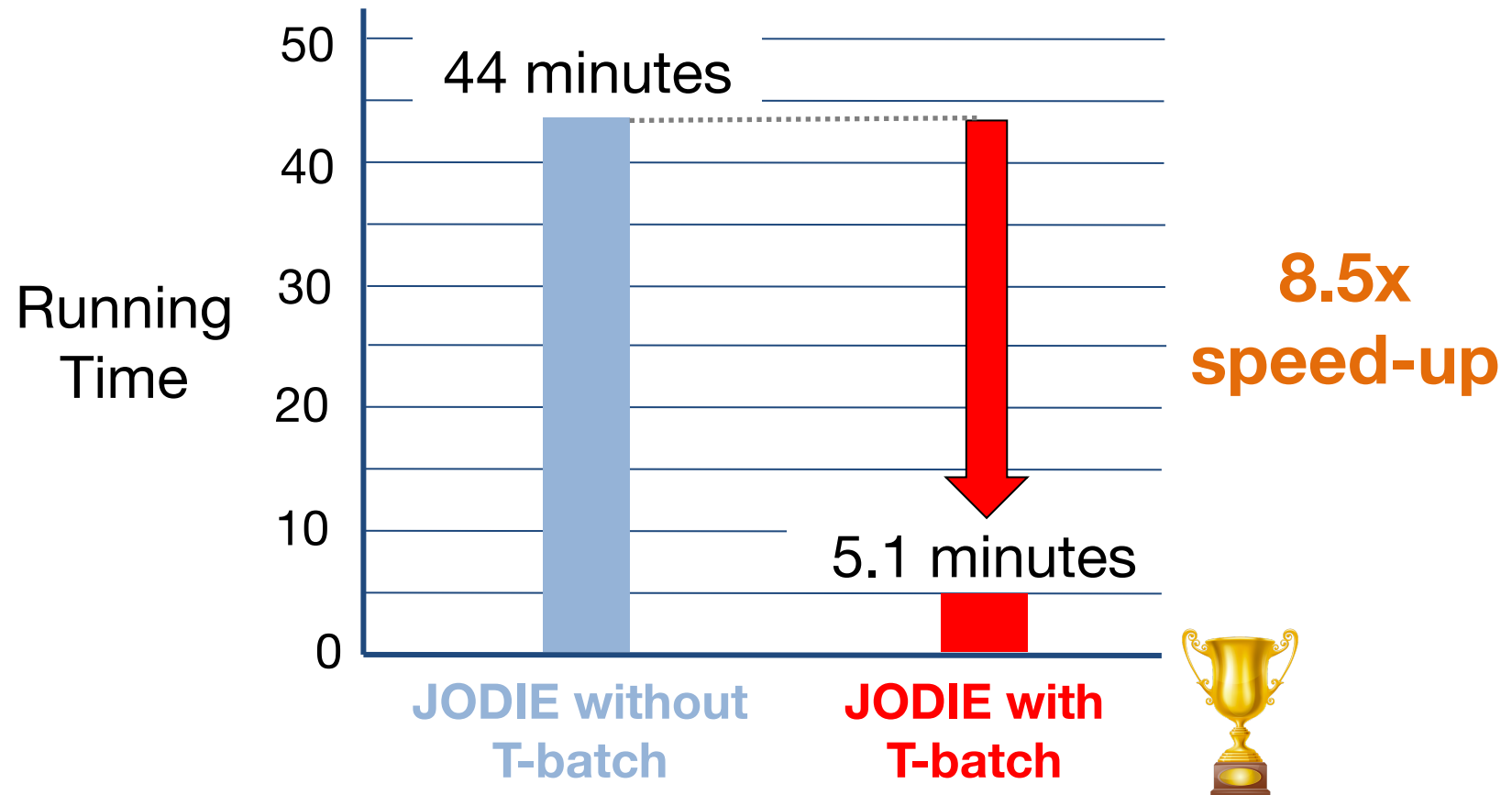
JODIE outperforms baselines by $> 20\%$

Experiment 2: Node Classification



JODIE outperforms all baselines by >12%

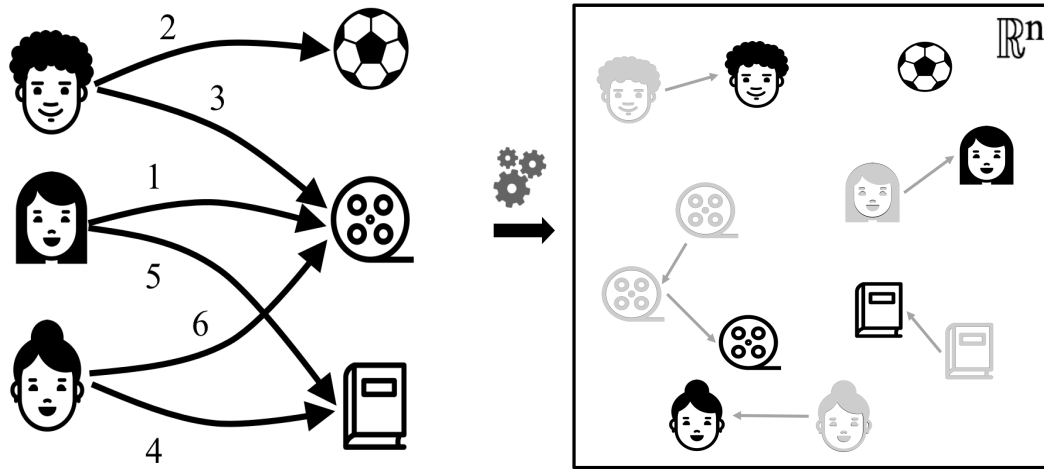
Experiment 3: T-batch Speed-up



T-batch leads to 8.5x speed-up in training

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JODIE generates and projects embedding trajectories

- **JODIE: a mutually-recursive RNN** framework
- **T-batch:** 8.5x training speed-up
- **Efficient** in temporal link prediction and node classification
- **Extendible** to > 2 entity types

Code and Data: <https://snap.stanford.edu/jodie>

Open Positions @ Georgia Tech

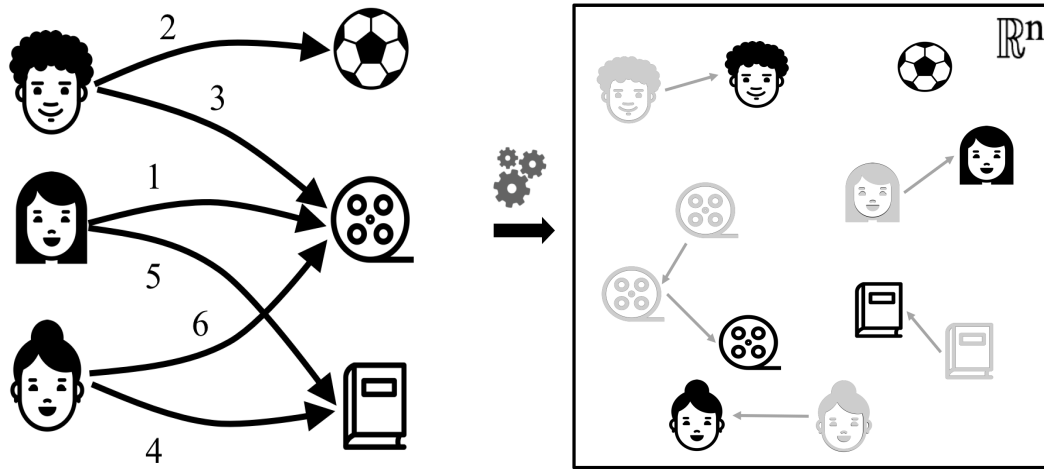
- **Hiring multiple Ph.D. students**
- **Research areas:**
 - Machine Learning for Networks
 - Safety, Integrity, and Anti-Abuse
 - Computational Social Science
- **Collaborations**



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