

High Efficiency Power Amplifier Based on Envelope Elimination and Restoration Technique

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Abstract -- Due to complex envelope and phase modulation employed in modern transmitters it is necessary to use power amplifiers that have high linearity. Linear power amplifiers (classes A, B and AB) are commonly used, but they suffer from low efficiency especially if the transmitted signal has high peak to average power ratio (PAPR). Kahn's technique based on envelope elimination and restoration (EER) is based on idea that high efficiency power supply (envelope amplifier) could be used to modulate the envelope of high efficient non linear power amplifiers (classes D or E). This paper presents solutions for power amplifier that performs envelope modulation and class E amplifier that is used as a non linear amplifier. The envelope amplifier is implemented as a multilevel converter in series with linear regulator and can provide up to 100 W of instantaneous power and reproduce 2 MHz sine wave. The implemented Class E amplifier can operate at 120 MHz with efficiency near to 85%. The envelope amplifier and class E amplifier have been integrated and efficiency and linearity of the implemented transmitter has been measured and presented.

Index Terms—Kahn's technique, envelope elimination and restoration, envelope amplifier, power amplifier, multilevel converter

I. INTRODUCTION

Due to the ultra fast development of communication technologies and their functionalities (data, voice and video transmitting), the bandwidth has become of crucial importance. In order to increase the spectral efficiency, modern radio techniques use methods such as CDMA (Code Division Multiple Access), WCDMA (Wide Code Division Multiple Access), or EDGE (Enhanced Data rate for GSM Evolution) that use time variable envelopes. Due to the instantaneous envelope and phase modulation these systems require linear PA (class A, B or AB). Unfortunately, although they offer high linearity, these PA suffer from low efficiency. For example, a class B amplifier has efficiency of $\pi/4$, but only in the case when it amplifies a sine wave of the maximal amplitude, without envelope modulation.

The power conversion efficiency of linear Radio Frequency PA (RF PA) is limited to less than 25% for signals with high envelope variations [1]. For example, WCDMA signals have a very high peak-to-average ratio, between 9 dB and 11 dB, and it is necessary that the RF PA amplifies both

high and low amplitude signals. In order to obtain a sufficiently high level of linearity, a technique known as back-off is used [1].

When the back-off is applied, the linear RF PA is supplied by voltage much higher than the signal's maximal amplitude. However, this leads to deteriorated efficiency of the transmitter. Poor system efficiency means significant power that is wasted and higher cooling requirements, bigger volume of devices and, in the case that they were battery operated much shorter autonomy. Having in mind that for the battery operated devices their autonomy is crucial, the problem of low efficient RF PA gains on its importance.

There are a lot of techniques that are used in order to enhance the efficiency and linearity of RF PA (some of them will be explained in the next section), but two of them have often been exploited lately. One of them is called Kahn's Technique or Envelope Elimination and Restoration (EER) Technique [2]. The power supply is varied dynamically in the same way, but this time the load is not a linear PA, but a non-linear PA. In this way, the RF PA works as a time domain multiplier, where the envelope modulation is injected to the non-linear PA. Figure 1 presents a block diagram of this technique.

The high efficiency of EER technique lies in the employed non-linear PAs (class E, D, F) that have high efficiency (theoretically 100%) and its high efficiency power supply. Non-linear PAs are based on the idea of employing a transistor as a switching device, not as a current source, and in the way that the power losses on the transistor are very low, comparing them with the case when it works as a current source in linear classes.

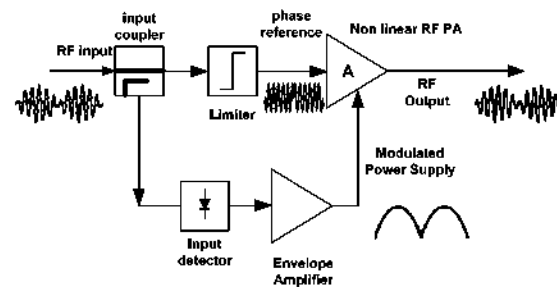


Fig.1. Block diagram of Kahn's technique

Thanks to the EER technique, the efficiency of the transmitter is almost constant for a wide load range and it does not depend heavily on the level of the transmitted signal, as in the case of linear amplifiers [3]. Average efficiency three to five times those of linear amplifiers has been demonstrated from HF to L band [4, 5].

In this paper solutions for the power supply that acts as the envelope amplifier and class E amplifier that is used as a non-linear amplifier are presented. The envelope amplifier is based on a multilevel converter in series with a linear regulator and its bandwidth is in the range of 2 MHz, while the class E amplifier operates at 120 MHz. The instantaneous output power provided by the class E power amplifier is in range of 90 W. The proposed solutions for the envelope amplifier and class E amplifier are integrated into an EER transmitter and set of tests have been conducted in order to characterize the transmitter

II. ENVELOPE AMPLIFIER

Due to high bandwidth requirements, conventional solutions for tracking power supplies [6-8] are not energy efficient. In [9] a buck converter is integrated on a chip. It operates at 130 MHz and the bandwidth is 15 MHz, but the peak power was just 2.2 W, while the average power around 1 W. For the range of power that should be used in the desired EER PA, this solution is unacceptable as well.

The proposed envelope amplifier consists of a multilevel converter and a linear regulator in series, [10]. Its block schematic is shown in Figure 2. The multilevel converter supplies the linear regulator with discrete voltage levels that are as close as possible to the output voltage of the envelope amplifier. In this way, the power losses on the linear regulator are minimal, because they are directly proportional to the difference between its input and output voltage. However, in order to guarantee correct work of the linear regulator, the output voltage of the multilevel converter has to be higher than the output voltage of the linear regulator. Time diagrams of the multilevel and linear regulator voltage are shown in Figure 3.

By using the architecture proposed in this thesis, it is possible to take advantage of all the good characteristics of the linear regulator (high bandwidth, high linearity, etc.) and to obtain significantly higher efficiency comparing it with the solution when the linear regulator is supplied by a constant voltage. Additionally, the need for the complicated output filter design is avoided because most of the switching noise that comes from the switching converter will be filtered by the linear regulator and the feedback loop that is used can be very simple.

Thanks to the linear regulator that is employed as a post regulator, the output voltage will not have any voltage ripple, which is always present if only a switching dc-dc converter is used. In some applications for the envelope amplifier, the

specifications for the voltage ripple, and not the desired bandwidth, lead to the necessity of very high switching frequency [7].

The main disadvantage of this architecture is that it is composed of two stages, and in order to obtain high efficiency of the envelope amplifier, it is necessary that the efficiency of both stages should be as high as possible. The efficiency of the linear amplifier will depend on the regulating precision of the dc-dc switching converter, and in order to obtain good precision for the linear regulator's input voltage the switching converter should operate at the switching frequency that is at least 5 times higher than the desired bandwidth of the envelope amplifier's output voltage [11]. If the requested bandwidth is 2 MHz, the switching frequency should be 10 MHz. At such a high switching frequency the efficiency of conventional converters (buck, boost, buck-boost etc) drops heavily due to high switching losses.

A. Optimization of number of levels

In order to optimize the efficiency of the linear regulator it is necessary to make a proper decision about the voltage levels that should be generated by the multilevel converter. The input voltage of the linear regulator is the output voltage of the multilevel converter and it is a function of the transmitted signal's envelope. It can be represented as:

$$V_{in \text{ linear regulator}} = V_{in \text{ linear regulator}}(V_{envelope}) \quad (1)$$

where $V_{envelope}$ is the value of the signal's envelope.

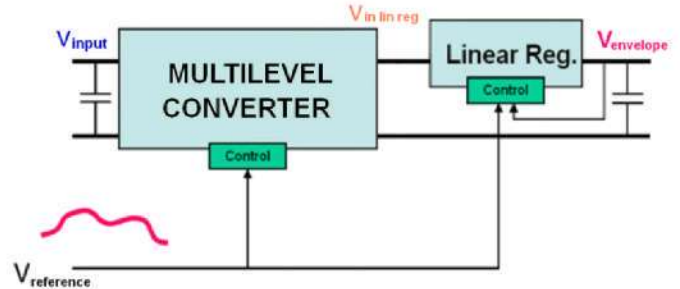


Fig.2. Simplified schematic of the proposed envelope amplifier

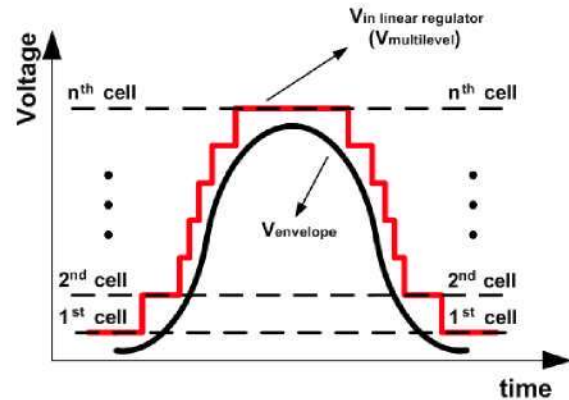


Fig.3. Time diagrams of the proposed envelope amplifier

III. CLASS E AMPLIFIER

The class E amplifier that is used to amplify the constant envelope, phase modulated, component of the signal, operates at the VHF band and exhibits wide fractional bandwidth (from 95 MHz to 120 MHz). The drain to source voltage of the implemented class E amplifier can be seen in Figure 7 at 120 MHz showing that the amplifier is operating near nominal Class-E conditions.

The design of the amplifier and its load network has been optimized to reduce power losses to a minimum. The results of efficiency measurements are shown in Figure 8. When the class E amplifier is supplied with constant voltage of 24 V, its output power exhibits a peak value of 90 W operating between 100MHz and 110MHz. The drain efficiency of the amplifier in that frequency range is around 85% (A Bird 5000EX wattmeter has been used to measure output power, the accuracy of this instrument is 5%).

The RF power MOSFET used with this amplifier is a MRF6V4300N from Freescale Semiconductors. Input and output ports have been modeled for switching operation using the model proposed in [13].

This amplifier has been designed based upon the load impedance synthesis design technique as shown in [14] and simulated and optimized using Advanced Design System (ADS) software from Agilent.

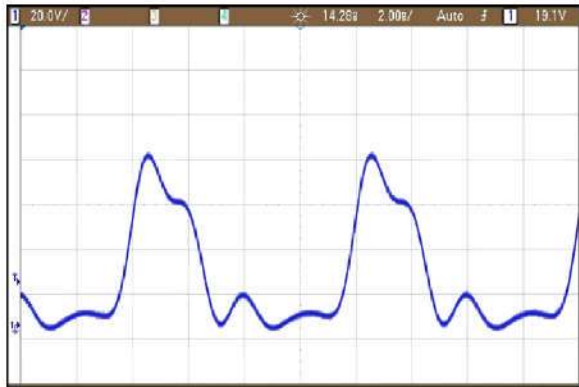


Fig. 7. Drain voltage of the implemented class E amplifier when it operates at 120MHz

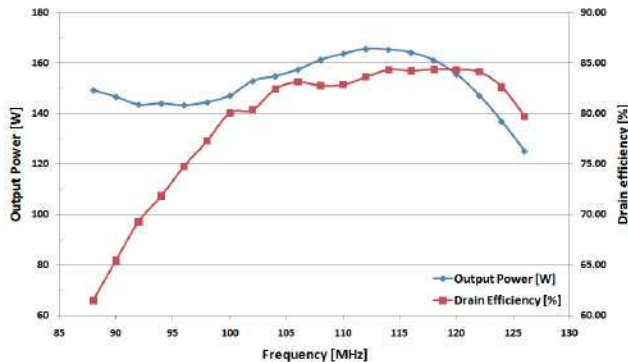


Fig. 8. Measured output power and the efficiency of the implemented class E for different switching frequencies (instrument accuracy: 5%).

IV. INTEGRATION OF THE ENVELOPE AMPLIFIER WITH THE CLASS E AMPLIFIER

The integration of the implemented envelope amplifier and the class E amplifier has been done in order to demonstrate the advantage of one EER system over a linear power amplifiers and that overall efficiency is increased for the same level of linearity. The efficiency of an EER transmitter depends on the efficiency of the envelope amplifier and the efficiency of the nonlinear amplifier. Even more, the overall efficiency can be roughly estimated as a product of efficiencies of the envelope amplifier and nonlinear amplifier.

Besides the envelope amplifier and class E amplifier, the implemented transmitter has a module that is used to receive the RF reference signal and to generate the phase and envelope references. It consists of a FPGA Virtex 4 development board fitted with D/A and A/D converters. The transmitter receives the RF reference signal through A/D converters, and the envelope and phase references are extracted inside a FPGA. The digitalized references are converted to analog signals using high speed D/A converters, and connected to the envelope and class E amplifiers. Additionally, two delay filters and the envelope's amplifier triggering logic are implemented in the employed FPGA. The first delay filter is used in order to synchronize the envelope reference signal connected to the linear regulator with the output voltage of the multilevel converter in order to avoid the distortion of the reproduced envelope. The differential delay between the produced envelope and phase modulation should not be higher than one tenth of the bandwidth of the RF signal [15]. The second delay filter is used to adjust the differential delay in order to obtain high overall linearity of the system. The triggering logic needed by the multilevel converter is a simple set of comparators that has to regulate the state of the voltage cells.

Figure 9 shows the implemented EER transmitter.

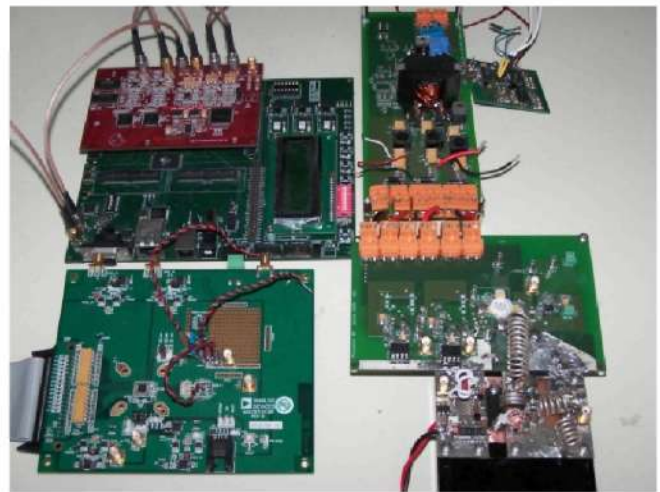


Fig.9. Photograph of the implemented EER Transmitter (on the right) with FPGA board, A/D and D/A converters (on the left)

In [16] the results of the efficiency measurements in the case of a simple AM modulation have been presented. It has been demonstrated that the efficiency of the implemented EER PA is significantly higher than the theoretical efficiency of the class B amplifier when the signals with high PAPR (Peak to Average Power Ratio) are transmitted. The power losses were up to 40% lower in the implemented EER PA than in the case of the ideal class B PA:

In this paper the experiments regarding the linearity of the system and its efficiency with more complicated modulations are presented. The class E amplifier is seen as resistive (5Ω) impedance by the implemented envelope amplifier.

A. Linearity Test

In order to measure the overall linearity of the transmitter the two tone test has been conducted. The two tone test can, actually, be presented as Double Side Band – Suppressed Carrier (DSB-SC) Modulation. A DSB-SC wave is given by:

$$s(t) = m(t)A_c \cos(\omega_c t) \quad (3)$$

where $m(t)$ is the transmitted signal, and ω_c angular speed of the carrier.

Analyzing equation (3) it can be concluded that the spectrum of the modulated signal is actually the same as the signal's base band spectrum, just translated to high frequencies. If the transmitted signal is a simple sine wave of frequency f_s , then the envelope of the signal can be presented as:

$$envelope_{ref} = |\sin(2\pi f_s t)| \quad (4)$$

and the output signal is then:

$$s(t) = |\sin(2\pi f_s t)| \cos(2\pi f_c t + \varphi_s(2\pi f_s t)) \quad (5)$$

Therefore, from equations (3)-(5) it yields that the reference signal for the class E amplifier is a sine wave with the same frequency as the carrier and that this sine wave has to change its phase for 180 degrees each time when the envelope reference is equal to zero.

These two reference signals are created in MATLAB and then stored in a look-up table in an FPGA. In Figure 10 the envelope reference, the output of the multilevel converter, the output of the envelope amplifier and the output of the implemented EER transmitter are shown during the linearity measurements. Figure 11 shows the spectrum of the output of the transmitter.

In Figure 10 a huge amount of the RF noise in the envelope reference can be seen but, due to the low pass property of the implemented envelope amplifier, that noise does not have influence on the output signal of the envelope amplifier. The spectrum of the transmitter's output shows two harmonics around 125 MHz, like it is expected, but there are more components that are products of AM-PM distortion of the class E amplifier. It can be seen that the attenuation of the highest additional harmonic is 18 dB, which means that the quality of the output signal will not be high.

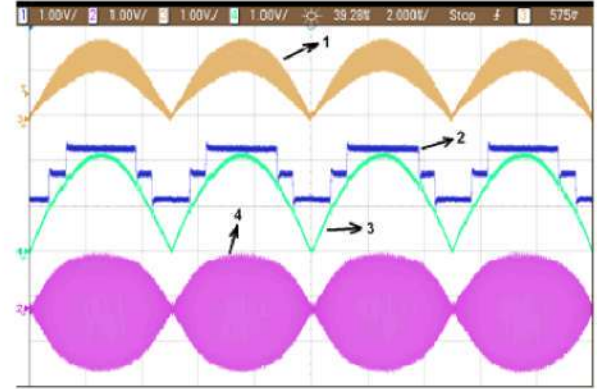


Fig10. The reference signal (label 1, channel 3), the output of the multilevel converter (label 2, channel 4), the output of the envelope amplifier (label 3, channel 1) and the output of the EER transmitter (label 4, channel 2) when the envelope reference signal is rectified 100 kHz sine wave

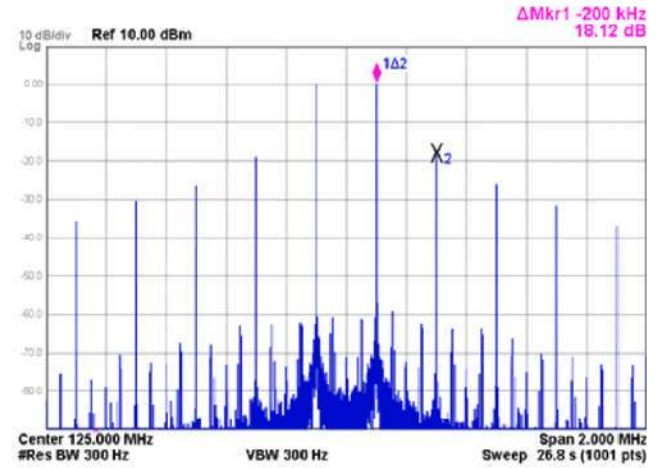


Fig.11. Spectrum of the output of the EER transmitter when the transmitted signal is a sine wave of 100kHz, carrier is a 125 MHz sine wave and the applied modulation is DSB-SC

The AM-PM conversion is due to the presence of the non-linear capacitor between the drain and the source of the class E MOSFET. Depending on the applied supply voltage, this capacitor changes its value and it influences the phase delay between the signal sent to the MOSFET's gate and the signal reproduced by the class E amplifier.

In order to improve this attenuation, a measurement of the AM-PM conversion has been conducted and it is represented in the terms of the aforementioned phase delay. The result of the measurement can be seen in Figure 12.

The predistorter used to enhance the linearity is implemented in the way that it inserts the inverted phase delay in order to cancel the influence of the class E amplifier. The simplified block schematic is presented in Figure 13.

Having in mind that the relationship between phase delay and the class E amplifier supply voltage (this voltage is proportional to the envelope of the transmitted signal) is known, the predistorter is made as a look-up table. Each time that the envelope reference is sent, the corresponding phase delay is inserted in the phase modulation.

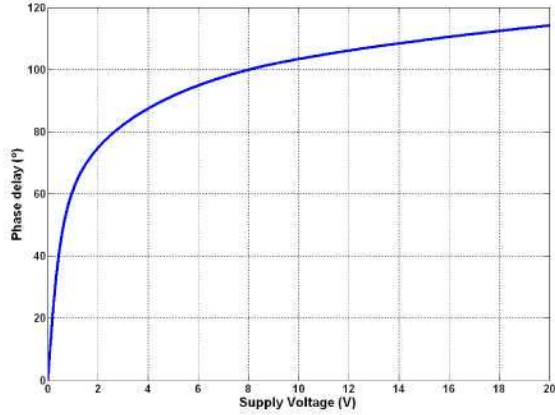


Fig. 12. Dependency of the phase delay between the output of the implemented class E PA and gate signal depending on the supply voltage of the PA

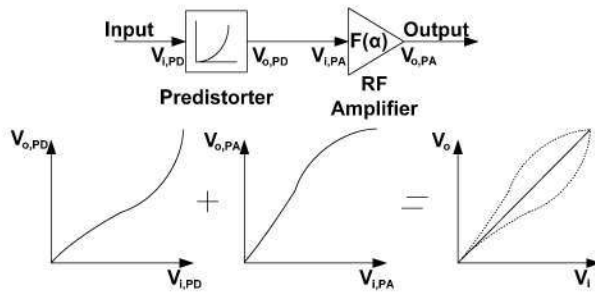


Fig. 13. Block diagram of predistortion concept and amplitude correction by predistortion

In order to facilitate the testing, the two-tone signal is generated in MATLAB, and the envelope reference and predistorted phase reference are sent to the EER amplifier via the signal generator (Agilent 81150A). The measured linearity after the predistortion in the case that the f_s is 500kHz, and f_c is 100 MHz, is presented in Figure 14

Figure 15 shows the attenuation of the 3rd order intermodulation products for different carrier and envelope frequencies.

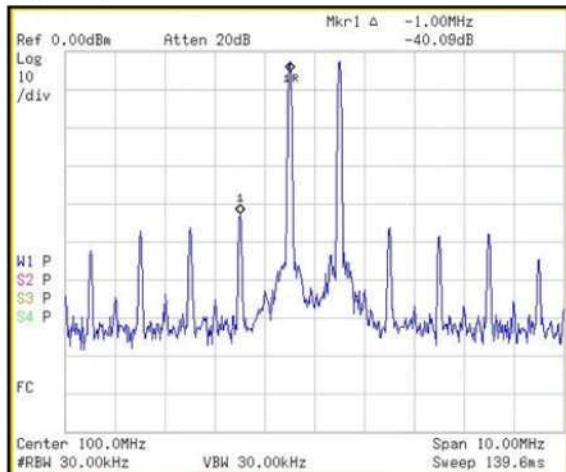


Fig. 14. Spectrum of the PA's output voltage when two tones are sent as the PA's reference signal ($f_c=100$ MHz, $f_s=500$ kHz)

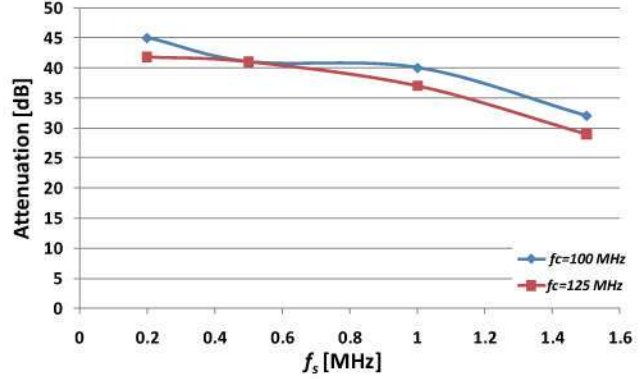


Fig. 15. Measured attenuation of the third order intermodulation products, for the different frequencies of the envelope (f_s) and carrier signal (f_c)

B. Efficiency measurements

Once the high linearity of the PA has been obtained, efficiency measurements in the case of a 64QAM have been performed.

The 64QAM-modulated signal can be presented as:

$$x(t) = Q(t) \sin(\omega t) + I(t) \cos(\omega t) \quad (6)$$

$$Q(t), I(t) \in [-7, -5, -3, \dots, 3, 5, 7] \quad (7)$$

Graphically, the 64QAM modulation can be presented with its constellation as in Figure 16.

In order to make the test as real as possible, the I and Q signals are generated as random signals with Gaussian distribution. In that way, the envelope of the test signal has Rayleigh's distribution with a high PAPR. Figure 17 shows the constellation and the transitions of the generated signal.

As it can be seen, due to the Gaussian distribution of the I and Q signals, the probability that I and Q have high values at the same time (and in that way high envelope values) is low, and it corresponds to the high PAPR signal.

The impedance seen by the envelope amplifier is around 5Ω and the maximal value of the envelope is 22V. This leads to the conclusion that the envelope amplifier has to provide up to 100W of instantaneous power.

The generated signal has a ratio between the maximal value and the average value of 8.6 dB. The density of the probability for the envelope is shown in Figure 18. High PAPR can be observed once again. The high peak that is presented for the envelope value of 2 V is due to the short interval of time where the envelope has this value in order to facilitate the synchronization between envelope and phase modulation. However, that part of the envelope is just 3% of the overall signal and it does not have any significant influence on the overall efficiency.

The same I, Q pattern is used with different data rates in order to see how the bandwidth of the transmitted signals influences the efficiency of the implemented EER transmitter. The bandwidth of the transmitted signal is, approximately, twice the bit rate.

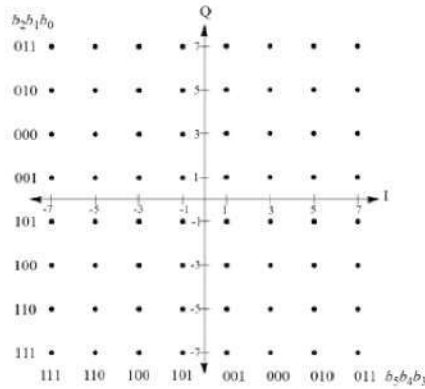


Fig. 16. Constellation of the I and Q signals for 64QAM modulation

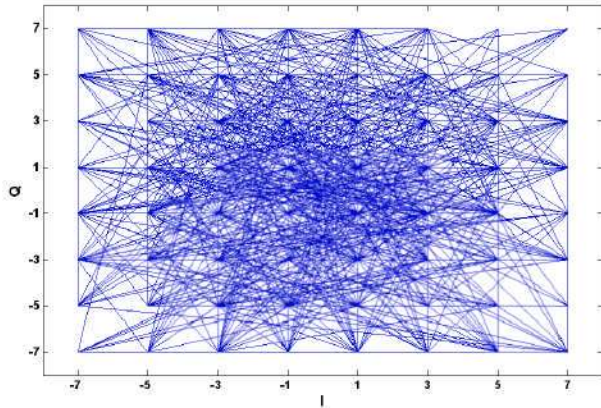


Fig. 17. Generated constellation and transitions of the I and Q signal in the case of 64QAM modulation

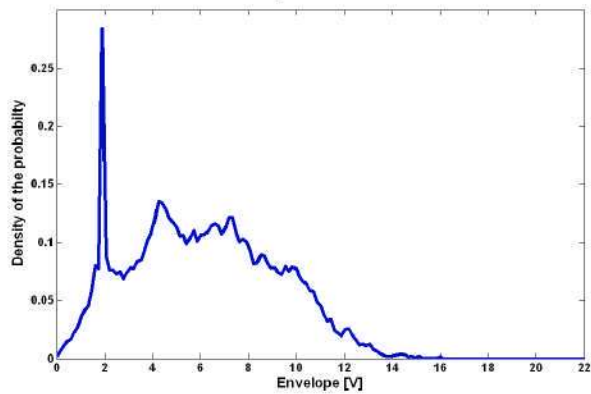


Fig. 18. Density of the probability of the envelope signal for the generated test pattern based on 64QAM modulation

The measured efficiency is presented in Figure 19 and it is compared with the theoretical efficiency of an ideal class B amplifier supplied by 24 V. The efficiency measurements are conducted with carrier signals of 100 MHz and 125 MHz. The reason for this is to see how the efficiency of the system depends on the frequency of the carrier signal and, in that way, on the input impedance of the class E amplifier. The average output power of the transmitted signal is 13 W.

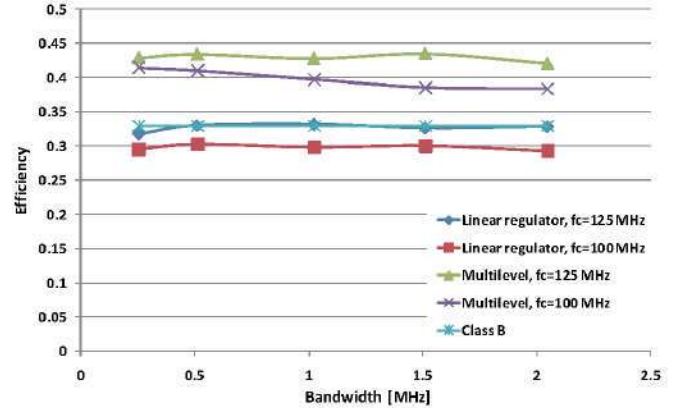


Fig. 19. Measured efficiency of the implemented EER PA in the case when the class E amplifier is supplied by classical linear regulator supplied by constant voltage and supplied by the proposed hybrid solution. The measured efficiency is compared with the theoretical efficiency of an ideal class B PA supplied by 24 V

When the carrier signal is 125 MHz, it can be seen that if the implemented EER PA uses a linear regulator supplied by a constant voltage as the envelope amplifier the efficiency is practically the same as the theoretical efficiency of the ideal class B amplifier. In the case that the multilevel converter is used the efficiency is improved from approximately 32% to 43% (the power losses are decreased for 25%). The main reason for this is the high PAPR of the transmitted signal.

For the carrier signal of 100 MHz similar conclusions can be made. The implemented EER PA exhibits higher efficiency if it employs the multilevel converter in series with linear regulator than the efficiency when only the linear regulator is used. The efficiency is improved from 30% to 40% (improvement of 25% in the terms of power losses) and it is higher than the estimated efficiency of ideal class B amplifier for the same signal pattern. However, when the frequency of the carrier is 100 MHz, the input impedance of the class E amplifier is lower than in the case of 125 MHz carrier wave. Due to this, the envelope amplifier has to process higher currents and it has more power losses. Therefore, the overall efficiency is slightly lower for the 100 MHz carrier than in the case when the frequency of the carrier is 125 MHz.

The time waveforms of the multilevel converter, envelope amplifier and output of the implemented EER PA in the case that the transmitted signal has the bandwidth of 2 MHz can be observed in Figure 20. The constellation and the spectrum of the demodulated signal can be seen in Figure 21. The demodulation is performed by Agilent MxA Signal Analyzer N9020A.

By analyzing the constellation of the demodulated signal, it can be concluded that the EER PA has correctly reproduced the signal because there can be clearly distinguished all 64 possible points. The error vector magnitude (the measure of how far the points are from the ideal locations) is around 2.7%.

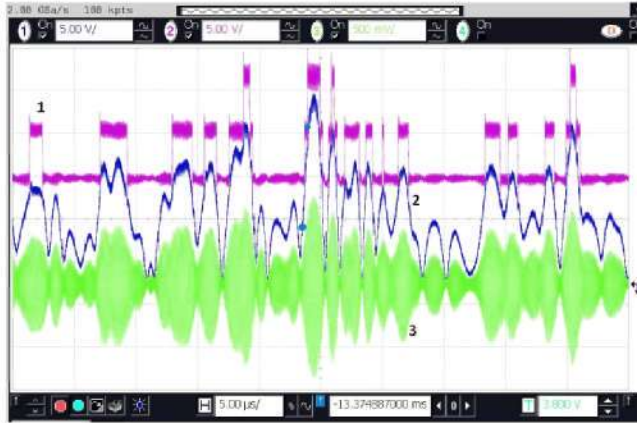


Fig.20. Oscilloscope capture of the multilevel converter's output voltage (label 1), envelope amplifier's output voltage (label 2) and complete RF signal (label 3) in the case when a 64QAM signal with the bit rate of 1024kbit/s is amplified

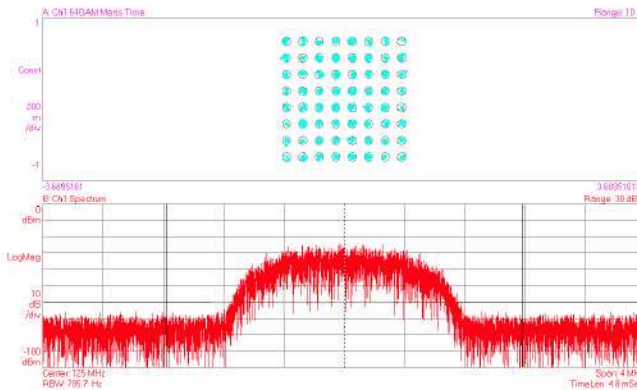


Fig.21. The constellation and the spectrum of the demodulated 64QAM signal amplified by the implemented EER PA

V. CONCLUSIONS

In this paper a radio transmitter based on the Kahn's technique (EER) is presented. The implemented transmitter is composed of envelope amplifier (responsible for envelope injection) and a class-E amplifier (performs phase modulation). The envelope amplifier has to fulfill strict requirements regarding its bandwidth and linearity, and, therefore, it is implemented as a multilevel converter in series with a linear regulator. In this way, high frequency signals can be reproduced applying relatively low switching frequency.

The implemented EER PA can provide up to 100W of instantaneous power and reproduce a 2 MHz sine wave of maximal excursion (from 0 V to 22 V).

The linearity of the implemented EER PA was measured using two tone signals. First linearity measurements indicated that due to the non-linear effects in the class E amplifier, it would be necessary to use predistortion in order to increase the system's linearity. By employing predistortion, the attenuation of the intermodulation products of the third order is around 40 dB in wide range of bandwidths (up to 1 MHz).

Once the system's high linearity was obtained, the complete EER PA was tested with a 64QAM modulation where the envelope of the signal has high PAPR (8.6 dB). By measuring the power consumption it was demonstrated that the power losses of the implemented EER PA are, approximately, 25% lower than the power losses of an ideal linear class B PA. The maximum bandwidth of the transmitted signal was around 2 MHz (bit rate was 1024 kbit/s).

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