Collision Detection

衝突検出

Applications

Computer Graphics



(Wikipedia)

Robotics



(Wikipedia)

CAD



(Credit: freeformer @ Wikipedia)

Popular Rigid Body Simulation Engine

Bullet



(Credit: SteveBaker at Wikipedia)

Open Dynamic Engine



(Credit: Kborer at Wikipedia)

Real-time Collision Detection using GPU

Vivace: a Practical Gauss-Seidel Method for Stable Soft Body Dynamics

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Marco Fratarcangeli, Valentina Tibaldo, Fabio Pellacini ACM Transactions on Graphics (SIGGRAPH Asia), 2016 http://www.cse.chalmers.se/~marcof

Brute-force Collision Detection Never Works

• If there are N objects, there are N(N-1)/2 number of pair

 $\bigcirc \mathcal{O}(N^2)$ complexity is too slow!



Collision Detection in Two Stages



Idea of Finding Collision (like a Garimpeiro)





1D Collision Detection

• What is the condition that two line segments intersect?



What is "Convex" Shape

Interpolation of two points is always included



Separation Axis Theorem (SAT)

• If two convex shapes do not collide, there exists an axis where their projections will not overlap



Separation Axis Theorem for 2D Polygons

• One of the edges will be perpendicular to the separation axis



Collision Detection for 2D Polygons

• Check all the axes perpendicular to polygon's edges



Collision of AABB and k-DOP

- Project the Bounding Volume (BV) on axes
- Two BVs collide if all projections overlap



Data Structure of AABB & k-DOP

• Minimum and maximum along the axis

<pre>template <int naxis=""></int></pre>
class CKdops
double minmax[navie][2].
L.
, I
<pre>constexpr double axes[3][2] = {</pre>
{0,1},
{1,0},
<pre>{1,1} };</pre>
<pre>std::vector< CKdops<3> > aKdops;</pre>

Non-type template parameter (compile time argument)

Broad-phase Collision Detection

How We can Find Collisions of Circles?





 $dist(\vec{p}_1, \vec{p}_2) \le r_1 + r_2 \Rightarrow$ Collision

Approaches

- Brute force approach
- Sweep & Prune method
- Spatial Hashing (e.g., Regular grid)
- Spatial Partitioning (e.g., KD-tree)
- Bounding Volume Hierarchy (BVH)



Sweep & Prune (Sort & Sweep) Method

• Simple but effective culling method





 X_1 : remove X in the stack

How to Choose Sweeping Axis ?

- kDOPs -> Sweep in the kDOPs' axis
- Sphere, AABB, OOBB -> XYZ-axis or PCA



- Putting circles in a grid based on circles' center positions
- Grid length is maximum diameter of the circle
 - Look only 1-ring neighborhood



Possible collisions: {A,E}, {E,C}, {C,D}, {D,B}

No need to check for {E,D},{C,B}...etc

• Creating look-up table from grid index to circle index



circle index	Α	В	С	D	Ε
grid index	0	7	5	2	0

• Creating look-up table from grid index to circle index



• Creating look-up table from grid index to circle index





Space Partitioning with K-D Tree

1. Select axis (e.g., y-axis)
2. Split the space along median



Space Partitioning with K-D Tree

Select axis (e.g., y-axis)
 Split the space along median
 Repeat along other axis (e.g., x-axis)





Space Partitioning with K-D Tree

Select axis (e.g., y-axis)
 Split the space along median
 Repeat along other axis (e.g., x-axis)





Bounding Volume Hierarchy (BVH)

- Near triangles are in the same branch
- Each node has a BV that includes two child BVs





Example of BVH Data Structure in C++

index	0	1	2	3	4	5	6
left-child index	1	3	4	tri index	tri index	tri index	tri index
Right-child index	2	5	6	-1	-1	-1	-1
BV data							





Evaluation of BVH using Recursion

 Ask question to the root node -> if true the node asks the same question to two child nodes and so on



Top-down Approach to Build BVH

• Use PCA for separating triangles into two groups



Linear BVH: Fully Parallel Construction

- Construct BVH based on Morton code (i.e., Z-order curve)
- Two cells with close Morton codes tends to be near



2D square domain with 2^n edge division



 2^{2n} number of cells



Cell index is size of 2n in binary

Linear BVH: Fully Parallel Construction

• Convert XYZ coordinate into 1D (linear) integer coordinate





Linear BVH: Fully Parallel Construction

• Sort objects by their Morton codes



From Morton Code to BVH Tree

• Divide tree when digits of sorted Morton codes are different



Reference

• "Real-Time Collision Detection" by Christer Ericson



Japanese translation available



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Reference

• GPU Gems 3: Chapter 32. Broad-Phase Collision Detection with CUDA



Available for free at: https://developer.nvidia.cn/gpugems/gpugems3/part-v-physicssimulation/chapter-32-broad-phase-collision-detection-cuda



Reference on Linear-BVH

• Thinking Parallel, Part III: Tree Construction on the GPU

by Tero Karras



https://developer.nvidia.com/blog/thinking-parallel-part-iii-tree-construction-gpu/

