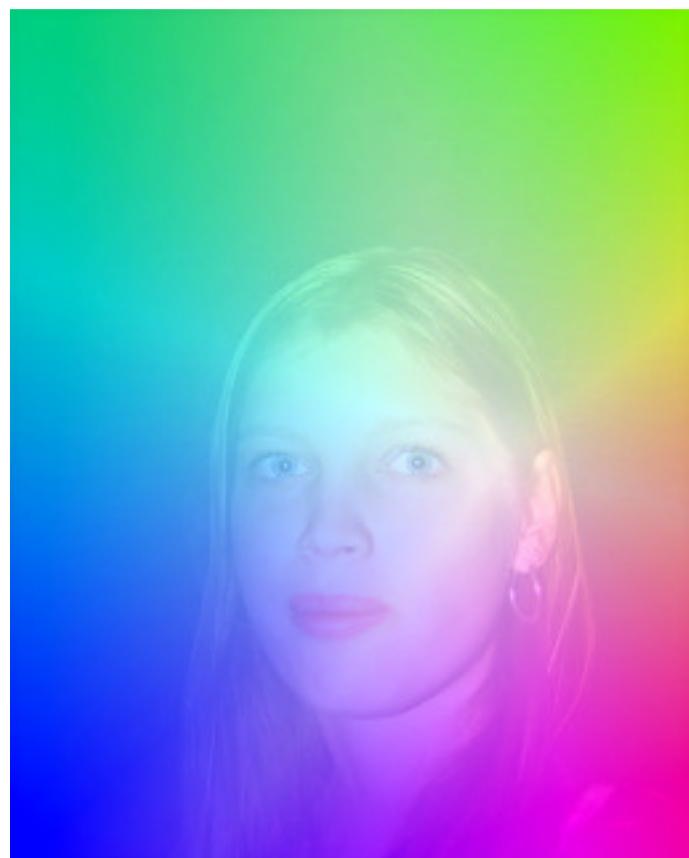


Gernot Hoffmann

CIE Color Space



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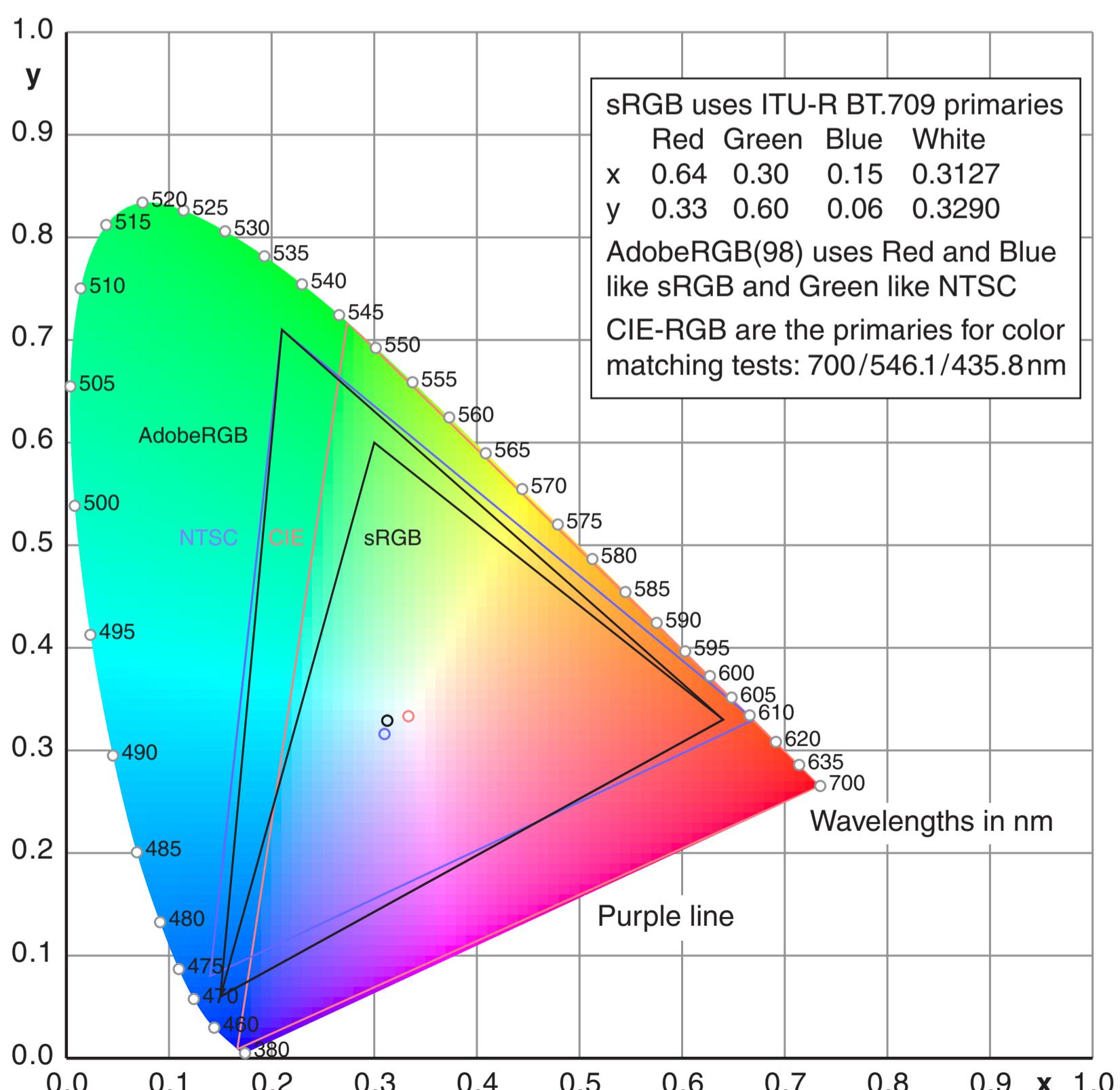
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1. CIE Chromaticity Diagram (1931)

The threedimensional color space CIE XYZ is the basis for all color management systems. This color space contains all perceivable colors - the human gamut. Many of them cannot be shown on monitors or printed.

The twodimensional CIE chromaticity diagram xyY (below) shows a special projection of the threedimensional CIE color space XYZ.

Some interpretations are possible in xyY, others require the threedimensional space XYZ or the related threedimensional space CIELab.



2. Color Perception by Eye and Brain

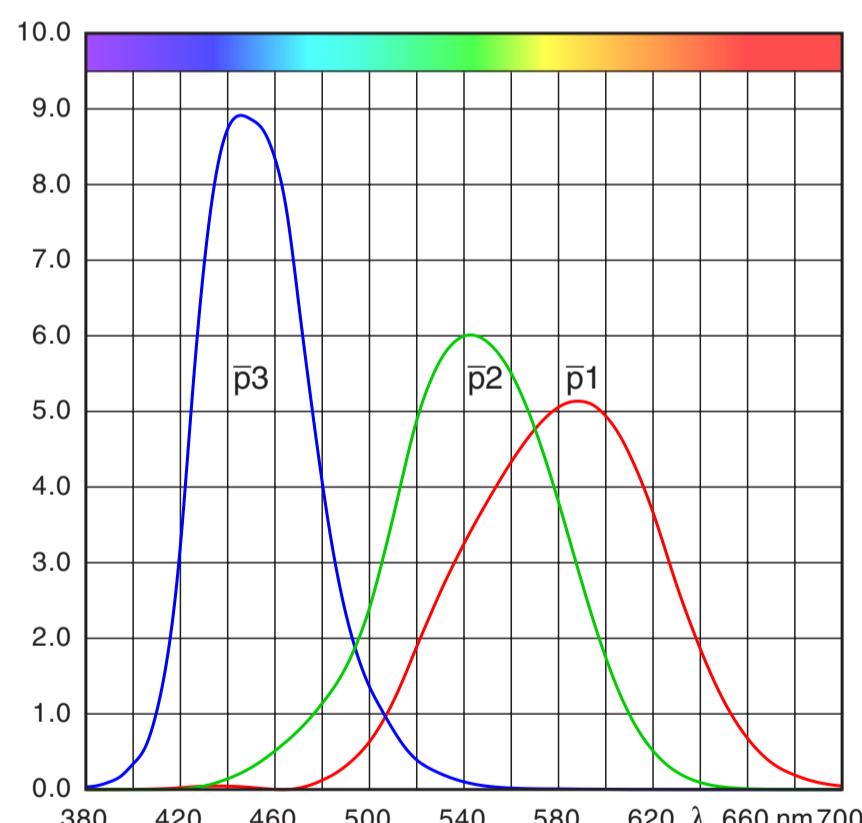
The retina contains two groups of sensors, the rods and the cones. In each eye are about 100 millions of rods responsible for the luminance. About 6 millions of cones measure color. The sensors are already 'wired' in the retina – only 1 million nerve fibres carry the information to the brain. The perception of colors by cones requires an absolute luminance of at least some cd/m^2 (candela per squaremeter). A monitor delivers about 100 cd/m^2 for white and 1 cd/m^2 for black.

Three types of cones (together with the rods) form a tristimulus measuring system. Spectral information is lost and only three color informations are left. We may call these colors blue, green and red but the red sensor is in fact an orange sensor.

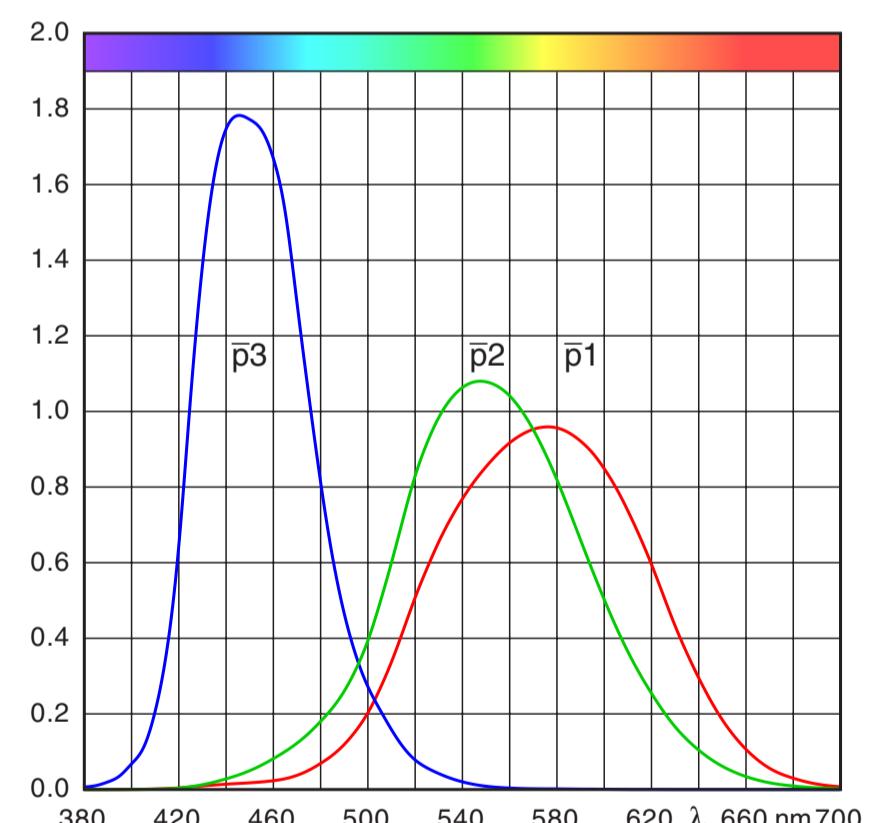
The optical system is not color corrected. It would be impossible to focus simultaneously for three different wavelengths. The overlapping sensitivities of the green and the red sensor may indicate that the focussing happens mainly in the overlapping range whereas blue is generally out of focus. This sounds strange, but the gap for image parts on the blind spot is corrected as well – another example for the surprising features of eye and brain.

These diagrams show two of several models for the cone sensitivities. These and similar functions cannot be measured directly – they are mathematical interpretations of color matching experiments.

The sensitivity between 700nm and 800nm is very low, therefore all the diagrams are drawn for the range 380nm to 700nm.



Cone sensitivities [3]



Cone sensitivities [1]

3. RGB Color-Matching

The color matching experiment was invented by Hermann Graßmann (1809 – 1877) about 1853.

Three lamps with spectral distributions $\mathbf{R}, \mathbf{G}, \mathbf{B}$ and weight factors $R, G, B = 0..100$ generate the color impression $\mathbf{C} = R\mathbf{R} + G\mathbf{G} + B\mathbf{B}$.

The three lamps must have linearly independent spectra, without any other special specification.

A fourth lamp generates the color impression \mathbf{D} .

Can we match the color impressions \mathbf{C} and \mathbf{D} by adjusting R, G, B ? In many cases we can:

$$\text{BlueGreen} = 7\mathbf{R} + 33\mathbf{G} + 39\mathbf{B}$$

In other cases we have to move one of the three lamps to the left side and match indirectly:

$$\text{Vibrant BlueGreen} + 38\mathbf{R} = 42\mathbf{G} + 91\mathbf{B}$$

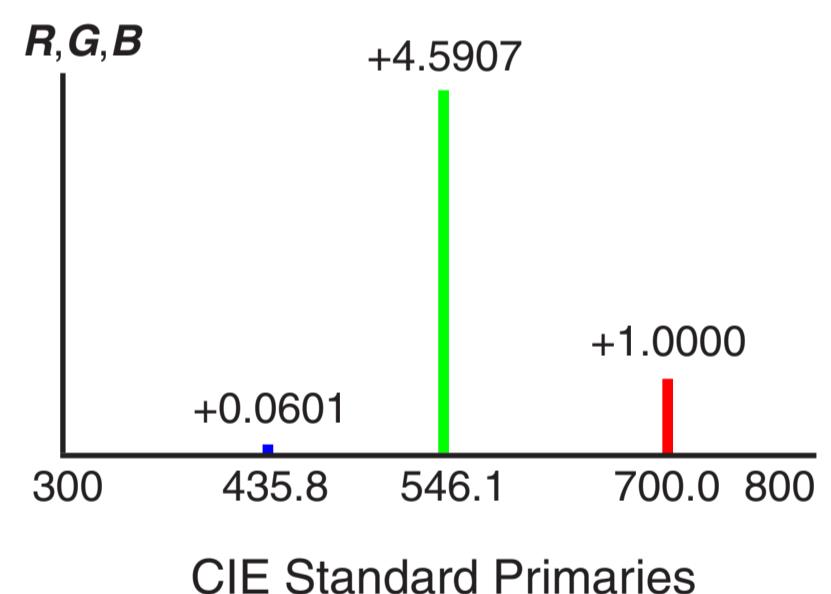
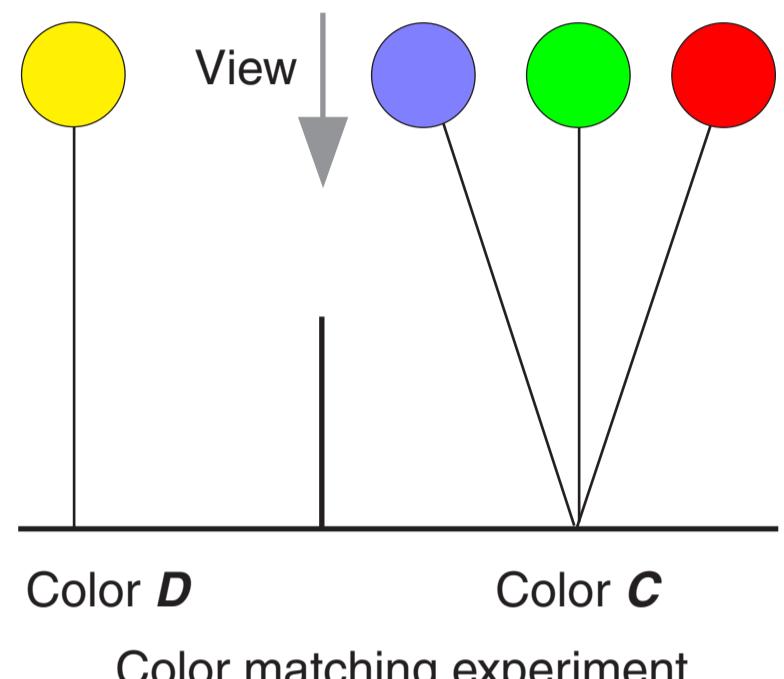
$$\text{Vibrant BlueGreen} = -38\mathbf{R} + 42\mathbf{G} + 91\mathbf{B}$$

This is the introduction of 'negative' colors. The equal sign means 'matched by'. It is generally possible to match a color by three weight factors, but one or even two can be negative (only one for CIE-RGB).

Data for the example are shown in Appendix A.

The CIE Standard Primaries (1931) are narrow band light sources, monochromats, line spectra or delta functions $\mathbf{R}, 700\text{nm}$, $\mathbf{G}, 546.1\text{nm}$ and $\mathbf{B}, 435.8\text{ nm}$.

They replace the red, green and blue lamps in the drawing above. In fact these sources were actually not used – all results were calculated for these primaries after tests with other sources.



The normalized weight factors are called CIE Color-Matching Functions $\bar{r}(\lambda), \bar{g}(\lambda), \bar{b}(\lambda)$.

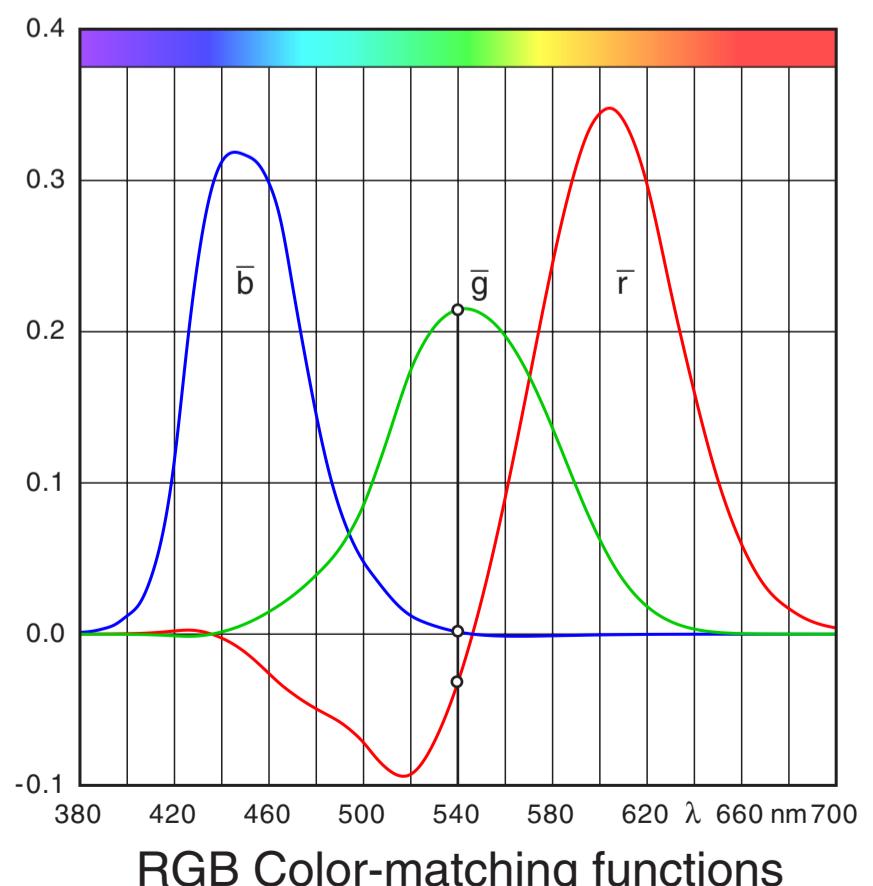
The diagram shows for example the three values for matching a spectral pure color (monochromat) with wavelength $\lambda=540\text{nm}$. This requires a negative value for red.

RGB colors for a spectrum $P(\lambda)$ are calculated by these integrals in the range from 380nm to 700nm or 800nm :

$$R = k \int P(\lambda) \bar{r}(\lambda) d\lambda$$

$$G = k \int P(\lambda) \bar{g}(\lambda) d\lambda$$

$$B = k \int P(\lambda) \bar{b}(\lambda) d\lambda$$



4. XYZ Coordinates

In order to avoid negative RGB numbers, the CIE consortium had introduced a new coordinate system XYZ.

The RGB system is essentially defined by three non-orthogonal base vectors in XYZ.

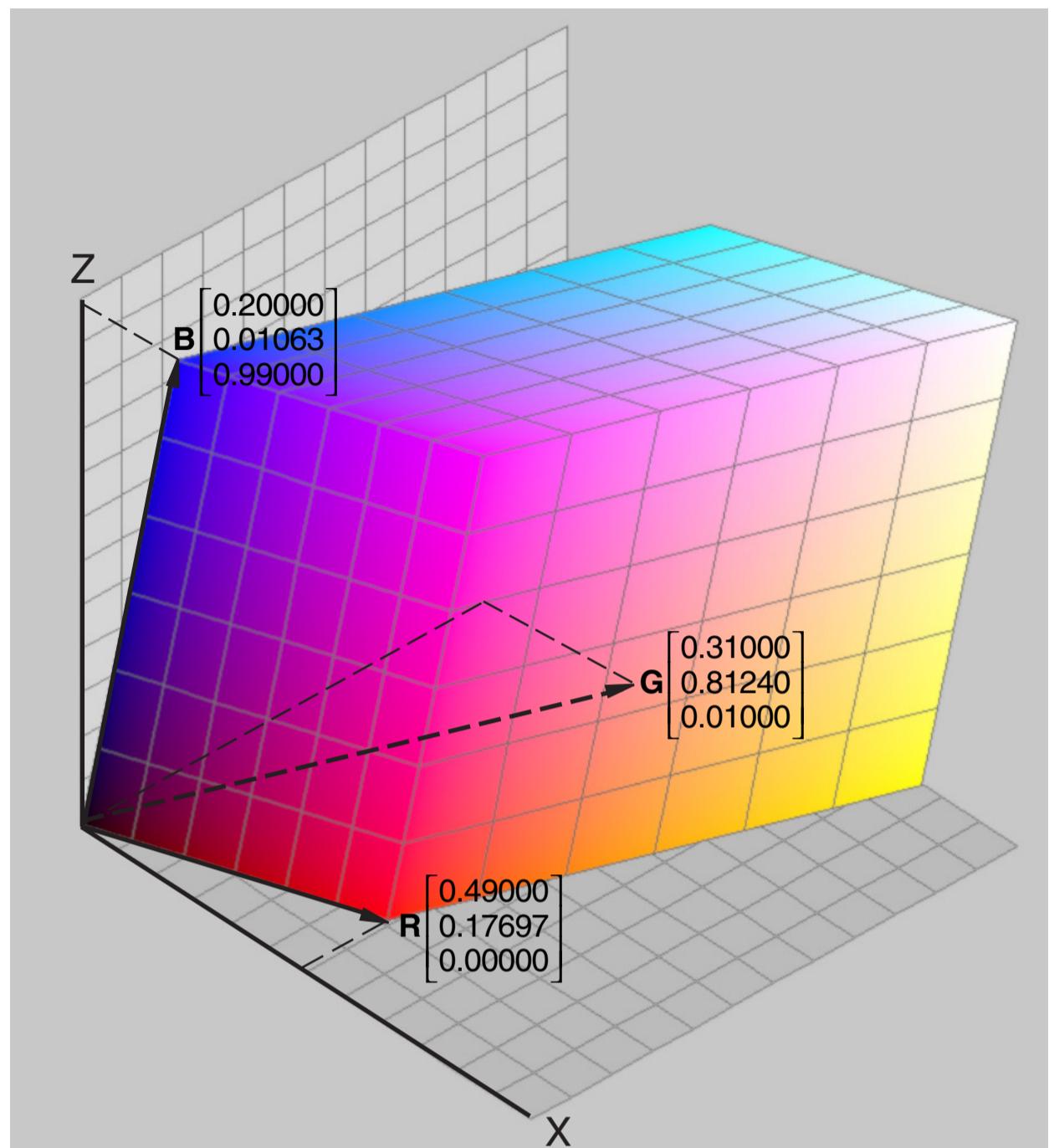
The bottom image explains the situation for 2D coordinates R,G and X,Y a little simplified.

The shaded area shows the human gamut. A plane divides the space in two half spaces.

The new coordinates X,Y are chosen so, that the gamut is entirely accessible for positive values.

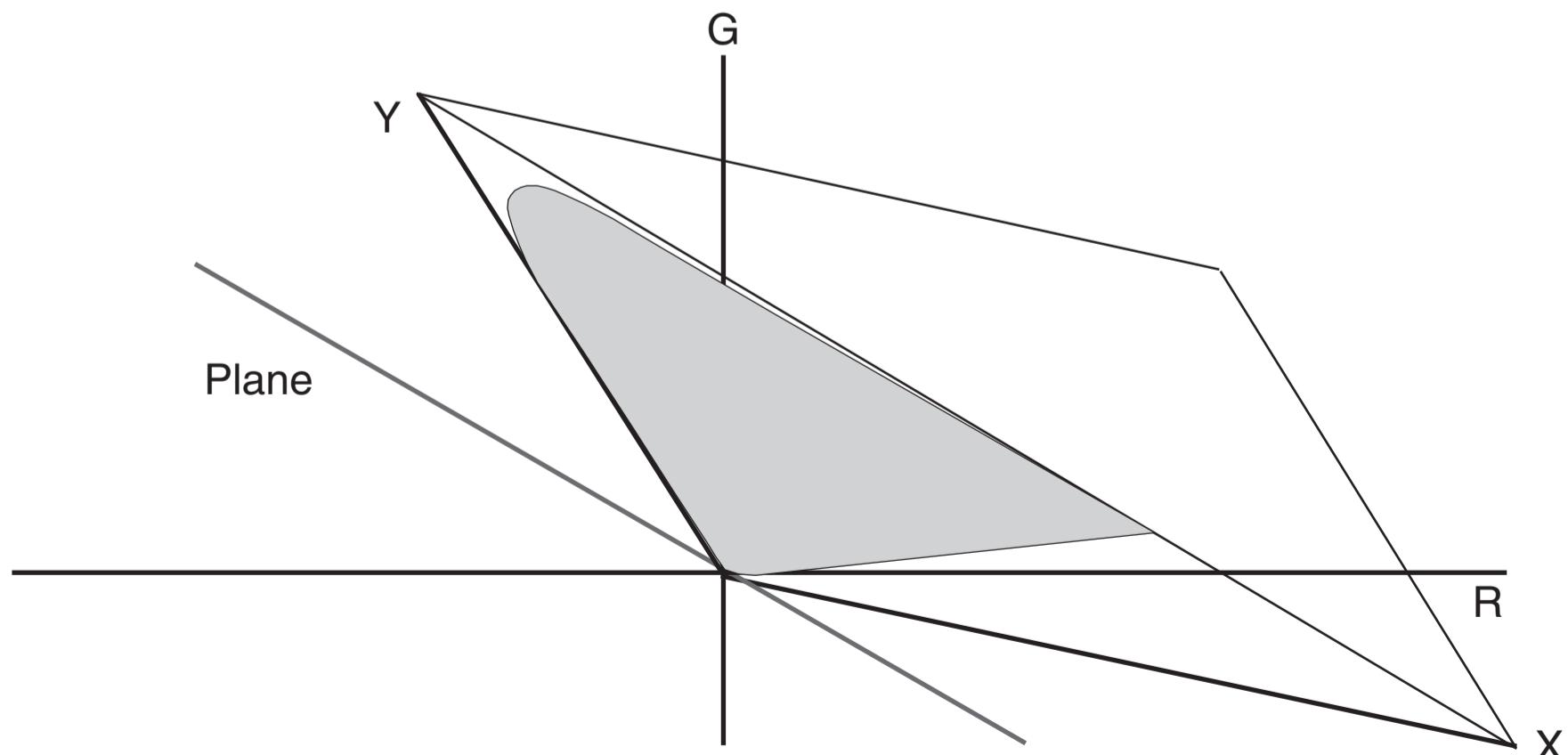
This can be generalized for the 3D space.

In the upper image the axes XYZ are drawn orthogonally, in the lower image the axes RGB.



RGB base vectors and color cube in XYZ

The coordinates of the base vectors in XYZ (coordinates of the primaries as shown above) for any RGB system are found as columns of the matrix C_{xr} in chapter 11.



2D visualization for RG and XY

5. XYZ Primaries (see App. B for further Explanations)

The coordinate systems XYZ and RGB are related to each other by linear equations.

$$X = C_{xr} R$$

$$X = +0.49000R + 0.31000G + 0.20000B$$

$$Y = +0.17697R + 0.81240G + 0.01063B \quad (1)$$

$$Z = +0.00000R + 0.01000G + 0.99000B$$

$$R = C_{rx} X$$

$$R = +2.36461X - 0.89654Y - 0.46807Z$$

$$G = -0.51517X + 1.42641Y + 0.08876Z \quad (2)$$

$$B = +0.00520X - 0.01441Y + 1.00920Z$$

Another view is possible by introducing synthetical or 'imaginary' primaries X, Y, Z .

The Standard Primaries R, G, B are monochromatic stimuli. Mathematically they are single delta functions with well defined areas.

In the diagram the height represents the contribution to the luminance.

The ratios are 1.0:4.5907:0.0601.

The spectra X, Y, Z are calculated by the application of the matrix operation (2) and the scale factors.

An example:

$X=1, Y=0, Z=0$:

$$X = +2.36461 \cdot 1.0000 R$$

$$-0.51517 \cdot 4.5907 G$$

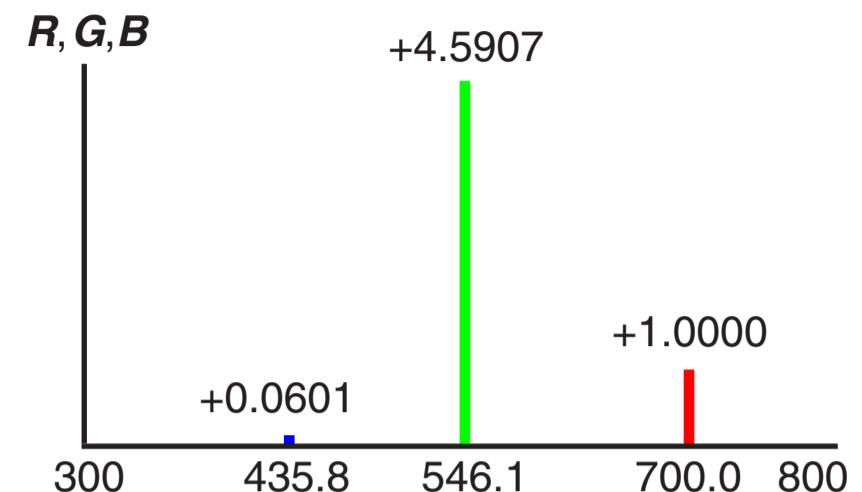
$$+0.00520 \cdot 0.0601 B$$

$$X = +2.36461R - 2.36499G + 0.00031B$$

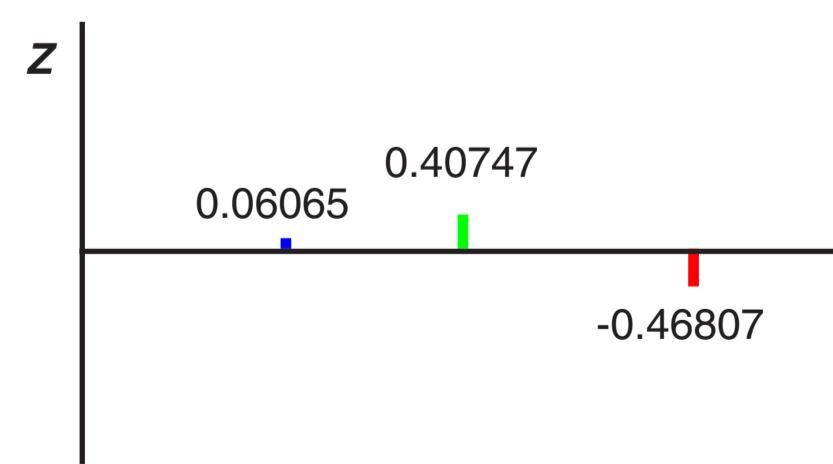
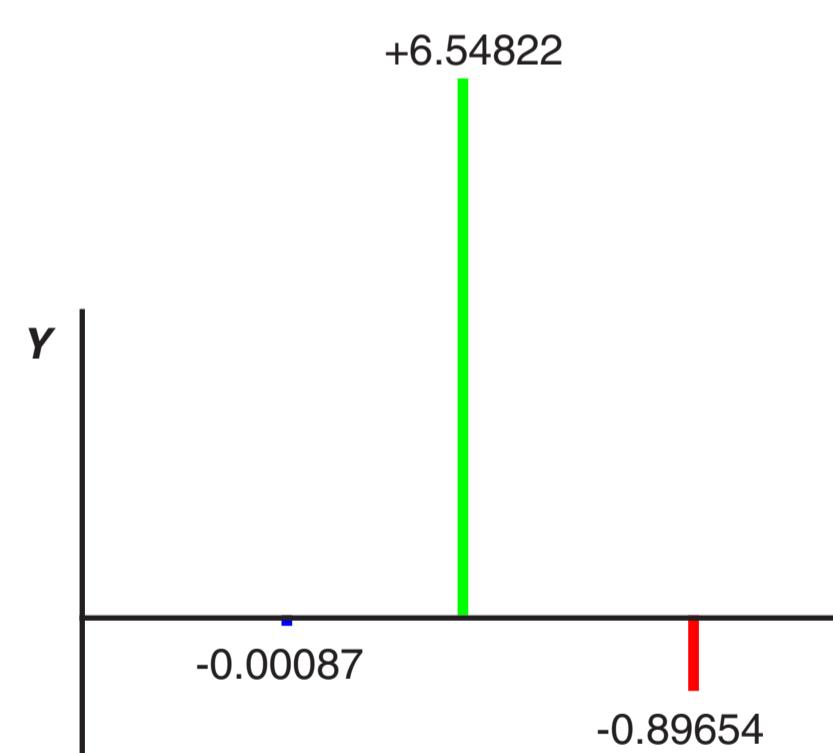
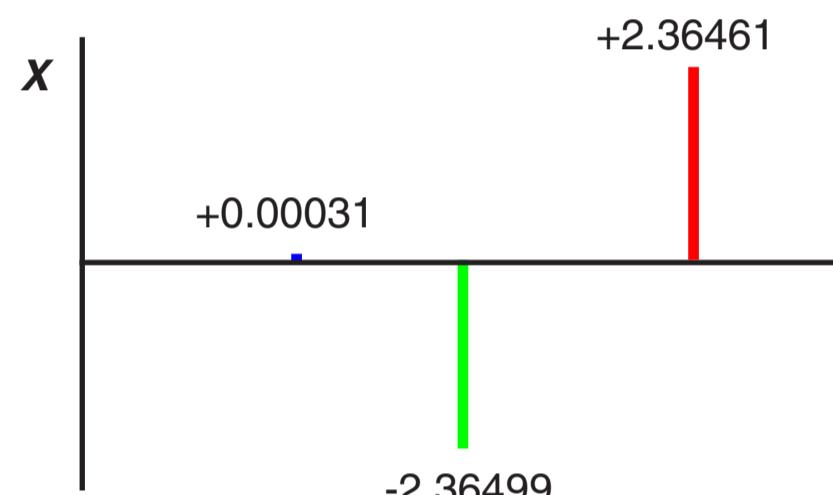
The primaries X, Y, Z are sums of delta functions.

X and Z do not contribute to the luminance. This is a special trick in the CIE system. The integrals are zero, here represented by the sum of the heights.

The luminance is defined by Y only.



CIE primaries R, G, B



Synthetical primaries X, Y, Z

In color matching experiments negative values or weight factors R, G, B are allowed.

Some matchable colors cannot be generated by the Standard Primaries. Other light sources are necessary, especially spectral pure sources (monochromats).

6. XYZ Color-Matching Functions

The new color-matching functions $\bar{x}(\lambda), \bar{y}(\lambda), \bar{z}(\lambda)$ have non-negative values, as expected. They are calculated from $\bar{r}(\lambda), \bar{g}(\lambda), \bar{b}(\lambda)$ by using the matrix \mathbf{C}_{xr} in chapter 5.

The functions $\bar{x}(\lambda), \bar{y}(\lambda), \bar{z}(\lambda)$ can be understood as weight factors. For a spectral pure color \mathbf{C} with a fixed wavelength λ read in the diagram the three values. Then the color can be mixed by the three Standard Primaries:

$$\mathbf{C} = \bar{x}(\lambda) \mathbf{X} + \bar{y}(\lambda) \mathbf{Y} + \bar{z}(\lambda) \mathbf{Z}$$

Generally we write

$$\mathbf{C} = X \mathbf{X} + Y \mathbf{Y} + Z \mathbf{Z}$$

and a given spectral color distribution $P(\lambda)$ delivers the three coordinates XYZ by these integrals in the range from 380nm to 700nm or 800nm:

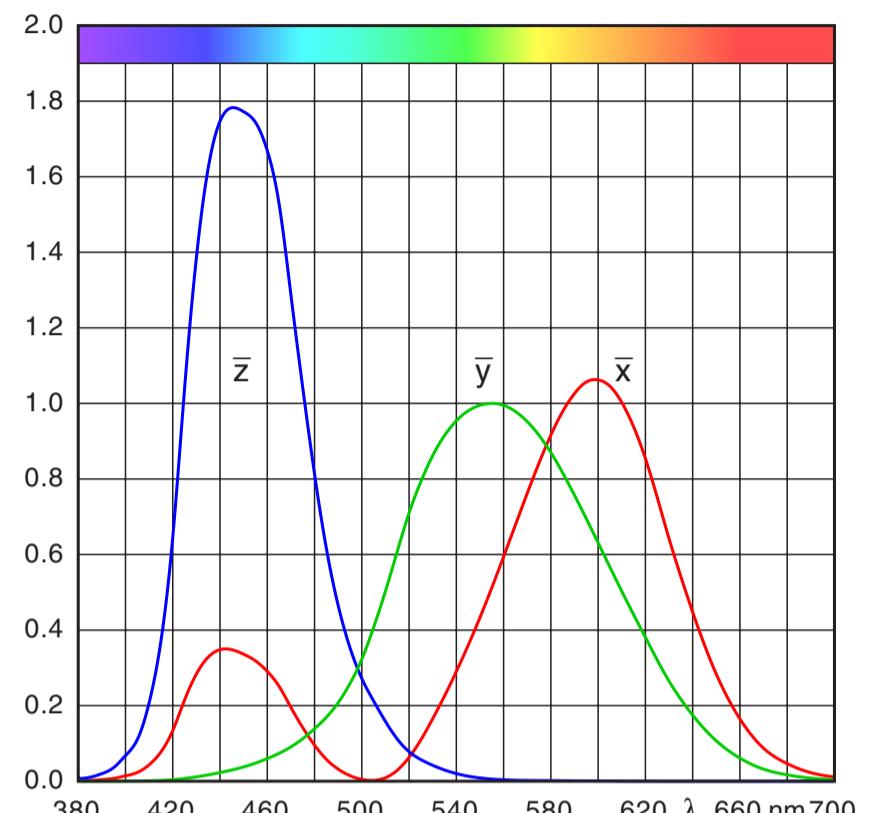
$$X = k \int P(\lambda) \bar{x}(\lambda) d\lambda$$

$$Y = k \int P(\lambda) \bar{y}(\lambda) d\lambda$$

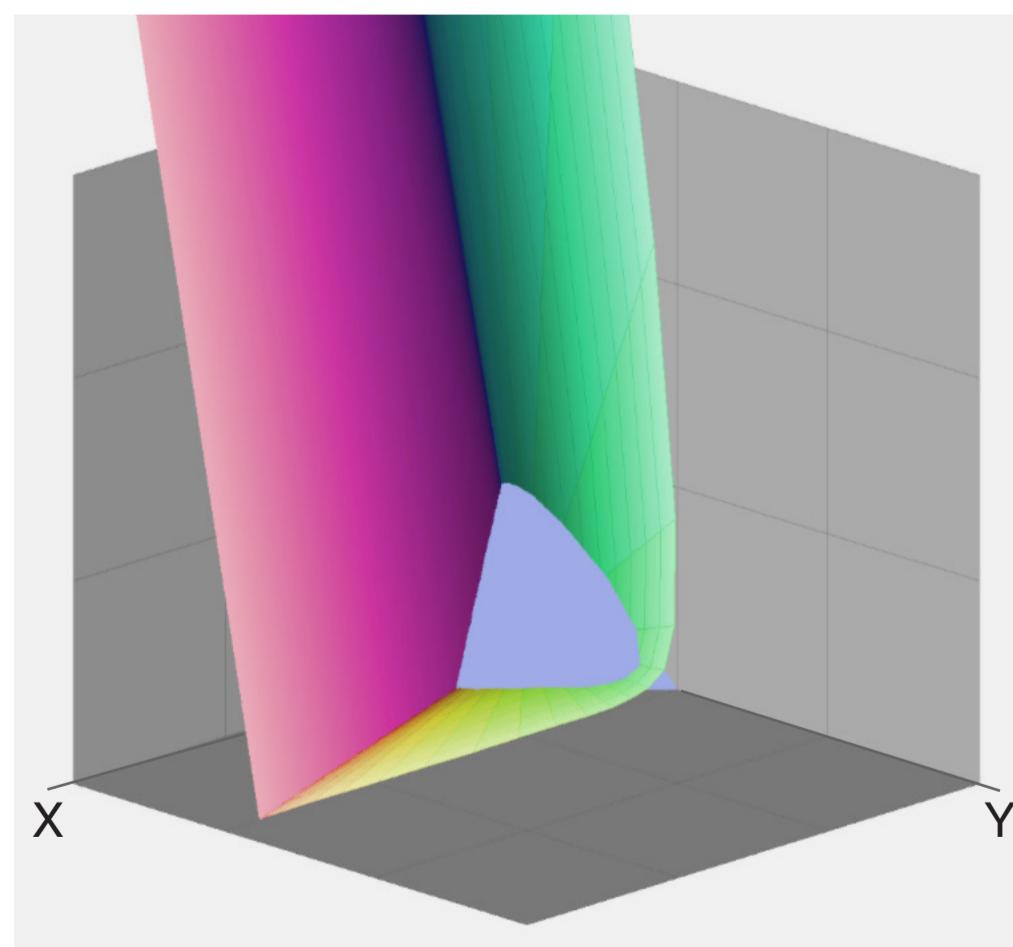
$$Z = k \int P(\lambda) \bar{z}(\lambda) d\lambda$$

Mostly, the arbitrary factor k is chosen for a normalized value $Y=1$ or $Y=100$. Matrix operations are always normalized for R,G,B,Y=0 to 1.

This diagram shows already the human gamut in XYZ. It is an irregularly shaped cone. The intersection with the blue-ish colored plane in the corner will deliver the chromaticity diagram.



XYZ Color-matching functions



Human gamut in XYZ

7. Chromaticity Values

The chromaticity values x, y, z depend only on the hue or dominant wavelength and the saturation. They are independent of the luminance:

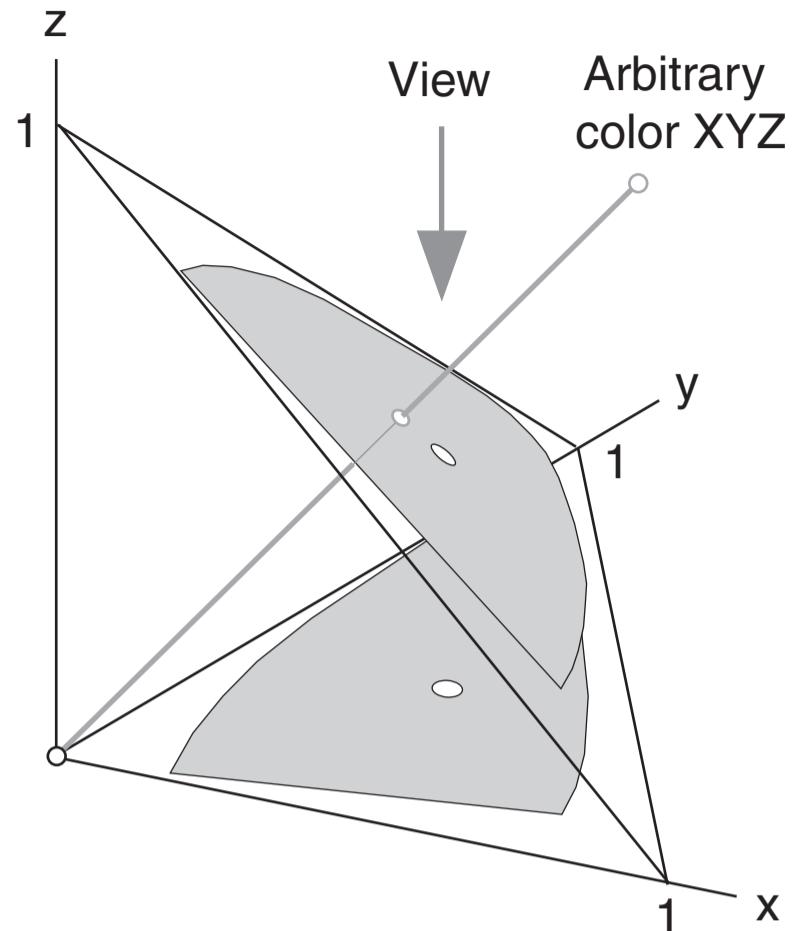
$$x = \frac{X}{X + Y + Z}$$

$$y = \frac{Y}{X + Y + Z}$$

$$z = \frac{Z}{X + Y + Z}$$

Obviously we have $x + y + z = 1$. All the values are on the triangle plane, projected by a line through the arbitrary color XYZ and the origin, if we draw XYZ and xyz in one diagram.

This is a planar projection. The center of projection is in the origin.



Projection and chromaticity plane

The vertical projection onto the xy -plane is the chromaticity diagram xyY (view direction). To reconstruct a color triple XYZ from the chromaticity values xy , we need an additional information, the luminance Y .

$$z = 1 - x - y$$

$$X = \frac{x}{y} Y$$

$$Z = \frac{z}{y} Y$$

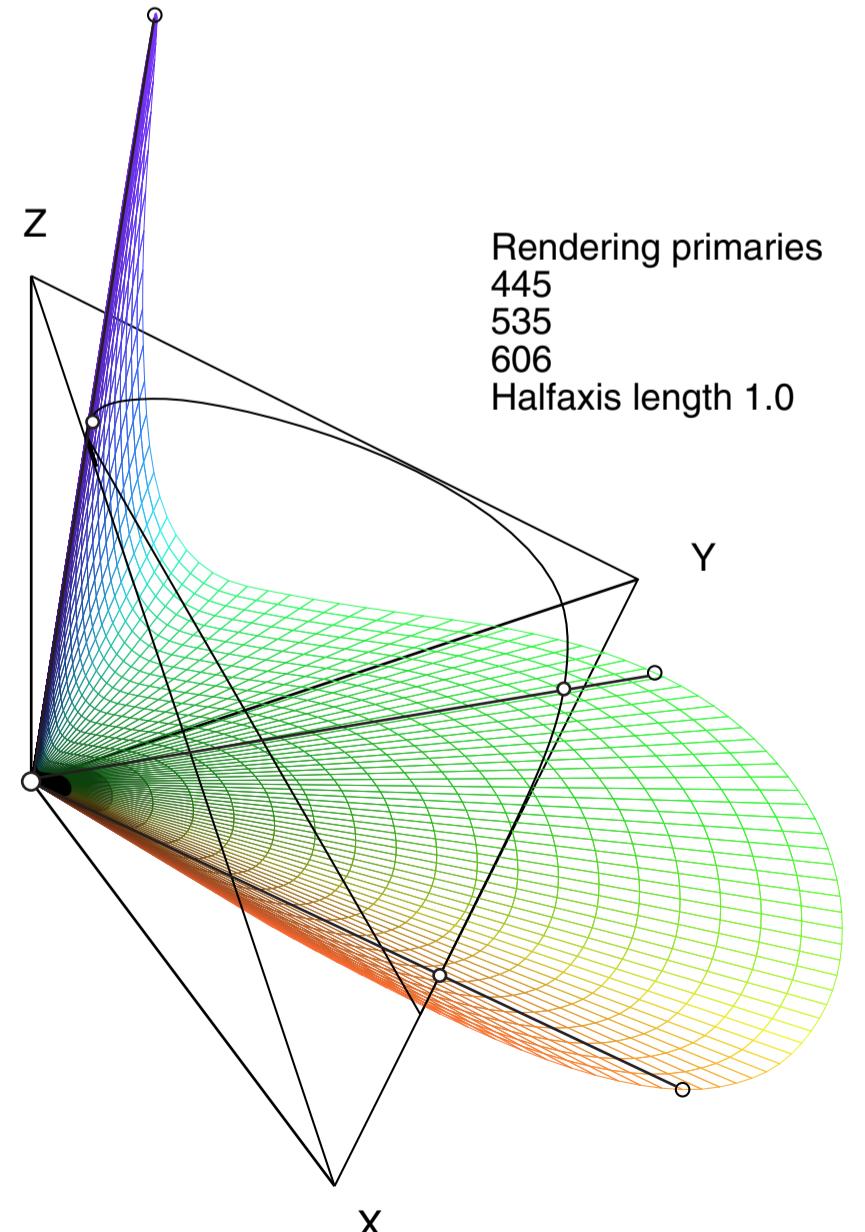
All visible (matchable) colors which differ only by luminance map to the same point in the chromaticity diagram. This is sometimes called 'horseshoe diagram' (page 2).

The right image shows a 3D view of the color-matching functions, connected by rays with the origin. The contour is here called 'locus of unit mono-chromats' [18]. For spectral colors this is the same as XYZ .

Then the contour is mapped onto the plane as above.

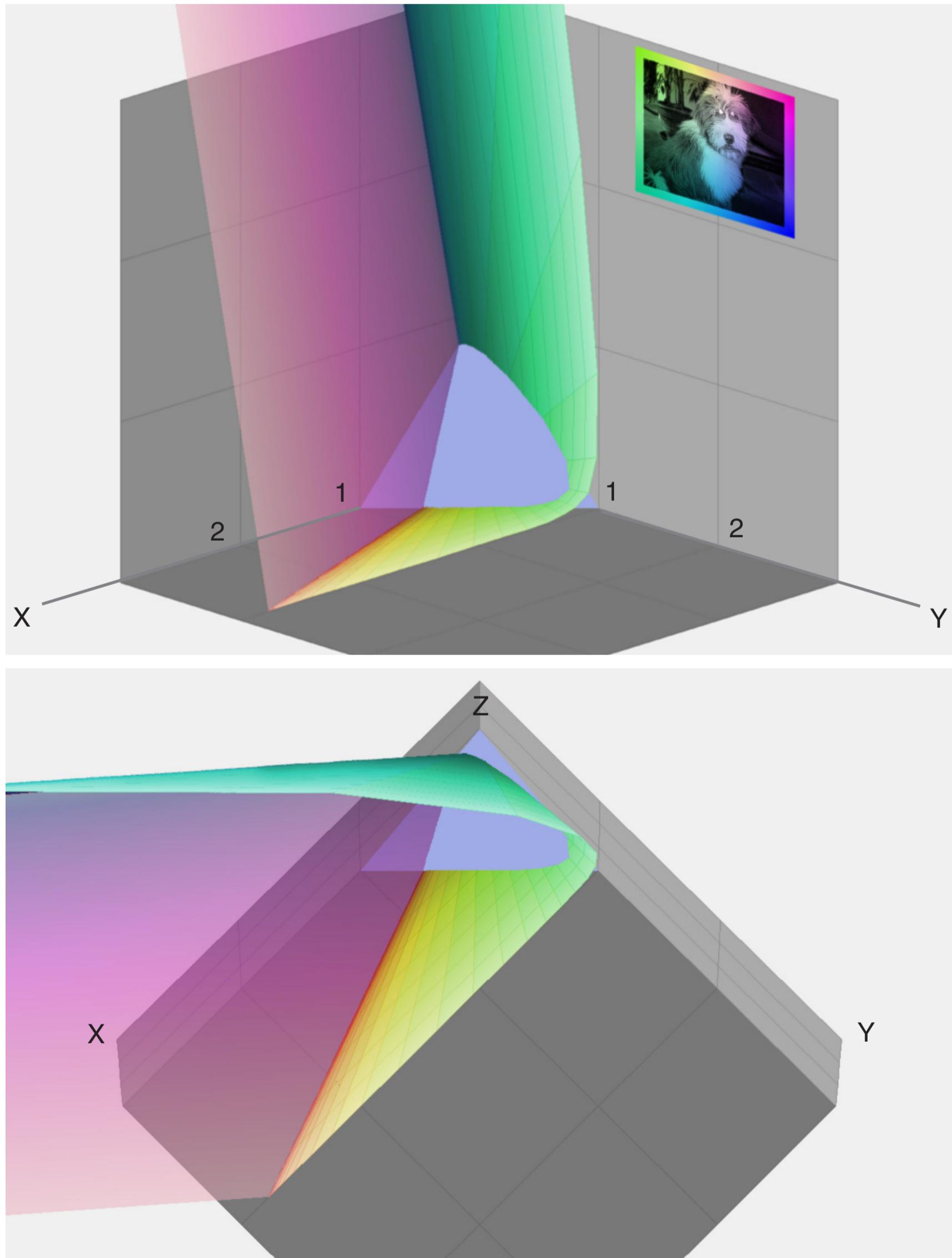
The spectral loci for blue and for red end nearly in the origin: colors with short and long wavelengths appear rather dark, they are almost invisible for a reasonably limited power.

The chromaticity diagram conceals this important fact. The purple line can be considered as a fake. Real purples are inside the horseshoe contour.



8. Color Space Visualization

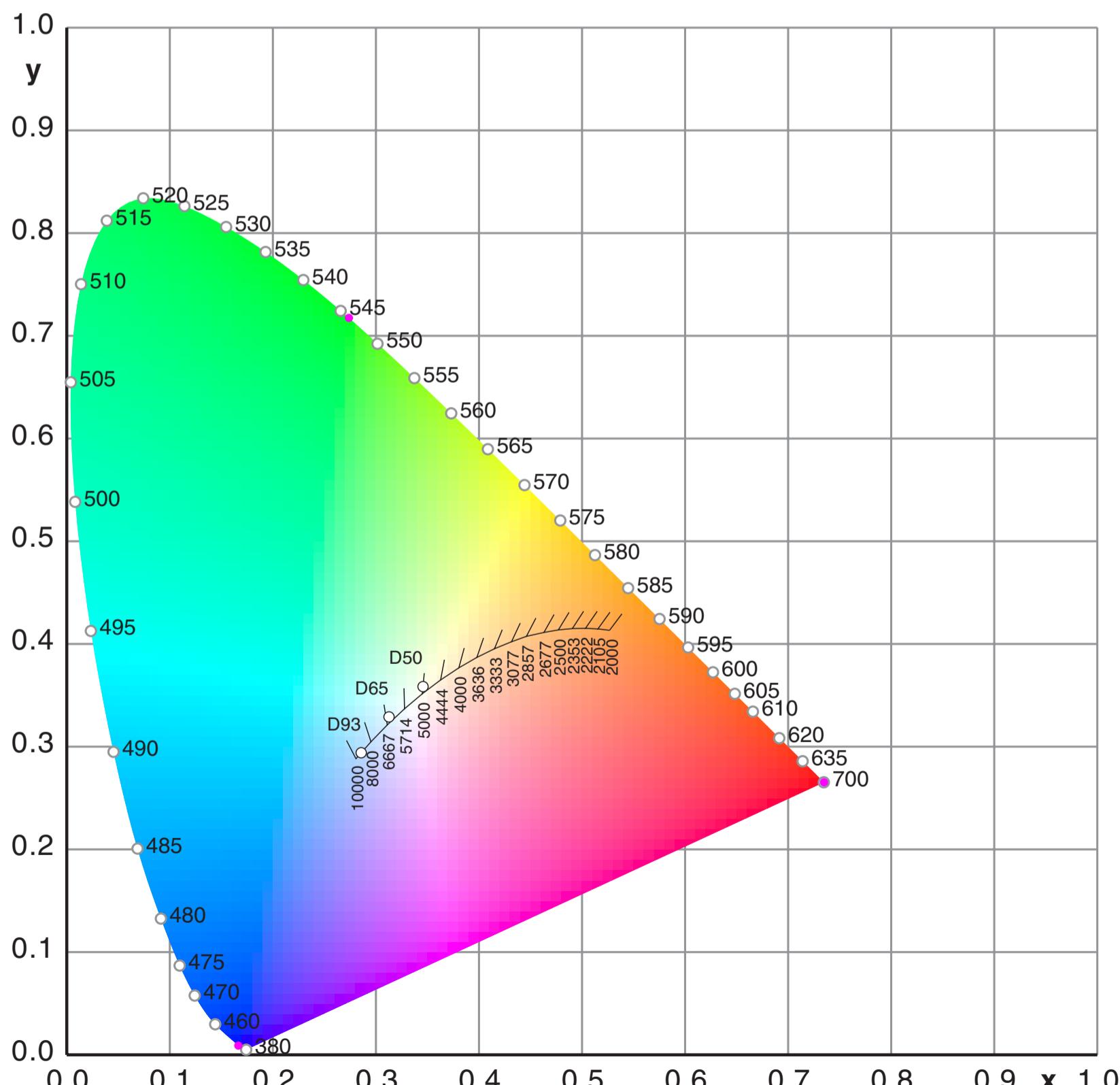
These images are computer graphics. Accurate transformations and a few applications of image processing. The contour of the horseshoe is mapped to XYZ for luminances $Y = 0..1$. The purple plane is shown transparent. All colors were selected for readability. The colors are not correct, this is anyway impossible. More important is here the geometry. The gamut volume is confined by the color surface (pure spectral colors), the purple plane and the plane $Y = 1$. The regions with small values Y appear extremely distorted - near to a singularity. For blue very high values Z are necessary to match a color with specified luminance $Y = 1$.



9. Color Temperature and White Points

The graphic shows the color temperature for the Planck radiator from 2000K to 10000K, the directions of correlated color temperatures and the white points for daylight D50 and D65. Uncalibrated monitors have about 9300K which is here simply called D93. Data by [3]. The EPS graphic is available here [15].

T/K	x	y	Dir y/x
2000	0.52669	0.41331	1.33101
2105	0.51541	0.41465	1.39021
2222	0.50338	0.41525	1.45962
2353	0.49059	0.41498	1.54240
2500	0.47701	0.41368	1.64291
2677	0.463	0.41121	1.76811 % error in table [3], estimated values
2857	0.446	0.40742	1.92863
3077	0.43156	0.40216	2.14300
3333	0.41502	0.39535	2.44455
3636	0.39792	0.38690	2.90309
4000	0.38045	0.37676	3.68730
4444	0.36276	0.36496	5.34398
5000	0.34510	0.35162	11.17883
5714	0.32775	0.33690	-39.34888
6667	0.31101	0.32116	-6.18336
8000	0.29518	0.30477	-3.08425
10000	0.28063	0.28828	-1.93507

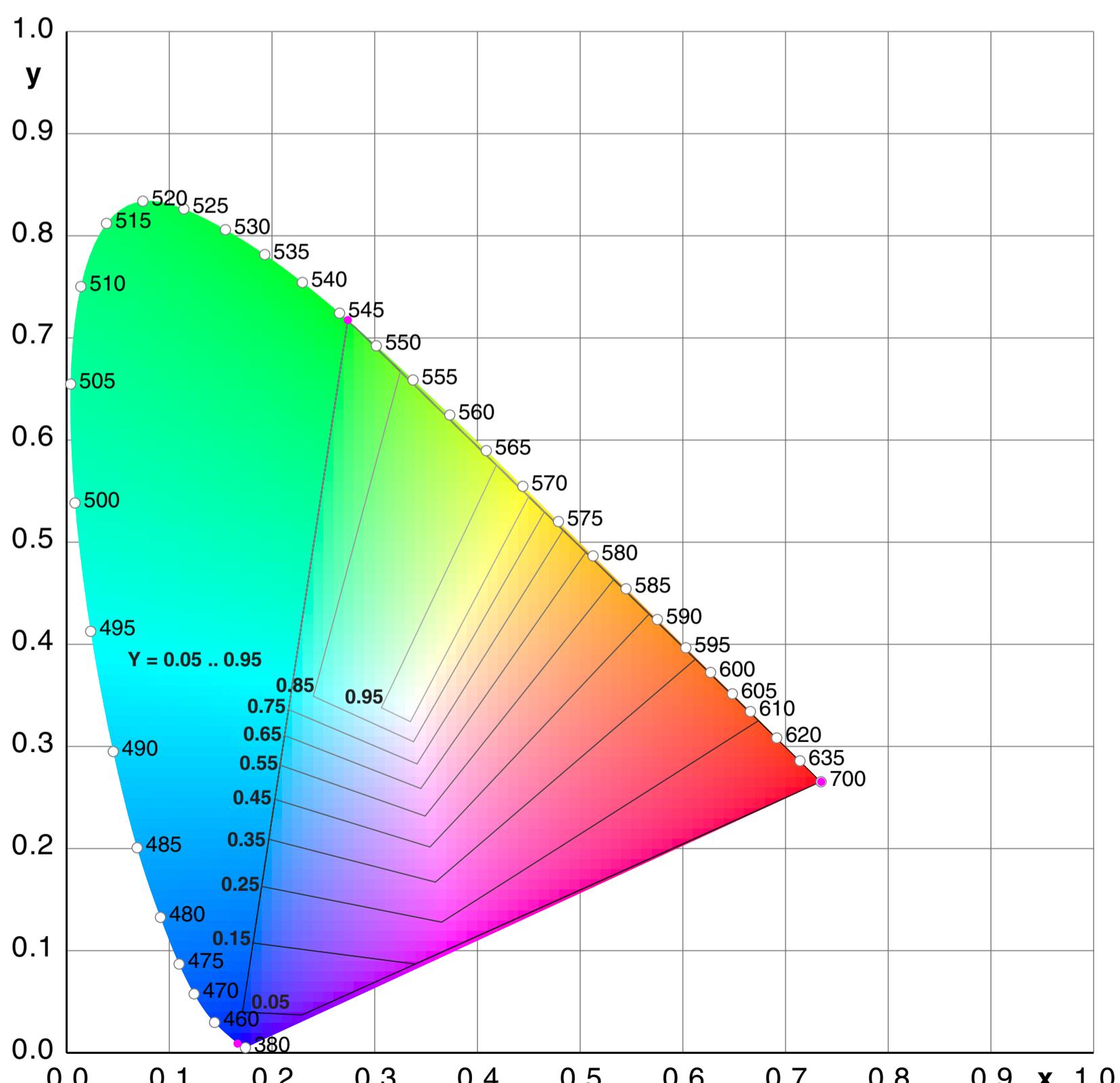


10. CIE RGB Gamut in xyY

The gamut of any RGB system is mostly visualized by a triangle in xyY. For different luminances $Y=\text{const.}$ we get the intersection of a vertical plane and the RGB cube (chapter 4). The intersection delivers a triangle, a quadrilateral, a pentagon or a hexagon. These polygons are projected onto the xy-plane

The chromaticity diagram below shows the actual gamut for different luminances Y. Low luminances seem to produce a large gamut. But that is a fake – a result of the perspective projection from XYZ to xyY.

The gamut appears similarly in all RGB systems. A color outside the triangle (which is defined by the primaries) is always out-of-gamut. A color inside the triangle is not necessarily in-gamut.



11.1 Color Space Calculations / General

In this chapter we derive the relations between CIE xyY, CIE XYZ and any arbitrary RGB space. It is essential to understand the principle of RGB basis vectors in the XYZ coordinate system. This was shown on previous pages.

Given are the coordinates for the primaries in CIE xyY and for the white point: $x_r, y_r, x_g, y_g, x_b, y_b, x_w, y_w$. CIE xyY is the horseshoe diagram. Furtheron we need the luminance V.

We want to derive the relation between any color set r,g,b and the coordinates X,Y,Z .

$$(1) \quad \mathbf{r} = (r, g, b)^T \quad \text{Color values in RGB}$$

$$(2) \quad \mathbf{X} = (X, Y, Z)^T \quad \text{Color values in XYZ}$$

$$(3) \quad \mathbf{x} = (x, y, z)^T \quad \text{Color values in xyY}$$

$$(4) \quad L = X + Y + Z \quad \text{Scaling value}$$

$$(5) \quad x = X/L$$

$$y = Y/L$$

$$z = Z/L$$

$$(6) \quad z = 1 - x - y$$

$$(7) \quad \mathbf{X} = L \mathbf{x}$$

V is the luminance of the stimulus, according to the luminous efficiency function $V(\lambda)$ in [3]. We should not call this immediately Y because Y is mostly normalized for 1 or 100.

$$(8) \quad X = V x / y$$

$$Y = V$$

$$Z = V z / y$$

Basis vectors for the primaries and white point in XYZ:

$$(9) \quad \mathbf{R} = L \mathbf{x}_r = L(x_r, y_r, z_r)^T$$

$$\mathbf{G} = L \mathbf{x}_g = L(x_g, y_g, z_g)^T$$

$$\mathbf{B} = L \mathbf{x}_b = L(x_b, y_b, z_b)^T$$

$$(10) \quad \mathbf{W} = L \mathbf{w} = L(x_w, y_w, z_w)^T$$

Set of scale factors for the white point correction:

$$(11) \quad \mathbf{u} = (u, v, w)^T$$

11.2 Color Space Calculations / General

For the white point correction, the basis vectors $\mathbf{R}, \mathbf{G}, \mathbf{B}$ are scaled by u, v, w . This does not change their coordinates in xyY . The mapping from XYZ to xyY is a central planar projection.

$$(12) \quad \mathbf{X} = L(x, y, z)^T = ru\mathbf{R} + gv\mathbf{G} + bw\mathbf{B}$$

For the white point we have $r = g = b = 1$.

$$(13) \quad \mathbf{W} = L(x_w, y_w, z_w)^T = Lu(x_r, y_r, z_r)^T + Lv(x_g, y_g, z_g)^T + Lw(x_b, y_b, z_b)^T$$

This can be re-arranged, L cancels on both sides.:

$$(14) \quad \begin{bmatrix} x_w \\ y_w \\ z_w \end{bmatrix} = \begin{bmatrix} x_r & x_g & x_b \\ y_r & y_g & y_b \\ z_r & z_g & z_b \end{bmatrix} \begin{bmatrix} u \\ v \\ w \end{bmatrix} = \mathbf{P} \begin{bmatrix} u \\ v \\ w \end{bmatrix}$$

It is not necessary to invert the whole matrix numerically. We can simplify the calculation by adding the first two rows to the third row and find so immediately Eq.(15), which is anyway clear:

$$(15) \quad w = 1 - u - v$$

$$(16) \quad \begin{bmatrix} x_w \\ y_w \end{bmatrix} = \begin{bmatrix} x_r & x_g & x_b \\ y_r & y_g & y_b \end{bmatrix} \begin{bmatrix} u \\ v \\ 1-u-v \end{bmatrix}$$

$$(17) \quad x_w = (x_r - x_b)u + (x_g - x_b)v + x_b \\ y_w = (y_r - y_b)u + (y_g - y_b)v + y_b$$

These linear equations are solved by Cramer's rule.

$$(18) \quad D = (x_r - x_b)(y_g - y_b) - (y_r - y_b)(x_g - x_b)$$

$$U = (x_w - x_b)(y_g - y_b) - (y_w - y_b)(x_g - x_b)$$

$$V = (x_r - x_b)(y_w - y_b) - (y_r - y_b)(x_w - x_b)$$

$$(19) \quad u = U/D$$

$$v = V/D$$

$$w = 1 - u - v$$

In the next step we assume that u, v, w are already calculated and we use the general color transformation Eq.(12) and furtheron Eq.(8). We get the matrices \mathbf{C}_{xr} and \mathbf{C}_{rx} .

$$(20) \quad \begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = V \begin{bmatrix} ux_r/y_w & vx_g/y_w & wx_b/y_w \\ uy_r/y_w & vy_g/y_w & wy_b/y_w \\ uz_r/y_w & vz_g/y_w & wz_b/y_w \end{bmatrix} \begin{bmatrix} r \\ g \\ b \end{bmatrix}$$

$$(21) \quad \mathbf{X} = V \mathbf{C}_{xr} \mathbf{r}$$

$$(22) \quad \mathbf{r} = (1/V) \mathbf{C}_{xr}^{-1} \mathbf{X} = (1/V) \mathbf{C}_{rx} \mathbf{X}$$

11.3 Color Space Calculations / General

For better readability we show the last two equations again, but now with $V=1$, as in most publications.

$$(23) \mathbf{X} = \mathbf{C}_{xr} \mathbf{r}$$

$$(24) \mathbf{r} = \mathbf{C}_{xr}^{-1} \mathbf{X} = \mathbf{C}_{rx} \mathbf{X}$$

Now we can easily derive the relation between two different RGB spaces, e.g. working spaces and image source spaces.

$$(25) \mathbf{X} = \mathbf{C}_{xr1} \mathbf{r}_1$$

$$(26) \mathbf{X} = \mathbf{C}_{xr2} \mathbf{r}_2$$

$$(27) \mathbf{r}_2 = \mathbf{C}_{xr2}^{-1} \mathbf{C}_{xr1} \mathbf{r}_1$$

$$(28) \mathbf{r}_2 = \mathbf{C}_{21} \mathbf{r}_1$$

An example shows the conversion of Rec.709/D65 to D50 and D93. The resulting matrix \mathbf{C}_{21} is diagonal, because the source and destination primaries are the same. The explanation as above is valid for the representation of the same physical color in two different RGB systems. For the simulation of D50 or D93 effects in the same D65 RGB system one has to apply the inverse matrix.

Rec.709			
xr= 0.6400	yr= 0.3300	zr= 0.0300	
xg= 0.3000	yg= 0.6000	zg= 0.1000	
xb= 0.1500	yb= 0.0600	zb= 0.7900	
D65			
xw= 0.3127	yw= 0.3290	zw= 0.3583	
D50			
xw= 0.3457	yw= 0.3585	zw= 0.2958	
Matrix Cxr: X=Cxr*R65			
0.4124 0.3576 0.1805			
0.2126 0.7152 0.0722			
0.0193 0.1192 0.9505			
Matrix Crx: R65=Crx*X			
3.2410 -1.5374 -0.4986			
-0.9692 1.8760 0.0416			
0.0556 -0.2040 1.0570			
Matrix Dxr: X=Dxr*R50			
0.4852 0.3489 0.1303			
0.2502 0.6977 0.0521			
0.0227 0.1163 0.6861			
Matrix Drx: R50=Drx*X			
2.7548 -1.3068 -0.4238			
-0.9935 1.9229 0.0426			
0.0771 -0.2826 1.4644			
Matrix Err: R50=Err*R65=Drx*Cxr*R65			
0.8500 0.0000 0.0000			
0.0000 1.0250 0.0000			
0.0000 0.0000 1.3855			
Matrix Frr: R65=Frr*R50=Crx*Dxr*R50			
1.1765 0.0000 0.0000			
0.0000 0.9756 0.0000			
0.0000 0.0000 0.7218			

Rec.709			
xr= 0.6400	yr= 0.3300	zr= 0.0300	
xg= 0.3000	yg= 0.6000	zg= 0.1000	
xb= 0.1500	yb= 0.0600	zb= 0.7900	
D65			
xw= 0.3127	yw= 0.3290	zw= 0.3583	
D93			
xw= 0.2857	yw= 0.2941	zw= 0.4202	
Matrix Cxr: X=Cxr*R65			
0.4124 0.3576 0.1805			
0.2126 0.7152 0.0722			
0.0193 0.1192 0.9505			
Matrix Crx: R65=Crx*X			
3.2410 -1.5374 -0.4986			
-0.9692 1.8760 0.0416			
0.0556 -0.2040 1.0570			
Matrix Dxr: X=Dxr*R93			
0.3706 0.3554 0.2455			
0.1911 0.7107 0.0982			
0.0174 0.1185 1.2929			
Matrix Drx: R93=Drx*X			
3.6066 -1.7108 -0.5549			
-0.9753 1.8877 0.0418			
0.0409 -0.1500 0.7771			
Matrix Err: R93=Err*R65=Drx*Cxr*R65			
1.1128 0.0000 0.0000			
0.0000 1.0063 0.0000			
0.0000 0.0000 0.7352			
Matrix Frr: R65=Frr*R93=Crx*Dxr*R93			
0.8986 0.0000 0.0000			
0.0000 0.9938 0.0000			
0.0000 0.0000 1.3602			

11.4 Color Space Calculations / Simplified

Now we clean up the mathematics. Eq.(14) delivers:

$$(29) \mathbf{u} = \mathbf{P}^{-1} \mathbf{w}$$

Eq.(12) and Eq.(20) can be written using the diagonal matrix \mathbf{D} with elements u/y_w etc.:

$$(30) \mathbf{X} = \mathbf{P} \mathbf{D} \mathbf{r}$$

$$(31) \mathbf{X} = \mathbf{C}_{xr} \mathbf{r}$$

Together with Eq.(29) we find this simple formula for the matrix \mathbf{C}_{xr} :

$$(32) \mathbf{C}_{xr} = \mathbf{P} \begin{bmatrix} u/y_w & 0 & 0 \\ 0 & v/y_w & 0 \\ 0 & 0 & w/y_w \end{bmatrix}$$

The examples in chapter 12 were written by Pascal. Here is a new example in MatLab.
Calculation of the matrices for sRGB:

```
% G.Hoffmann
% January 14 / 2005
% Matrix Cxr and Crx for sRGB

xr=0.6400; yr=0.3300; zr=1-xr-yr;
xg=0.3000; yg=0.6000; zg=1-xg-yg;
xb=0.1500; yb=0.0600; zb=1-xb-yb;
xw=0.3127; yw=0.3290; zw=1-xw-yw;

W=[xw; yw; zw];
P=[xr xg xb;
   yr yg yb;
   zr zg zb];

u=inv(P)*W

% D=[u(1) 0 0;
%     0 u(2) 0;
%     0 0 u(3)]/yw

D=diag(u/yw)

Cxr=P*D
Crx=inv(Cxr)

% Result:

% Cxr 0.4124    0.3576    0.1805
%      0.2126    0.7152    0.0722
%      0.0193    0.1192    0.9505

% Crx 3.2410    -1.5374   -0.4986
%      -0.9692    1.8760    0.0416
%      0.0556    -0.2040    1.0570
```

11.5 Color Space Calculations / Application

The task: red, green and blue lasers generate monochromatic light at wavelengths 671nm, 532nm and 473nm. The powers are to be adjusted so that the three lasers together deliver white light D65. Calculate the matrices, the radiant power ratios and the photometric ratios.

In order to test the algorithms we are doing the same for CIE primaries and Equal Energy White, just as if the lasers had these primaries. The results are known in advance, based on standard text books. Thanks to Gerhard Fuernkranz for important clarifications.

CIE primaries and white point E

```
% G.Hoffmann
% January 19 / 2005
% Calculations for CIE primaries
% x-bar,y-bar,z-bar interpolated
% 700.0      546.1      435.8 nm
xbr=0.011359; xbg=0.375540; xbb=0.333181;
ybr=0.004102; ybg=0.984430; ybb=0.017769;
zbr=0.000000; zbg=0.012207; zbb=1.649716;
% Equal Energy WP
Xw=1; Yw=1; Zw=1;

%Chromaticity coordinates
D=xbr+ybr+zbr; xr=xbr/D; yr=ybr/D; zr=zbr/D;
D=xbg+ybg+zbg; xg=xbg/D; yg=ybg/D; zg=zbg/D;
D=xbb+ybb+zbb; xb=xbb/D; yb=ybb/D; zb=zbb/D;
D=Xw +Yw+ Zw; xw=Xw/D; yw=Yw/D; zw=Zw/D;

w=[xw; yw; zw];
P=[xr xg xb;
   yr yg yb;
   zr zg zb];

u=inv(P)*w
D=diag(u/yw)

Cxr=P*D
% 0.4902    0.3099    0.1999
% 0.1770    0.8123    0.0107
% 0.0000    0.0101    0.9899
Crx=inv(Cxr)
% 2.3635   -0.8958   -0.4677
% -0.5151    1.4265    0.0887
% 0.0052   -0.0145    1.0093

% Radianc power ratios
Xbar=[xbr xbg xbb;
      ybr ybg ybb;
      zbr zbg zbb];
W=[Xw; Yw; Zw];

R=inv(Xbar)*W

R=R/R(3)
% 71.9166 1.3751 1.0000
% 72.0962 1.3791 1.0000 Wyszecki & Stiles

% Luminous efficiency ratios
L=[R(1)*ybr; R(2)*ybg; R(3)*ybb]
L=L/L(1)
% 1.0000 4.5889 0.0602
% 1.0000 4.5907 0.0601 Wyszecki & Stiles
```

Laser primaries and white point D65

```
% G.Hoffmann
% January 19 / 2005
% Calculations for Laser primaries
% x-bar,y-bar,z-bar interpolated
% 671      532      473 nm
xbr=0.0819; xbg=0.1891; xbb=0.1627;
ybr=0.0300; ybg=0.8850; ybb=0.1034;
zbr=0.0000; zbg=0.0369; zbb=1.1388;
% D65
Xw=0.9504; Yw=1.0000; Zw=1.0890;

%Chromaticity coordinates
D=xbr+ybr+zbr; xr=xbr/D; yr=ybr/D; zr=zbr/D;
D=xbg+ybg+zbg; xg=xbg/D; yg=ybg/D; zg=zbg/D;
D=xbb+ybb+zbb; xb=xbb/D; yb=ybb/D; zb=zbb/D;
D=Xw +Yw+ Zw; xw=Xw/D; yw=Yw/D; zw=Zw/D;

w=[xw; yw; zw];
P=[xr xg xb;
   yr yg yb;
   zr zg zb];

u=inv(P)*w
D=diag(u/yw)

Cxr=P*D
% 0.6571    0.1416    0.1516
% 0.2407    0.6629    0.0964
% 0.0000    0.0276    1.0614
Crx=inv(Cxr)
% 1.6476   -0.3435   -0.2042
% -0.6005    1.6394   -0.0631
% 0.0156   -0.0427    0.9438

% Radianc power ratios
Xbar=[xbr xbg xbb;
      ybr ybg ybb;
      zbr zbg zbb];
W=[Xw; Yw; Zw];

R=inv(Xbar)*W

R=R/R(1)
% 1.0000 0.0934 0.1162
R=R/R(2)
% 10.7111 1.0000 1.2442
R=R/R(3)
% 8.6088 0.8037 1.0000

% Luminous efficiency ratios
L=[R(1)*ybr; R(2)*ybg; R(3)*ybb];
L=L/L(1)
% 1.0000 2.7542 0.4004
L=L/L(2)
% 0.3631 1.0000 0.1454
L=L/L(3)
% 2.4977 6.8791 1.0000
```

12.1 Matrices / CIE + E

CIE Primaries and white point E [3]. Page 5 shows the same results.
Data are in the Pascal source code.

```
Program CiCalcCi;
{ Calculations RGB-CIE }
{ G.Hoffmann February 01, 2002 }
Uses Crt,Dos,Zgraph00;
Var r,g,b,x,y,z,u,v,w,d          : Extended;
    i,j,k,flag                  : Integer;
    xr,yr,zr,xg,yg,zg,xb,yb,zb,xw,yw,zw : Extended;
    prn,cie                      : Text;
Var Cxr,Crx: ANN;
Begin
  ClrScr;
  { CIE Primaries }
  xr:=0.73467;
  yr:=0.26533;
  zr:=1-xr-yr;
  xg:=0.27376;
  yg:=0.71741;
  zg:=1-xg-yg;
  xb:=0.16658;
  yb:=0.00886;
  zb:=1-xb-yb;
  { CIE White Point }
  xw:=1/3;
  yw:=1/3;
  zw:=1-xw-yw;
  { White Point Correction }
  D:=(xr-xb)*(yg-yb)-(yr-yb)*(xg-xb);
  U:=(xw-xb)*(yg-yb)-(yw-yb)*(xg-xb);
  V:=(xr-xb)*(yw-yb)-(yr-yb)*(xw-xb);
  u:=U/D;
  v:=V/D;
  w:=1-u-v;
  { Matrix Cxr }
  Cxr[1,1]:=u*xr/yw; Cxr[1,2]:=v*xg/yw; Cxr[1,3]:=w*xb/yw;
  Cxr[2,1]:=u*yr/yw; Cxr[2,2]:=v*yg/yw; Cxr[2,3]:=w*yb/yw;
  Cxr[3,1]:=u*zr/yw; Cxr[3,2]:=v*zg/yw; Cxr[3,3]:=w*zb/yw;
  { Matrix Crx }
  HoInvers (3,Cxr,Crx,D,flag);

  Assign (prn,'C:\CiCalcCi.txt'); ReWrite(prn);

  Writeln (prn,'      Matrix Cxr');
  Writeln (prn,Cxr[1,1]:12:4, Cxr[1,2]:12:4, Cxr[1,3]:12:4);
  Writeln (prn,Cxr[2,1]:12:4, Cxr[2,2]:12:4, Cxr[2,3]:12:4);
  Writeln (prn,Cxr[3,1]:12:4, Cxr[3,2]:12:4, Cxr[3,3]:12:4);

  Writeln (prn,'      Matrix Crx');
  Writeln (prn,Crx[1,1]:12:4, Crx[1,2]:12:4, Crx[1,3]:12:4);
  Writeln (prn,Crx[2,1]:12:4, Crx[2,2]:12:4, Crx[2,3]:12:4);
  Writeln (prn,Crx[3,1]:12:4, Crx[3,2]:12:4, Crx[3,3]:12:4);
  Close(prn);
  Readln;
End.
```

Matrix Cxr
X 0.4900 0.3100 0.2000
Y 0.1770 0.8124 0.0106
Z -0.0000 0.0100 0.9900

$$\mathbf{X} = \mathbf{C}_{xr} \mathbf{R}$$

Matrix Crx
R 2.3647 -0.8966 -0.4681
G -0.5152 1.4264 0.0887
B 0.0052 -0.0144 1.0092

$$\mathbf{R} = \mathbf{C}_{rx} \mathbf{X}$$

12.2 Matrices / 709 + D65 / sRGB

ITU-R BT.709 Primaries and white point D65 [9]. Valid for sRGB.
Data are in the Pascal source code.

```
Program CiCalc65;
{ Calculations RGB-CIE }
{ G.Hoffmann February 01, 2002 }
Uses Crt,Dos,Zgraph00;
Var r,g,b,x,y,z,u,v,w,d           : Extended;
    i,j,k,flag                      : Integer;
    xr,yr,zr,xg,yg,zg,xb,yb,zb,xw,yw,zw : Extended;
    prn,cie                          : Text;
Var Cxr,Crx: ANN;
Begin
  ClrScr;
  { Rec 709 Primaries }
  xr:=0.6400;
  yr:=0.3300;
  zr:=1-xr-yr;
  xg:=0.3000;
  yg:=0.6000;
  zg:=1-xg-yg;
  xb:=0.1500;
  yb:=0.0600;
  zb:=1-xb-yb;
  { D65 White Point }
  xw:=0.3127;
  yw:=0.3290;
  zw:=1-xw-yw;
  { White Point Correction }
  D:=(xr-xb)*(yg-yb)-(yr-yb)*(xg-xb);
  U:=(xw-xb)*(yg-yb)-(yw-yb)*(xg-xb);
  V:=(xr-xb)*(yw-yb)-(yr-yb)*(xw-xb);
  u:=U/D;
  v:=V/D;
  w:=1-u-v;
  { Matrix Cxr }
  Cxr[1,1]:=u*xr/yw; Cxr[1,2]:=v*xg/yw; Cxr[1,3]:=w*xb/yw;
  Cxr[2,1]:=u*yr/yw; Cxr[2,2]:=v*yg/yw; Cxr[2,3]:=w*yb/yw;
  Cxr[3,1]:=u*zr/yw; Cxr[3,2]:=v*zg/yw; Cxr[3,3]:=w*zb/yw;
  { Matrix Crx }
  HoInvers (3,Cxr,Crx,D,flag);

  Assign (prn,'C:\CiMalc65.txt'); ReWrite(prn);

  Writeln (prn,'      Matrix Cxr');
  Writeln (prn,Cxr[1,1]:12:4, Cxr[1,2]:12:4, Cxr[1,3]:12:4);
  Writeln (prn,Cxr[2,1]:12:4, Cxr[2,2]:12:4, Cxr[2,3]:12:4);
  Writeln (prn,Cxr[3,1]:12:4, Cxr[3,2]:12:4, Cxr[3,3]:12:4);

  Writeln (prn,'      Matrix Crx');
  Writeln (prn,Crx[1,1]:12:4, Crx[1,2]:12:4, Crx[1,3]:12:4);
  Writeln (prn,Crx[2,1]:12:4, Crx[2,2]:12:4, Crx[2,3]:12:4);
  Writeln (prn,Crx[3,1]:12:4, Crx[3,2]:12:4, Crx[3,3]:12:4);
  Close(prn);
  Readln;
End.
```

Matrix Cxr
X 0.4124 0.3576 0.1805
Y 0.2126 0.7152 0.0722
Z 0.0193 0.1192 0.9505

$$\mathbf{X} = \mathbf{C}_{\mathbf{xr}} \mathbf{R}$$

Matrix Crx
R 3.2410 -1.5374 -0.4986
G -0.9692 1.8760 0.0416
B 0.0556 -0.2040 1.0570

$$\mathbf{R} = \mathbf{C}_{\mathbf{rx}} \mathbf{X}$$

12.3 Matrices / AdobeRGB + D65

AdobeRGB(98), D65.
Data are in the Pascal source code.

```
Program CiCalc98;
{ Calculations RGB-AdobeRGB98 }
{ G.Hoffmann März 28, 2004 }
Uses Crt,Dos,Zgraph00;
Var r,g,b,x,y,z,u,v,w,d          : Double;
    i,j,k,flag                  : Integer;
    xr,yr,zr,xg,yg,zg,xb,yb,zb,xw,yw,zw : Double;
    prn,cie                      : Text;
Var Cxr,Crx: ANN;
Begin
  ClrScr;
  { AdobeRGB(98) }
  xr:=0.6400;
  yr:=0.3300;
  zr:=1-xr-yr;
  xg:=0.2100;
  yg:=0.7100;
  zg:=1-xg-yg;
  xb:=0.1500;
  yb:=0.0600;
  zb:=1-xb-yb;
  { D65 White Point }
  xw:=0.3127;
  yw:=0.3290;
  zw:=1-xw-yw;
  { White Point Correction }
  D:=(xr-xb)*(yg-yb)-(yr-yb)*(xg-xb);
  U:=(xw-xb)*(yg-yb)-(yw-yb)*(xg-xb);
  V:=(xr-xb)*(yw-yb)-(yr-yb)*(xw-xb);
  u:=U/D;
  v:=V/D;
  w:=1-u-v;
  { Matrix Cxr }
  Cxr[1,1]:=u*xr/yw; Cxr[1,2]:=v*xg/yw; Cxr[1,3]:=w*xb/yw;
  Cxr[2,1]:=u*yr/yw; Cxr[2,2]:=v*yg/yw; Cxr[2,3]:=w*yb/yw;
  Cxr[3,1]:=u*zr/yw; Cxr[3,2]:=v*zg/yw; Cxr[3,3]:=w*zb/yw;
  { Matrix Crx }
  HoInvers (3,Cxr,Crx,D,flag);

  Assign (prn,'C:\CiMalc98.txt'); ReWrite(prn);

  Writeln (prn,'      Matrix Cxr');
  Writeln (prn,Cxr[1,1]:12:4, Cxr[1,2]:12:4, Cxr[1,3]:12:4);
  Writeln (prn,Cxr[2,1]:12:4, Cxr[2,2]:12:4, Cxr[2,3]:12:4);
  Writeln (prn,Cxr[3,1]:12:4, Cxr[3,2]:12:4, Cxr[3,3]:12:4);
  Writeln (prn,'');
  Writeln (prn,'      Matrix Crx');
  Writeln (prn,Crx[1,1]:12:4, Crx[1,2]:12:4, Crx[1,3]:12:4);
  Writeln (prn,Crx[2,1]:12:4, Crx[2,2]:12:4, Crx[2,3]:12:4);
  Writeln (prn,Crx[3,1]:12:4, Crx[3,2]:12:4, Crx[3,3]:12:4);
  Writeln (prn,'dummy');
  Readln;
End.
```

Matrix Cxr
X 0.5767 0.1856 0.1882
Y 0.2973 0.6274 0.0753
Z 0.0270 0.0707 0.9913

$$\mathbf{X} = \mathbf{C}_{xr} \mathbf{R}$$

Matrix Crx
R 2.0416 -0.5650 -0.3447
G -0.9692 1.8760 0.0416
B 0.0134 -0.1184 1.0152

$$\mathbf{R} = \mathbf{C}_{rx} \mathbf{X}$$

12.4 Matrices / NTSC + C

NTSC Primaries and white point C [4], also used as YIQ Model.
Data are in the Pascal source code.

```

Program CiCalcNT;
{ Calculations RGB-NTSC }
{ G.Hoffmann April 01, 2002 }
Uses Crt,Dos,Zgraph00;
Var r,g,b,x,y,z,u,v,w,d          : Extended;
    i,j,k,flag                   : Integer;
    xr,yr,zr,xg,yg,zg,xb,yb,zb,xw,yw,zw : Extended;
    prn,cie                      : Text;
Var Cxr,Crx: ANN;
Begin
  ClrScr;
  { NTSC Primaries }
  xr:=0.6700;
  yr:=0.3300;
  zr:=1-xr-yr;
  xg:=0.2100;
  yg:=0.7100;
  zg:=1-xg-yg;
  xb:=0.1400;
  yb:=0.0800;
  zb:=1-xb-yb;
  { NTSC White Point }
  xw:=0.3100;
  yw:=0.3160;
  zw:=1-xw-yw;
  { White Point Correction }
  D:=(xr-xb)*(yg-yb)-(yr-yb)*(xg-xb);
  U:=(xw-xb)*(yg-yb)-(yw-yb)*(xg-xb);
  V:=(xr-xb)*(yw-yb)-(yr-yb)*(xw-xb);
  u:=U/D;
  v:=V/D;
  w:=1-u-v;
  { Matrix Cxr }
  Cxr[1,1]:=u*xr/yw; Cxr[1,2]:=v*xg/yw; Cxr[1,3]:=w*xb/yw;
  Cxr[2,1]:=u*yr/yw; Cxr[2,2]:=v*yg/yw; Cxr[2,3]:=w*yb/yw;
  Cxr[3,1]:=u*zr/yw; Cxr[3,2]:=v*zg/yw; Cxr[3,3]:=w*zb/yw;
  { Matrix Crx }
  HoInvers (3,Cxr,Crx,D,flag);

  Assign (prn,'C:\CiMalcNT.txt'); ReWrite(prn);

  Writeln (prn,'      Matrix Cxr');
  Writeln (prn,Cxr[1,1]:12:4, Cxr[1,2]:12:4, Cxr[1,3]:12:4);
  Writeln (prn,Cxr[2,1]:12:4, Cxr[2,2]:12:4, Cxr[2,3]:12:4);
  Writeln (prn,Cxr[3,1]:12:4, Cxr[3,2]:12:4, Cxr[3,3]:12:4);
  Writeln (prn,'');
  Writeln (prn,'      Matrix Crx');
  Writeln (prn,Crx[1,1]:12:4, Crx[1,2]:12:4, Crx[1,3]:12:4);
  Writeln (prn,Crx[2,1]:12:4, Crx[2,2]:12:4, Crx[2,3]:12:4);
  Writeln (prn,Crx[3,1]:12:4, Crx[3,2]:12:4, Crx[3,3]:12:4);
  Close(prn);
  Readln;
End.

```

Matrix Cxr
X 0.6070 0.1734 0.2006
Y 0.2990 0.5864 0.1146
Z -0.0000 0.0661 1.1175

$$\mathbf{X} = \mathbf{C}_{xr} \mathbf{R}$$

Matrix Crx
R 1.9097 -0.5324 -0.2882
G -0.9850 1.9998 -0.0283
B 0.0582 -0.1182 0.8966

$$\mathbf{R} = \mathbf{C}_{rx} \mathbf{X}$$

12.5 Matrices / NTSC + C + YIQ

NTSC Primaries and white point C [4], YIQ Conversion.
Data are in the Pascal source code.

```
Program CiCalcYI;
{ Calculations RGB-NTSC YIQ }
{ G.Hoffmann April 01, 2002 }
Uses Crt,Dos,Zgraph00;
Var r,g,b,x,y,z,u,v,w,d           : Extended;
    i,j,k,flag                      : Integer;
    xr,yr,zr,xg,yg,zg,xb,yb,zb,xw,yw,zw : Extended;
    prn,cie                          : Text;
Var Cyr,Cry: ANN;
Begin
  ClrScr;
  { NTSC Primaries }
  xr:=0.6700;
  yr:=0.3300;
  zr:=1-xr-yr;
  xg:=0.2100;
  yg:=0.7100;
  zg:=1-xg-yg;
  xb:=0.1400;
  yb:=0.0800;
  zb:=1-xb-yb;
  { NTSC White Point }
  xw:=0.3100;
  yw:=0.3160;
  zw:=1-xw-yw;
  { Matrix Cyr, Sequence Y I Q }
  Cyr[1,1]:= 0.299; Cyr[1,2]:= 0.587; Cyr[1,3]:= 0.114;
  Cyr[2,1]:= 0.596; Cyr[2,2]:=-0.275; Cyr[2,3]:=-0.321;
  Cyr[3,1]:= 0.212; Cyr[3,2]:=-0.528; Cyr[3,3]:= 0.311;
  { Matrix Cry }
  HoInvers (3,Cyr,Cry,D,flag);

  Assign (prn,'C:\CiMalcYI.txt'); ReWrite(prn);

  Writeln (prn,'      Matrix Cyr');
  Writeln (prn,Cyr[1,1]:12:4, Cyr[1,2]:12:4, Cyr[1,3]:12:4);
  Writeln (prn,Cyr[2,1]:12:4, Cyr[2,2]:12:4, Cyr[2,3]:12:4);
  Writeln (prn,Cyr[3,1]:12:4, Cyr[3,2]:12:4, Cyr[3,3]:12:4);
  Writeln (prn,'');
  Writeln (prn,'      Matrix Cry');
  Writeln (prn,Cry[1,1]:12:4, Cry[1,2]:12:4, Cry[1,3]:12:4);
  Writeln (prn,Cry[2,1]:12:4, Cry[2,2]:12:4, Cry[2,3]:12:4);
  Writeln (prn,Cry[3,1]:12:4, Cry[3,2]:12:4, Cry[3,3]:12:4);
  Close(prn);
  Readln;
End.
```

Matrix Cyr
Y 0.2990 0.5870 0.1140
I 0.5960 -0.2750 -0.3210
Q 0.2120 -0.5280 0.3110

$$\mathbf{Y} = \mathbf{C}_{\text{yr}} \mathbf{R}$$

Matrix Cry
R 1.0031 0.9548 0.6179
G 0.9968 -0.2707 -0.6448
B 1.0085 -1.1105 1.6996

$$\mathbf{R} = \mathbf{C}_{\text{ry}} \mathbf{Y}$$

12.6 Matrices / NTSC + C + YCbCr

NTSC Primaries and white point C [4], YCbCr Conversion.
Data are in the Pascal source code.

```
Program CiCalcYC;
{ Calculations RGB-NTSC YCbCr }
{ G.Hoffmann April 03, 2002 }
Uses Crt,Dos,Zgraph00;
Var r,g,b,x,y,z,u,v,w,d : Extended;
    i,j,k,flag : Integer;
    xr,yr,zr,xg,yg,zg,xb,yb,zb,xw,yw,zw : Extended;
    prn,cie : Text;
Var Cyr,Cry: ANN;
Begin
  ClrScr;
  { NTSC Primaries }
  xr:=0.6700;
  yr:=0.3300;
  zr:=1-xr-yr;
  xg:=0.2100;
  yg:=0.7100;
  zg:=1-xg-yg;
  xb:=0.1400;
  yb:=0.0800;
  zb:=1-xb-yb;
  { NTSC White Point }
  xw:=0.3100;
  yw:=0.3160;
  zw:=1-xw-yw;
  { Matrix Cxr, Sequence Y Cb Cr }
  Cyr[1,1]:= 0.2990; Cyr[1,2]:= 0.5870; Cyr[1,3]:= 0.1140;
  Cyr[2,1]:=-0.1687; Cyr[2,2]:=-0.3313; Cyr[2,3]:=+0.5000;
  Cyr[3,1]:= 0.5000; Cyr[3,2]:=-0.4187; Cyr[3,3]:=-0.0813;
  { Matrix Cry }
  HoInvers (3,Cyr,Cry,D,flag);

  Assign (prn,'C:\CiMalcYC.txt'); ReWrite(prn);

  Writeln (prn,'      Matrix Cyr');
  Writeln (prn,Cyr[1,1]:12:4, Cyr[1,2]:12:4, Cyr[1,3]:12:4);
  Writeln (prn,Cyr[2,1]:12:4, Cyr[2,2]:12:4, Cyr[2,3]:12:4);
  Writeln (prn,Cyr[3,1]:12:4, Cyr[3,2]:12:4, Cyr[3,3]:12:4);
  Writeln (prn,'');
  Writeln (prn,'      Matrix Cry');
  Writeln (prn,Cry[1,1]:12:4, Cry[1,2]:12:4, Cry[1,3]:12:4);
  Writeln (prn,Cry[2,1]:12:4, Cry[2,2]:12:4, Cry[2,3]:12:4);
  Writeln (prn,Cry[3,1]:12:4, Cry[3,2]:12:4, Cry[3,3]:12:4);
  Close(prn);
  Readln;
End.
```

Matrix Cyr			
Y	0.2990	0.5870	0.1140
Cb	-0.1687	-0.3313	0.5000
Cr	0.5000	-0.4187	-0.0813

Note
This is a linear conversion, as used for JPEG
In TV systems the conversion is different

Matrix Cry			
R	1.0000	0.0000	1.4020
G	1.0000	-0.3441	-0.7141
B	1.0000	1.7722	0.0000

Note
Rounded for structural zeros

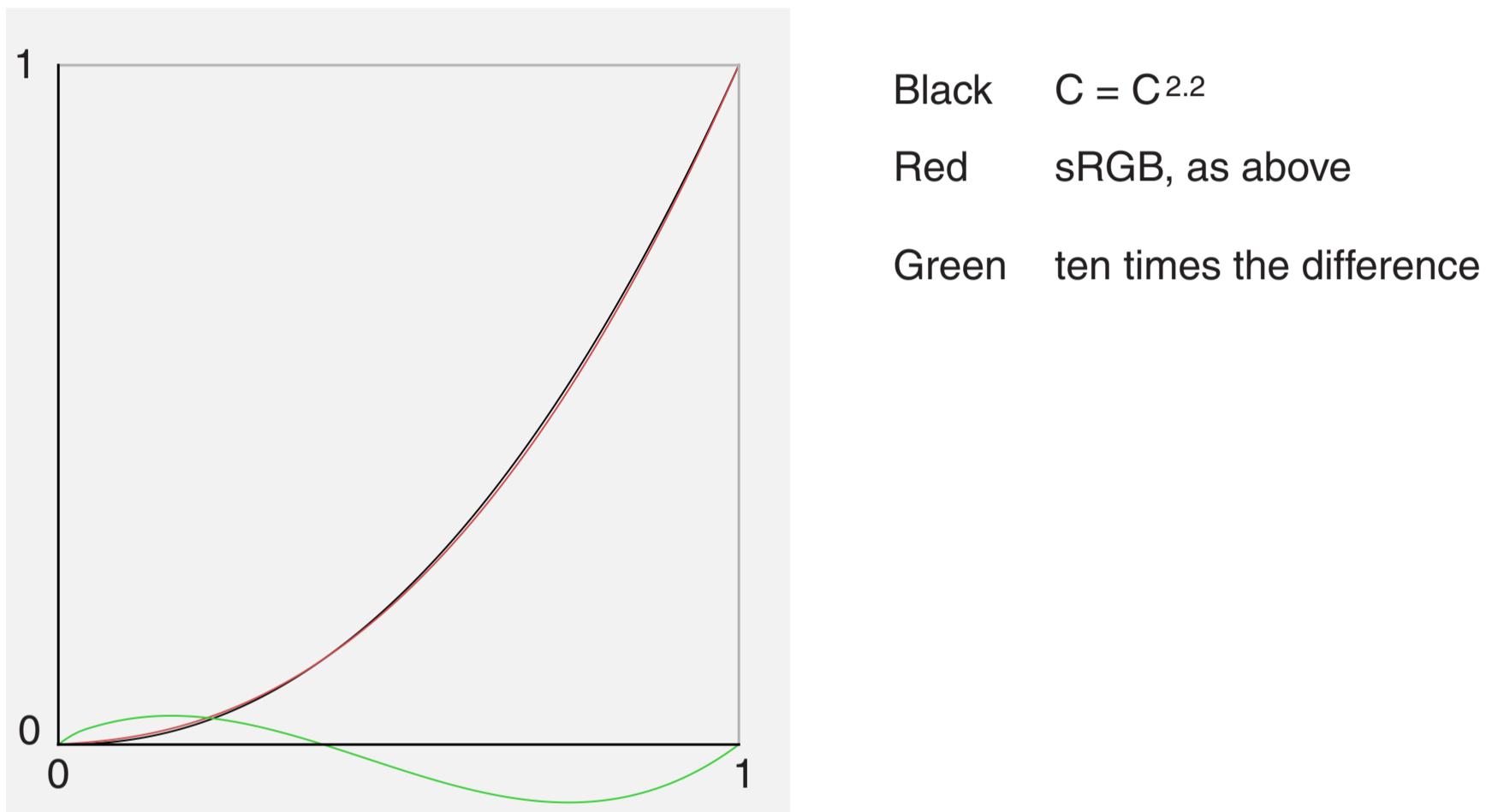
13. sRGB

sRGB is a standard color space, defined by companies, mainly Hewlett-Packard and Microsoft [9], [12].

The transformation of RGB image data to CIE XYZ requires primarily a Gamma correction, which compensates an expected inverse Gamma correction, compared to linear light data, here for normalized values $C = R,G,B = 0\dots 1$:

If $C \leq 0.03928$ Then $C = C/12.92$
Else $C = ((0.055+C)/1.055)^{2.4}$

The formula in the document [12] is misleading because a bracket was forgotten.



The conversion for D65 RGB to D65 XYZ uses the matrix on page 14, ITU-R BT.709 Primaries. D65 XYZ means XYZ without changing the illuminant.

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{D65} = \begin{bmatrix} 0.4124 & 0.3576 & 0.1805 \\ 0.2126 & 0.7152 & 0.0722 \\ 0.0193 & 0.1192 & 0.9505 \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}_{D65}$$

The conversion for D65 RGB to D50 XYZ applies additionally (by multiplication) the Bradford correction, which takes the adaptation of the eyes into account. This correction is an improved alternative to the Von Kries correction [1].

Monitors are assumed D65, but for printed paper the standard illuminant is D50. Therefore this transformation is recommended if the data are used for printing:

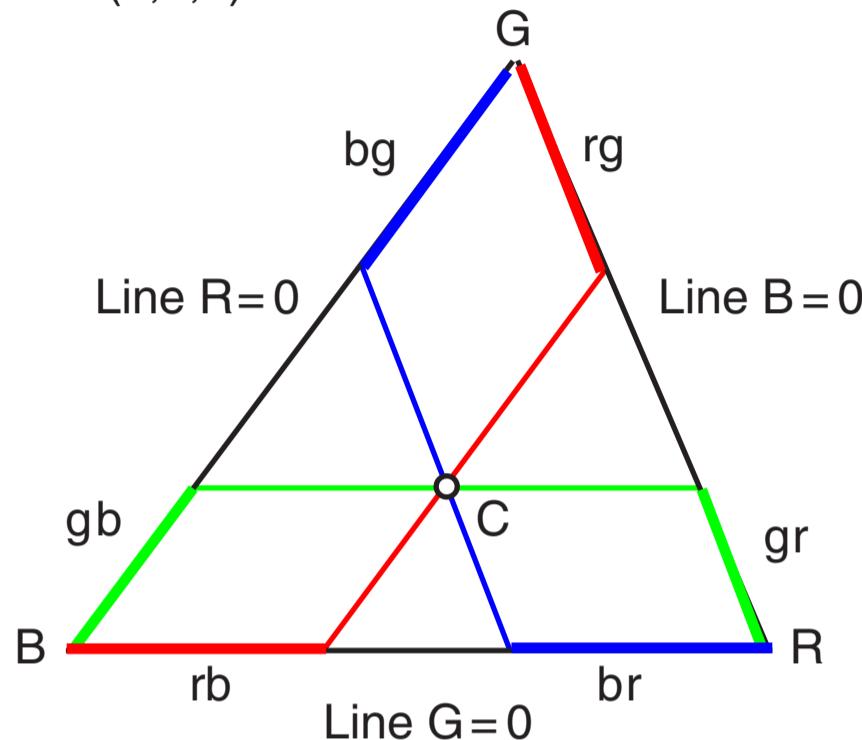
$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix}_{D50} = \begin{bmatrix} 0.4361 & 0.3851 & 0.1431 \\ 0.2225 & 0.7169 & 0.0606 \\ 0.0139 & 0.0971 & 0.7141 \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}_{D65}$$

14.1 Barycentric Coordinates / Concept

The corners R,G,B of a triangular gamut, e.g. for a monitor, are described in CIE xyY by three vectors $\mathbf{r}, \mathbf{g}, \mathbf{b}$ which have two components x,y each.

A color C is described either by \mathbf{c} with two values c_x, c_y or by three values R,G,B. These are the barycentric coordinates of C.

All points inside and on the triangle are reachable by $0 \leq R, G, B \leq 1$. Points outside have at least one negative coordinate. The corners R,G,B have barycentric coordinates (1,0,0), (0,1,0) and (0,0,1).



$$rg = R \underline{RG}$$

$$rb = R \underline{RB}$$

$$gr = G \underline{GR}$$

$$gb = G \underline{GB}$$

$$bg = B \underline{BG}$$

$$br = B \underline{BR}$$

Underline means length of ..

$$(1) \mathbf{c} = R\mathbf{r} + G\mathbf{g} + B\mathbf{b}$$

$$(2) 1 = R + G + B$$

Substitute R in (1) by (2):

$$(3) R = 1 - G - B$$

$$(4) G(g-r) + B(b-r) = c - r$$

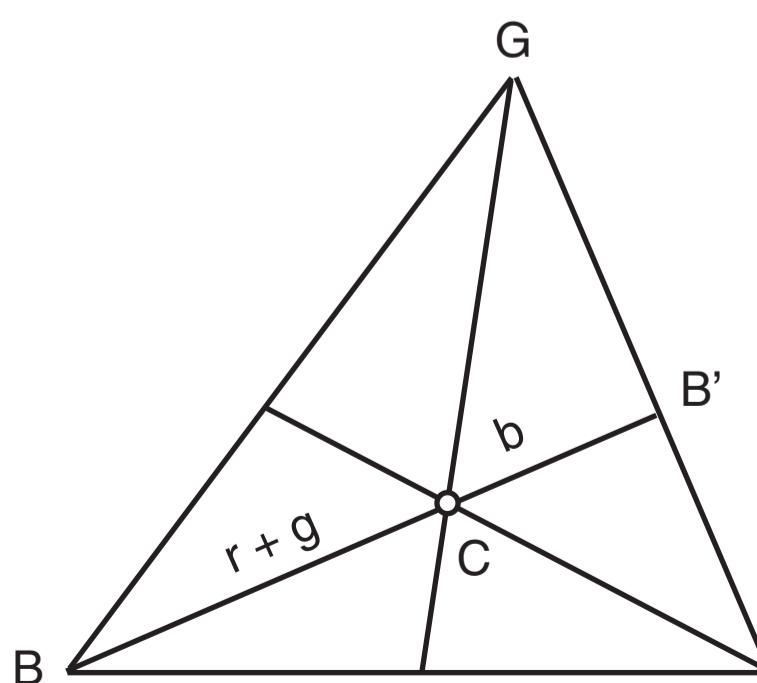
(4) consists of two linear equations for G,B, which can be solved by *Cramer's rule*.

R is calculated by (3).

$(g-r)$ and $(b-r)$ are the edge vectors from R to G and R to B .

The edge vectors are used in (4) as a vector base.

Any point inside the triangle is reached by $G + B < 1$, which leads to $R + G + B = 1$.



$$r+g = (R+G) \underline{BB'}$$

$$b = B \underline{BB'}$$

14.2 Barycentric Coordinates / Wrong

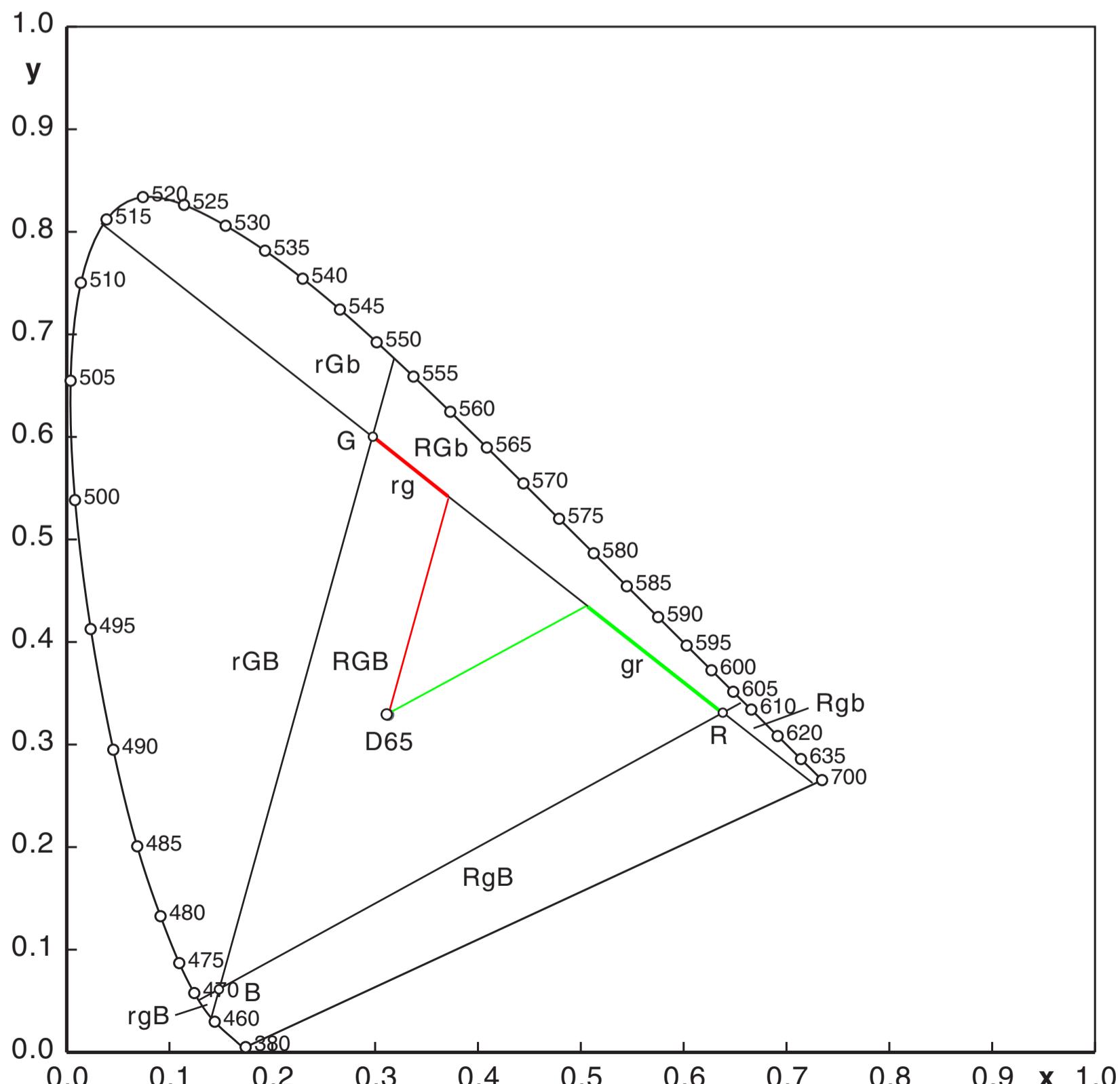
So far the barycentric coordinates remind much to the explanations in [3], chapter 3.2.2. It should be possible to find the relative values R,G,B for a given point $\mathbf{c}=(c_x, c_y)$ by measuring the proportions $R=rg/RG$, $G=gr/GR$ with $RG=GR$, then $B=1-R-G$.

Unfortunately this interpretation is wrong. The drawing shows the D65 white point and the measurable values $R=0.219$, $G=0.385$ and $B=0.396$ instead of the correct values $R=1/3$, $G=1/3$, $B=1/3$.

The base vectors **R,G,B** in CIE XYZ (chapter 4 for CIE primaries) do not have the same lengths. In [3] the mathematics were explained for unit vectors.

So far it is not clear, how the geometrically interpretation for barycentric coordinates could be applied to the actual task.

The diagram below shows additionally seven sectors. 'RGB' means, all values are positive (inside the triangle). 'rGB' means $R<0$, $G>0$, $B>0$ and so on. Negative values are not prohibited by the definition of coordinates. They just do not appear in technical RGB system. Of course they are essential for the color matching theory.



15. Optimal Primaries

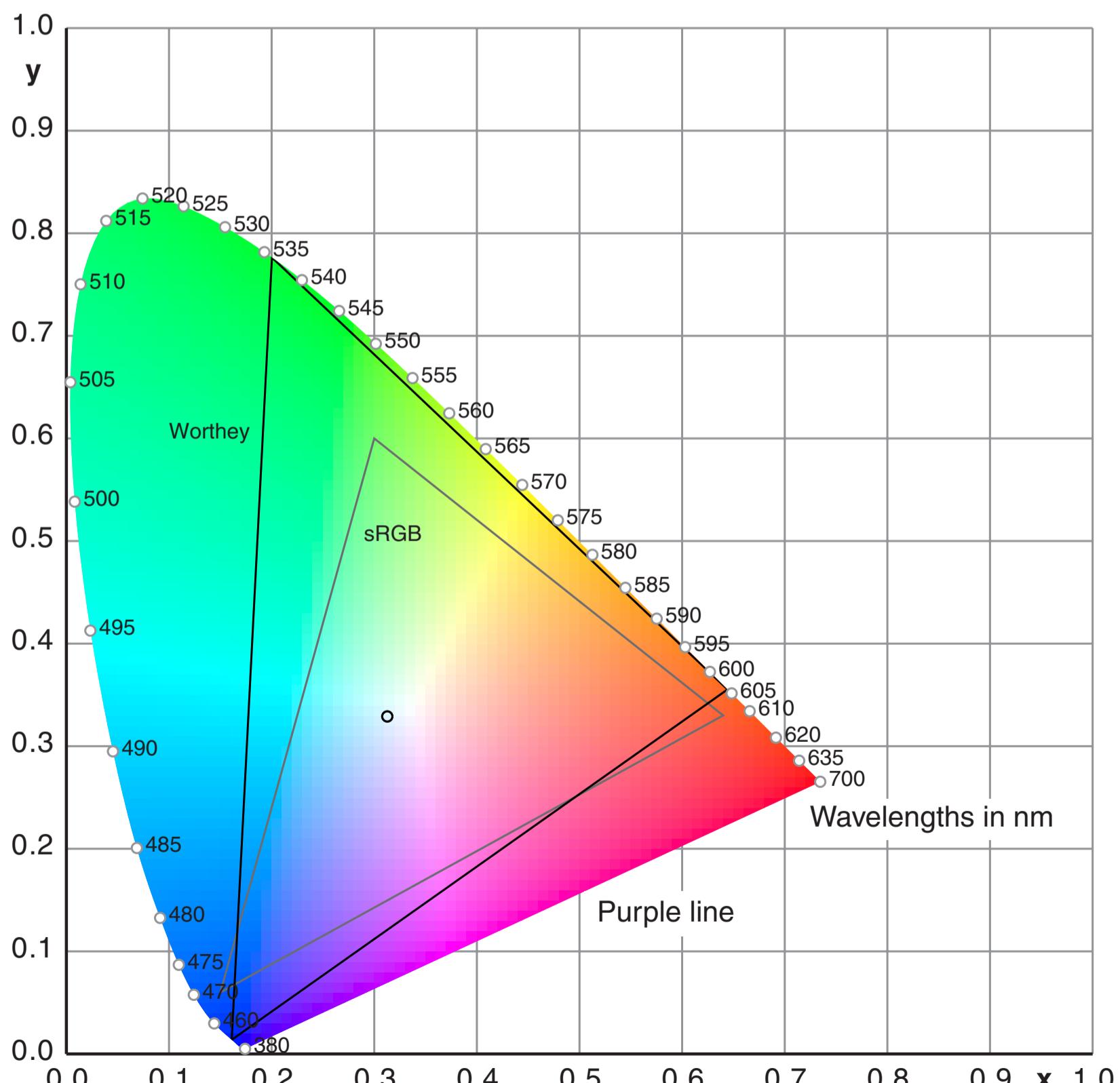
James A. Worhey had shown in recent publications [18] how to find optimal primaries. This approach is based on 'Amplitude not left out'. Which primaries should be used if the power is limited for each light source ?

The resulting wavelengths are shown by the corners of the triangle below: 445, 536, 604 nm. At least, the wavelengths should be near to these values.

For a real system (besides tests in a laboratory) pure spectral colors cannot be used. The corners have to be shifted on a radius towards the white point (which is here indicated by the circle for D65).

The optimal red at 604nm is hardly a good candidate for technical systems – it is more a kind of orange instead of vibrant red.

Additional illustrations for J.Worhey's concepts are shown in [19]. Everything PostScript vector graphics.



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Appendix A Color Matching

The calculation by program ColCalc [21] shows colors as defined by equal distances in CIELab. The corresponding values are drawn in the chromaticity diagram.

BlueGreen (4) can be matched by positive weights RGB for CIE primaries.

Vibrant BlueGreen (2) requires negative R. BlueGreen (1) is out of human gamut.

RGB values are here normalized for 0...100.

ColorCalc G.Hoffmann Dec.06 / 2006		Med.White: Ref.White: Input:	Eq.Energy D50 Lab	Primaries: Trc: Bradford:	CIE 1.0 No	Intent:	AbsCol		
X	0.090936	0.124317	0.165004	0.213721	0.271192	0.338140	0.415287	0.503358	0.603075
Y	0.281233	0.281233	0.281233	0.281233	0.281233	0.281233	0.281233	0.281233	0.281233
Z	1.271889	0.902067	0.611932	0.391815	0.232047	0.122959	0.054882	0.018146	0.001827
x	0.055312	0.095071	0.155933	0.241011	0.345700	0.455510	0.552683	0.627052	0.680568
y	0.171060	0.215073	0.265774	0.317144	0.358500	0.378851	0.374278	0.350343	0.317371
z	0.773627	0.689856	0.578293	0.441845	0.295800	0.165639	0.073039	0.022605	0.002062
L*	60.0000	60.0000	60.0000	60.0000	60.0000	60.0000	60.0000	60.0000	60.0000
a*	-100.0000	-75.0000	-50.0000	-25.0000	0.0000	25.0000	50.0000	75.0000	100.0000
b*	-100.0000	-75.0000	-50.0000	-25.0000	0.0000	25.0000	50.0000	75.0000	100.0000
R	-63.2553	-38.0477	-14.8426	6.9838	28.0552	48.9952	70.4276	92.9761	117.3231
G	46.7170	41.7155	37.0448	32.5818	28.2034	23.7865	19.2082	14.3453	9.0636
B	127.9629	90.6690	61.4185	39.2362	23.1472	12.1761	5.3480	1.6875	0.0930
R'	0.0000	0.0000	0.0000	6.9838	28.0552	48.9952	70.4276	92.9761	100.0000
G'	46.7170	41.7155	37.0448	32.5818	28.2034	23.7865	19.2082	14.3453	9.0636
B'	100.0000	90.6690	61.4185	39.2362	23.1472	12.1761	5.3480	1.6875	0.0930
CCT	none	none	none	12527 K	5001 K	2504 K	none	none	none
RGB	out-gam	out-gam	out-gam	in-gam	in-gam	in-gam	in-gam	in-gam	out-gam

Matrix Crx

2.364998	-0.896709	-0.468149
-0.515142	1.426371	0.088744
0.005202	-0.014403	1.008898

Matrix Cxr

0.489921	0.310016	0.200063
0.176937	0.812422	0.010641
0.000000	0.009999	0.990301

Appendix B Further Explanations for Chapter 5

Chapter 5 has always been enigmatic - since the beginning about ten years ago . Now I am very grateful to Monsieur Jean-Yves Chasle for giving further explanations, here posted unchanged.

Photometric luminance of color (page 4)

The CIE Photopic Luminous Efficiency function V is related to r_bar, g_bar and b_bar:

$$V(\lambda) = 1.0000 * r_{\text{bar}}(\lambda) + 4.5907 * g_{\text{bar}}(\lambda) + 0.0601 * b_{\text{bar}}(\lambda) \quad (1)$$

The theoretical light efficacy k equals 683 lm/W, based on the luminous flux measured at around 555 nm where $V(\lambda)$ equals 1. As on page 4, considering a light with a spectral power diffusion P in W/sr.m², the photometric luminance (in cd/m²) can be calculated as:

$$L = k * \int \{ P(\lambda) * V(\lambda) * d\lambda \} \quad (2)$$

where k is the efficacy of the source light.

Substituting (1) in (2):

$$\begin{aligned} L &= k * \int \{ P(\lambda) * (1.0000 * r_{\text{bar}}(\lambda) + 4.5907 * g_{\text{bar}}(\lambda) + 0.0601 * b_{\text{bar}}(\lambda)) * d\lambda \} \\ &= 1.0000 * k * \int \{ P(\lambda) * r_{\text{bar}}(\lambda) * d\lambda \} + 4.5907 * k * \int \{ P(\lambda) * g_{\text{bar}}(\lambda) * d\lambda \} + \\ &\quad 0.0601 * k * \int \{ P(\lambda) * b_{\text{bar}}(\lambda) * d\lambda \} \end{aligned}$$

Using notations from page 4 (in cd/m²):

$$L = 1.0000 * R + 4.5907 * G + 0.0601 * B \quad (3)$$

in cd/m².

The photometric luminance (in cd/m²) can be separated in terms of tristimulus values Lr, Lg and Lb:

$$L_r = 1.0000 * R \quad (4)$$

$$L_g = 4.5907 * G \quad (5)$$

$$L_b = 0.0601 * B \quad (6)$$

Lr, Lg and Lb represent the photometric luminance (in cd/m²) at each wavelength (700, 546.1 and 435.8 respectively). These luminances are reported on the graph named „R,G,B“ on page 4 and 6 for a matched white light of coordinates (1,1,1) in the CIE RGB space.

In practice, the light efficacy k is less than 683 lm/W. In [1], Hunt publishes samples of this value depending on the light type (page 75-79, and table 4.2 page 97).

Application (page 6)

These results can be applied on page 6, where X = 1, Y = 0 and Z = 0 representing X in the CIE XYZ space is converted to the CIE RGB space in order to evaluate its photometric luminance at each wavelength (700, 546.1 and 435.8 respectively):

$$R = +2.36461 * X - 0.89654 * Y - 0.46807 * Z = +2.36461$$

$$G = -0.51517 * X + 1.42641 * Y + 0.08876 * Z = -0.51517$$

$$B = +0.00520 * X - 0.01441 * Y + 1.00920 * Z = +0.00520$$

in colorimetric luminance of red, green and blue.

From (4), (5) and (6):

$$L_r = 1.0000 * R = 1.0000 * +2.36461 = +2.36461$$

$$L_g = 4.5907 * G = 4.5907 * -0.51517 = -2.36499$$

$$L_b = 0.0601 * B = 0.0601 * +0.00520 = +0.00031$$

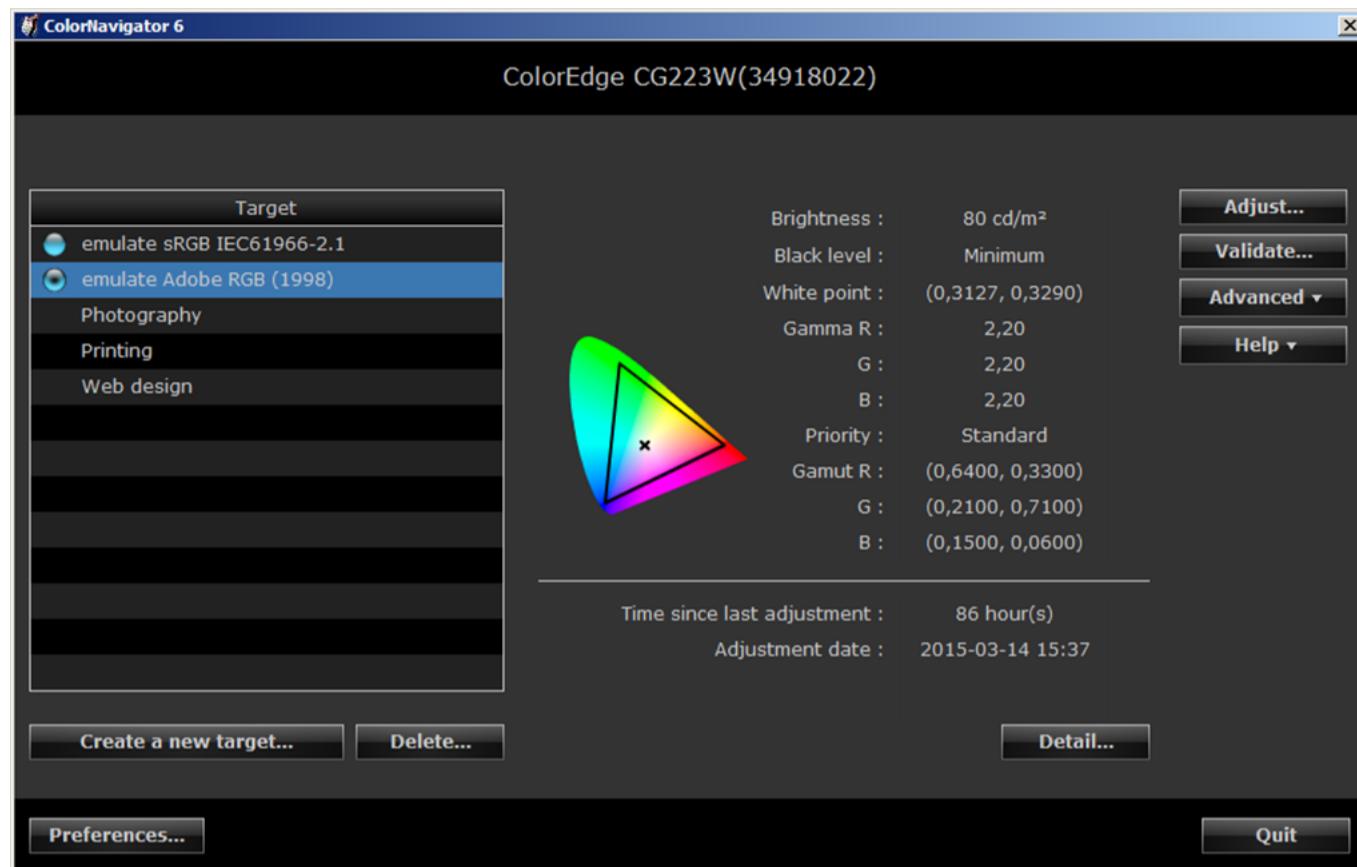
(in cd/m²)

These luminances are reported on the graph named „X“ on page 6. Using (3), they sum to 0 as expected.

Same calculations for Y and Z, leading to the graphs named „Y“ and „Z“ on page 6.

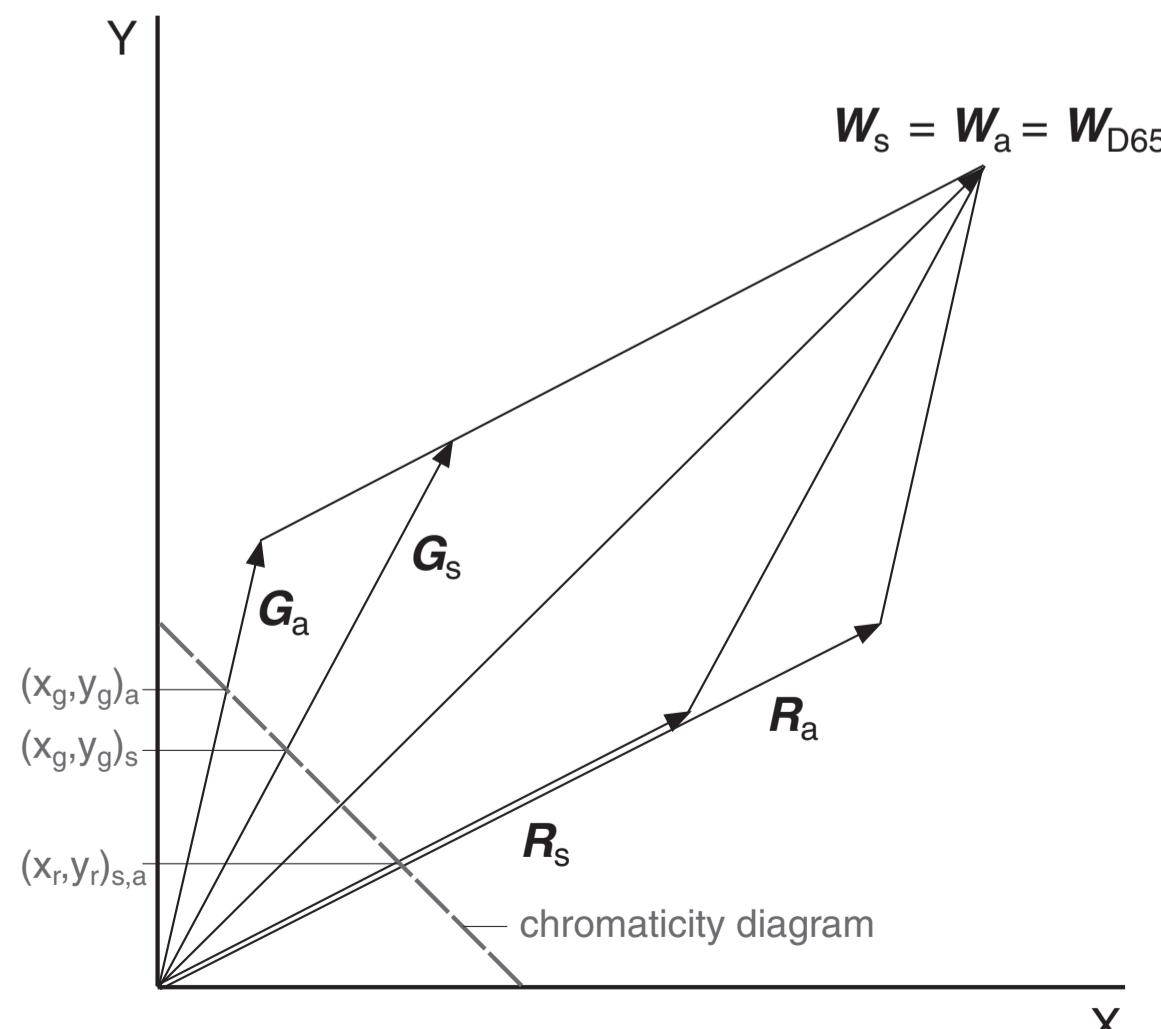
Appendix C Compare Primaries sRGB and Adobe RGB

On a wide gamut monitor one can choose alternatively sRGB and aRGB (abbreviation for Adobe RGB), more exactly: emulations for these working spaces as monitor profiles.



Switching from sRGB to aRGB, one can see that for the whole screen content not only the greens but also the reds and blues become more vibrant. According to p.2 it seems that the red primaries for both spaces are identical, and the blue primaries as well. But that is not true – only the chromaticity coordinates are identical, not the base vectors themselves.

R, G and B are the primaries in CIE XYZ. R, G and B are weight factors in the range 0 to 1. A color **C** is given by $\mathbf{C} = \mathbf{R}\mathbf{R} + \mathbf{G}\mathbf{G} + \mathbf{B}\mathbf{B}$. For $\mathbf{R} = \mathbf{G} = 1$ we get white, here D65 white for sRGB and aRGB. The situation is visualized below in 2D, Z is omitted. Coming from sRGB, \mathbf{G}_s is shifted to \mathbf{G}_a . The new primary \mathbf{R}_a has the same chromaticity coordinates as \mathbf{R}_s , but the vector has to be longer longer. Thus aRGB red is more vibrant than sRGB red for the same R.



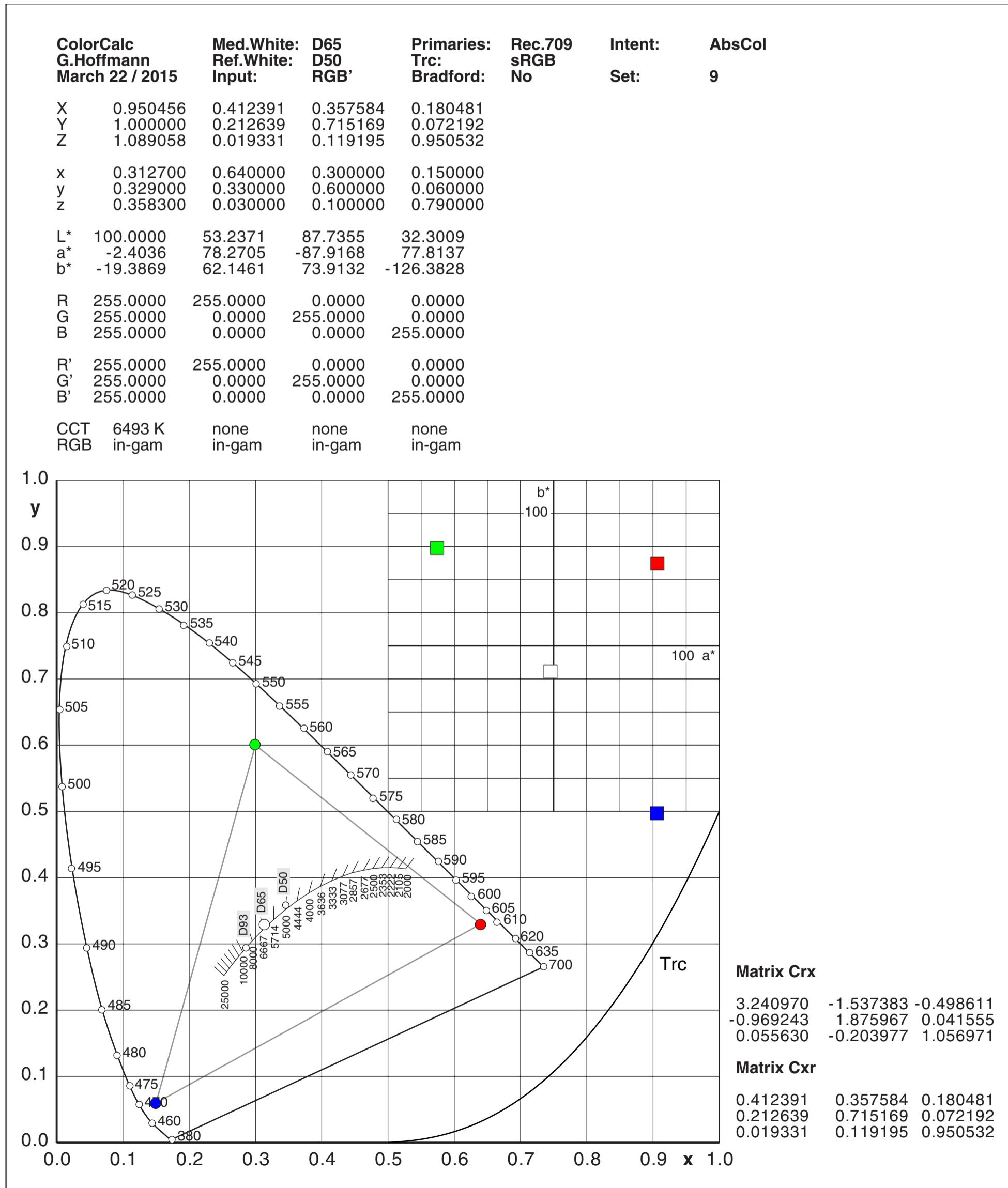
The components X, Y and Z for any primary are found in the matrices \mathbf{C}_{xr} , as column vectors, see p.18 and p.19.

$$\mathbf{C}_{xr} = (\mathbf{R} \ \mathbf{G} \ \mathbf{B})$$

Two-dimensional visualization of the three-dimensional situation

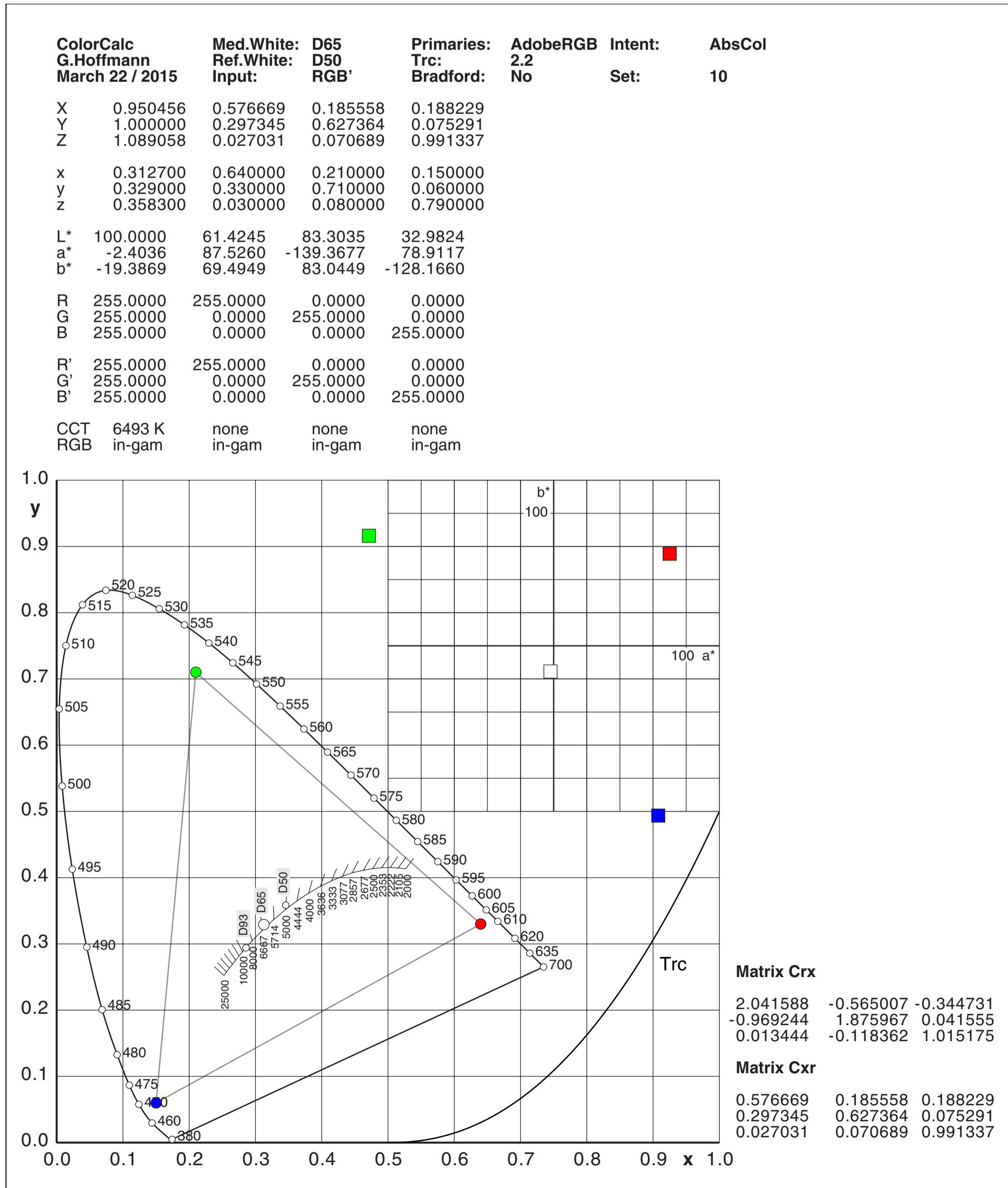
Appendix C Compare Primaries...cont. sRGB-noCAT

Whereas the primaries red and blue have the same chromaticity coordinates in sRGB and aRGB, they are in fact different in CIE XYZ and in CIELab. Here we have all color parameters for sRGB. sRGB white is D65 (first column). Reference white in CIELab is D50. No chromatic adaptation transform is applied (Bradford). The tone reproduction curve (TRC) is that of srRGB: a linear slope for small values and a power function with exponent 2.4 for large values, which leads to an effective TRC with exponent 2.2. Input for all calculations is RGB.



Appendix C Compare Primaries...cont. aRGB-noCAT

Here we have all color parameters for aRGB. aRGB white is D65 (first column). Reference white in CIELab is D50. No chromatic adaptation transform is applied (Bradford). The tone reproduction curve (TRC) is that of aRGB: a power function with exponent 2.2. Input for all calculations is RGB.



Appendix C Compare Primaries... aRGB+sRGB-noCAT

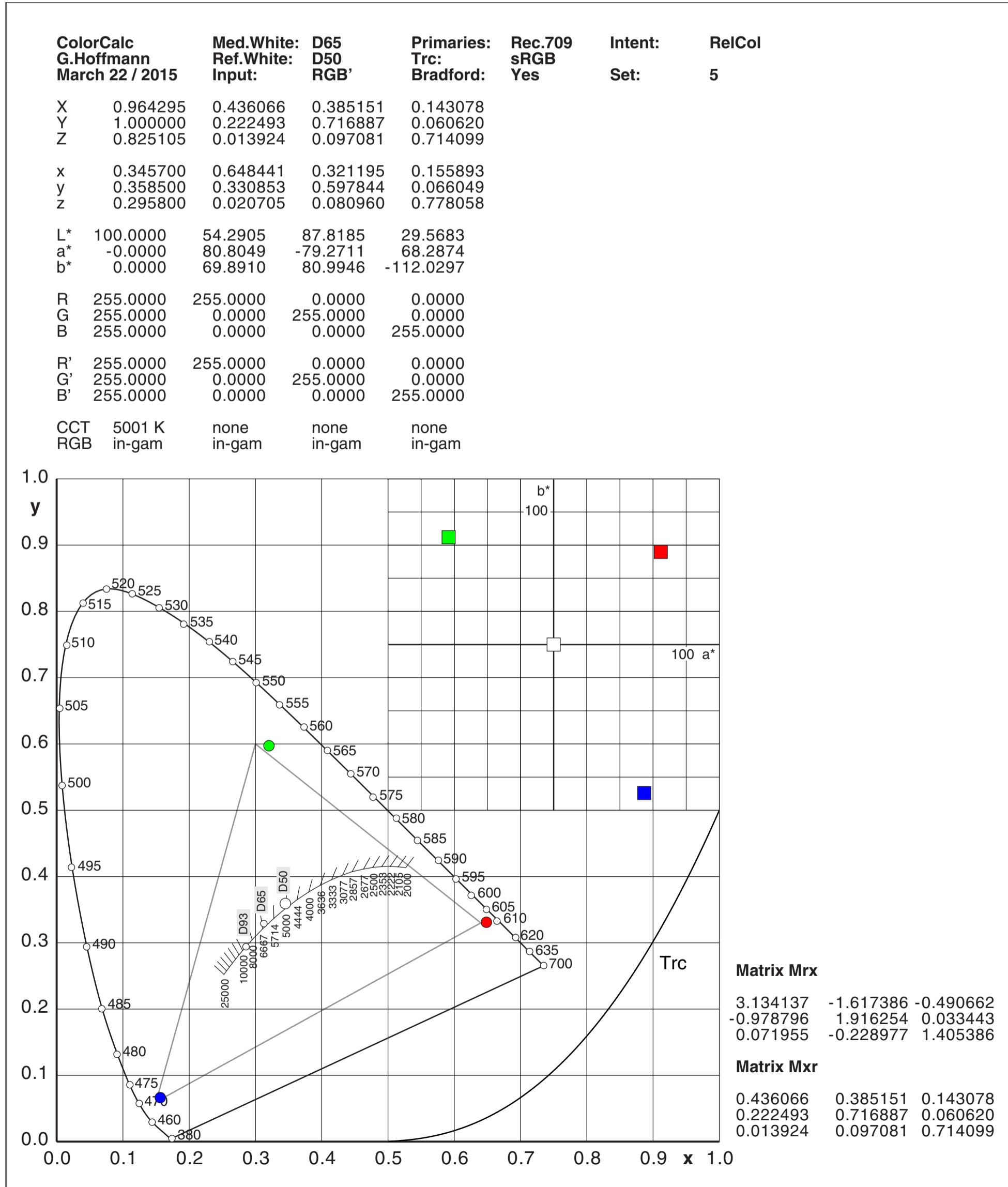
Here we have all color parameters for aRGB and sRGB. No chromatic adaptation transform is applied (Bradford). The tone reproduction curve (TRC) is that of aRGB: a power function with exponent 2.2. Input for all calculations is XYZ (values taken from previous calculations). Now we can compare aRGB directly with sRGB. Green and red are more vibrant in aRGB, compared to sRGB. Blue is practically not affected. a^* for aRGB-green exceeds the code range -128 for negative numbers. $R'G'B'$ are the inverse gamma encoded values (like a squareroot function).

ColorCalc G.Hoffmann March 23 / 2015	aRGB				sRGB		
	Med.White: Ref.White: Input:	D65 D50 XYZ	Primaries: Trc: Bradford:	AdobeRGB 2.2 No	Intent: Set:	AbsCol	
X	0.950456	0.576669	0.185558	0.188229	0.412391	0.357584	0.180481
Y	1.000000	0.297345	0.627364	0.075291	0.212639	0.715169	0.072192
Z	1.089058	0.027031	0.070689	0.991337	0.019331	0.119195	0.950532
x	0.312700	0.640000	0.210000	0.150000	0.640000	0.300000	0.150000
y	0.329000	0.330000	0.710000	0.060000	0.330000	0.600000	0.060000
z	0.358300	0.030000	0.080000	0.790000	0.030000	0.100000	0.790000
L*	100.0000	61.4245	83.3035	32.9823	53.2371	87.7355	32.3008
a*	-2.4035	87.5260	-139.3679	78.9123	78.2706	-87.9169	77.8142
b*	-19.3869	69.4952	83.0449	-128.1662	62.1459	73.9131	-126.3829
R	255.0000	255.0000	-0.0002	0.0003	182.3571	72.6427	0.0002
G	254.9999	0.0000	255.0002	-0.0003	-0.0001	255.0002	-0.0002
B	255.0001	-0.0001	0.0000	254.9999	0.0000	10.4963	244.5037
R'	255.0000	255.0000	0.0000	0.4995	218.9528	144.0969	0.3777
G'	255.0000	0.0916	255.0000	0.0000	0.0000	255.0000	0.0000
B'	255.0000	0.0000	0.1164	254.9999	0.2246	59.8090	250.1742
CCT	6493 K	none	none	none	none	none	none
RGB	in-gam	in-gam	in-gam	in-gam	in-gam	in-gam	in-gam

<img alt="A 2D plot showing color space coordinates (x, y) for various colors. The x-axis ranges from 0.0 to 1.0, and the y-axis ranges from 0.0 to 1.0. A grid is overlaid on the plot. Several points are plotted with their corresponding color swatches: a green point at approximately (0.48, 0.71), a blue point at approximately (0.22, 0.71), a red point at approximately (0.92, 0.88), and a black point at approximately (0.92, 0.88). Numerous other points are labeled with their coordinates, such as 500, 510, 515, 520, 525, 530, 535, 540, 545, 550, 555, 560, 565, 570, 575, 580, 585, 590, 595, 600, 605, 610, 615, 620, 635, 650, 660, 670, 680, 690, 700, 710, 720, 730, 740, 750, 760, 770, 780, 790, 800, 810, 820, 830, 840, 850, 860, 870, 880, 890, 900, 910, 920, 930, 940, 950, 960, 970, 980, 990, 1000, 1010, 1020, 1030, 1040, 1050, 1060, 1070, 1080, 1090, 1100, 1110, 1120, 1130, 1140, 1150, 1160, 1170, 1180, 1190, 1200, 1210, 1220, 1230, 1240, 1250, 1260, 1270, 1280, 1290, 1300, 1310, 1320, 1330, 1340, 1350, 1360, 1370, 1380, 1390, 1400, 1410, 1420, 1430, 1440, 1450, 1460, 1470, 1480, 1490, 1500, 1510, 1520, 1530, 1540, 1550, 1560, 1570, 1580, 1590, 1600, 1610, 1620, 1630, 1640, 1650, 1660, 1670, 1680, 1690, 1700, 1710, 1720, 1730, 1740, 1750, 1760, 1770, 1780, 1790, 1800, 1810, 1820, 1830, 1840, 1850, 1860, 1870, 1880, 1890, 1900, 1910, 1920, 1930, 1940, 1950, 1960, 1970, 1980, 1990, 2000, 2010, 2020, 2030, 2040, 2050, 2060, 2070, 2080, 2090, 2100, 2110, 2120, 2130, 2140, 2150, 2160, 2170, 2180, 2190, 2200, 2210, 2220, 2230, 2240, 2250, 2260, 2270, 2280, 2290, 2300, 2310, 2320, 2330, 2340, 2350, 2360, 2370, 2380, 2390, 2400, 2410, 2420, 2430, 2440, 2450, 2460, 2470, 2480, 2490, 2500, 2510, 2520, 2530, 2540, 2550, 2560, 2570, 2580, 2590, 2600, 2610, 2620, 2630, 2640, 2650, 2660, 2670, 2680, 2690, 2700, 2710, 2720, 2730, 2740, 2750, 2760, 2770, 2780, 2790, 2800, 2810, 2820, 2830, 2840, 2850, 2860, 2870, 2880, 2890, 2900, 2910, 2920, 2930, 2940, 2950, 2960, 2970, 2980, 2990, 3000, 3010, 3020, 3030, 3040, 3050, 3060, 3070, 3080, 3090, 3100, 3110, 3120, 3130, 3140, 3150, 3160, 3170, 3180, 3190, 3200, 3210, 3220, 3230, 3240, 3250, 3260, 3270, 3280, 3290, 3300, 3310, 3320, 3330, 3340, 3350, 3360, 3370, 3380, 3390, 3400, 3410, 3420, 3430, 3440, 3450, 3460, 3470, 3480, 3490, 3500, 3510, 3520, 3530, 3540, 3550, 3560, 3570, 3580, 3590, 3600, 3610, 3620, 3630, 3640, 3650, 3660, 3670, 3680, 3690, 3700, 3710, 3720, 3730, 3740, 3750, 3760, 3770, 3780, 3790, 3800, 3810, 3820, 3830, 3840, 3850, 3860, 3870, 3880, 3890, 3900, 3910, 3920, 3930, 3940, 3950, 3960, 3970, 3980, 3990, 4000, 4010, 4020, 4030, 4040, 4050, 4060, 4070, 4080, 4090, 4100, 4110, 4120, 4130, 4140, 4150, 4160, 4170, 4180, 4190, 4200, 4210, 4220, 4230, 4240, 4250, 4260, 4270, 4280, 4290, 4300, 4310, 4320, 4330, 4340, 4350, 4360, 4370, 4380, 4390, 4400, 4410, 4420, 4430, 4440, 4450, 4460, 4470, 4480, 4490, 4500, 4510, 4520, 4530, 4540, 4550, 4560, 4570, 4580, 4590, 4600, 4610, 4620, 4630, 4640, 4650, 4660, 4670, 4680, 4690, 4700, 4710, 4720, 4730, 4740, 4750, 4760, 4770, 4780, 4790, 4800, 4810, 4820, 4830, 4840, 4850, 4860, 4870, 4880, 4890, 4900, 4910, 4920, 4930, 4940, 4950, 4960, 4970, 4980, 4990, 5000, 5010, 5020, 5030, 5040, 5050, 5060, 5070, 5080, 5090, 5100, 5110, 5120, 5130, 5140, 5150, 5160, 5170, 5180, 5190, 5200, 5210, 5220, 5230, 5240, 5250, 5260, 5270, 5280, 5290, 5300, 5310, 5320, 5330, 5340, 5350, 5360, 5370, 5380, 5390, 5400, 5410, 5420, 5430, 5440, 5450, 5460, 5470, 5480, 5490, 5500, 5510, 5520, 5530, 5540, 5550, 5560, 5570, 5580, 5590, 5600, 5610, 5620, 5630, 5640, 5650, 5660, 5670, 5680, 5690, 5700, 5710, 5720, 5730, 5740, 5750, 5760, 5770, 5780, 5790, 5800, 5810, 5820, 5830, 5840, 5850, 5860, 5870, 5880, 5890, 5900, 5910, 5920, 5930, 5940, 5950, 5960, 5970, 5980, 5990, 6000, 6010, 6020, 6030, 6040, 6050, 6060, 6070, 6080, 6090, 6100, 6110, 6120, 6130, 6140, 6150, 6160, 6170, 6180, 6190, 6200, 6210, 6220, 6230, 6240, 6250, 6260, 6270, 6280, 6290, 6300, 6310, 6320, 6330, 6340, 6350, 6360, 6370, 6380, 6390, 6400, 6410, 6420, 6430, 6440, 6450, 6460, 6470, 6480, 6490, 6500, 6510, 6520, 6530, 6540, 6550, 6560, 6570, 6580, 6590, 6600, 6610, 6620, 6630, 6640, 6650, 6660, 6670, 6680, 6690, 6700, 6710, 6720, 6730, 6740, 6750, 6760, 6770, 6780, 6790, 6800, 6810, 6820, 6830, 6840, 6850, 6860, 6870, 6880, 6890, 6900, 6910, 6920, 6930, 6940, 6950, 6960, 6970, 6980, 6990, 7000, 7010, 7020, 7030, 7040, 7050, 7060, 7070, 7080, 7090, 7100, 7110, 7120, 7130, 7140, 7150, 7160, 7170, 7180, 7190, 7200, 7210, 7220, 7230, 7240, 7250, 7260, 7270, 7280, 7290, 7300, 7310, 7320, 7330, 7340, 7350, 7360, 7370, 7380, 7390, 7400, 7410, 7420, 7430, 7440, 7450, 7460, 7470, 7480, 7490, 7500, 7510, 7520, 7530, 7540, 7550, 7560, 7570, 7580, 7590, 7600, 7610, 7620, 7630, 7640, 7650, 7660, 7670, 7680, 7690, 7700, 7710, 7720, 7730, 7740, 7750, 7760, 7770, 7780, 7790, 7800, 7810, 7820, 7830, 7840, 7850, 7860, 7870, 7880, 7890, 7900, 7910, 7920, 7930, 7940, 7950, 7960, 7970, 7980, 7990, 8000, 8010, 8020, 8030, 8040, 8050, 8060, 8070, 8080, 8090, 8100, 8110, 8120, 8130, 8140, 8150, 8160, 8170, 8180, 8190, 8200, 8210, 8220, 8230, 8240, 8250, 8260, 8270, 8280, 8290, 8300, 8310, 8320, 8330, 8340, 8350, 8360, 8370, 8380, 8390, 8400, 8410, 8420, 8430, 8440, 8450, 8460, 8470, 8480, 8490, 8500, 8510, 8520, 8530, 8540, 8550, 8560, 8570, 8580, 8590, 8600, 8610, 8620, 8630, 8640, 8650, 8660, 8670, 8680, 8690, 8700, 8710, 8720, 8730, 8740, 8750, 8760, 8770, 8780, 8790, 8800, 8810, 8820, 8830, 8840, 8850, 8860, 8870, 8880, 8890, 8900, 8910, 8920, 8930, 8940, 8950, 8960, 8970, 8980, 8990, 9000, 9010, 9020, 9030, 9040, 9050, 9060, 9070, 9080, 9090, 9100, 9110, 9120, 9130, 9140, 9150, 9160, 9170, 9180, 9190, 9200, 9210, 9220, 9230, 9240, 9250, 9260, 9270, 9280, 9290, 93

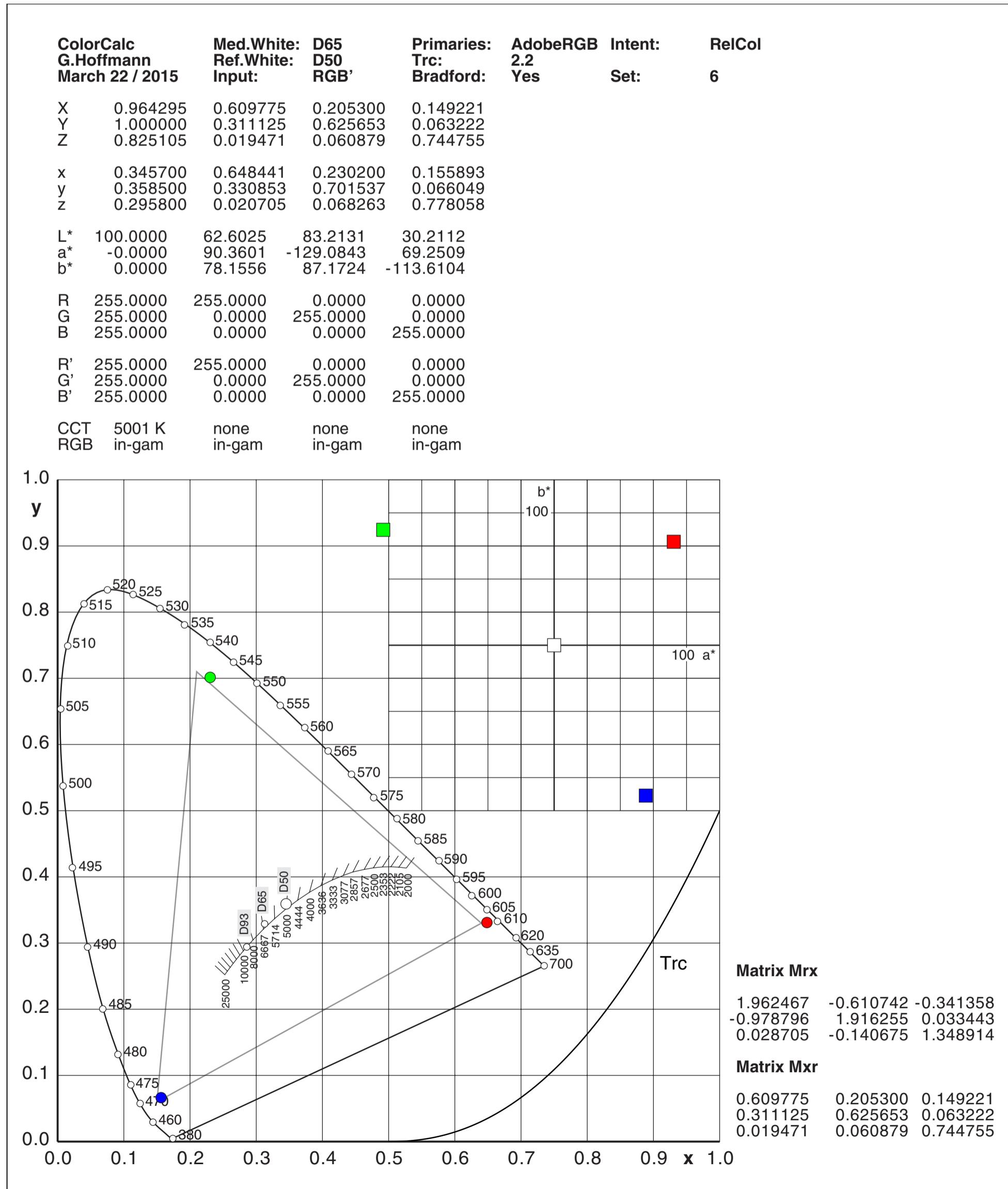
Appendix C Compare Primaries...cont. sRGB-CAT

The chromatic adaptation transform (CAT) type Bradford is applied. The Input is RGB. The graphic shows so-called adapted primaries for sRGB. This mode is used by Photoshop.



Appendix C Compare Primaries...cont. aRGB-CAT

The chromatic adaptation transform (CAT) type Bradford is applied. The Input is RGB. The graphic shows so-called adapted primaries for aRGB. This mode is used by Photoshop.



Appendix C Compare Primaries... aRGB+sRGB-CAT

The chromatic adaptation transform (CAT) type Bradford is applied. The Input is now XYZ. The values have to be taken from the two previous pages.

The graphic shows so-called adapted primaries for aRGB and sRGB. This mode is used by Photoshop. For instance:

in aRGB we can get sRGB-red by 219/0/0, -green by 144/255/60 and -blue by 0/0/250.

In aRGB we see aRGB-green with $a^*=-129$ just outside the code range -128.

